



PAST PRESENT AND FUTURE CHALLENGES IN THE DETERMINATION OF THE STRUCTURE OF THE PROTON

LECTURE I

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Grad Days 2019

Scope of the lectures

Give an overview on our understanding on the structure of the proton: from Feynman parton model to modern QCD picture

Introduce basic concepts and techniques behind the determination of the structure of the proton from experimental data

Wealth of ingredients involved: perturbative QCD, experimental measurements, statistical and mathematical problems, higher order predictions, phenomenology tools, machine learning.

Discuss PDF-related phenomenology at the Large Hadron Collider and beyond

Discuss current frontiers and challenges

Disclaimer: these lectures are far from providing a complete picture of the topic. You can find complementary information in excellent lectures on PDFs from W. Giele, G. Salam, A. Martin, P. Nadolsky, S. Forte, D. Stump, W. Melnitchouk, D. Stump, A. Guffanti, J. Rojo ... at recent graduate schools

References

- G. Ridolfi "Notes on deep-inelastic scattering and the Parton model"
- S. Forte lectures
- Ellis, Stirling and Webber "QCD and collider physics"
- G. Dissertori, I. Knowles, M. Schmelling "Quantum Chromo Dynamics"
- J. Gao, L. Harland-Lang, J. Rojo *Phys.Rept.* 742 (2018) 1-121
- S. Forte, G. Watt Ann.Rev.Nucl.Part.Sci. 63 (2013)
- S. Forte, Acta Phys.Polon. B41 (2010) 2859
- E. Perez, E. Rizvi, *Rep.Prog.Phys.* 76 (2013) 046201.
- A. Accardi, et al., *Eur. Phys. J.* C76 (8) (2016) 471
- A. De Roeck, R. S. Thorne, Prog.Part.Nucl.Phys. 66 (2011) 727
- http://pdg.lbl.gov/2017/reviews/rpp2017-rev-structure-functions.pdf

List of references complemented by specific references during the lectures

Outline

• First lecture (Today)

- Second lecture (Tuesday)
 - Experimental Data
 - Disentangling proton's components
 - Statistics and Methodology
- Third lecture (Wednesday)
 - Fits and methodology
 - The NNPDF approach
- Fourth lecture (Thursday)
 - New frontiers and challenges

- Motivation: the big picture
- Parton Model and QCD
- Collinear Factorisation

Standard Model of particle physics

- Standard Model (SM) of particle physics one of the greatest triumph of Quantum Field Theories in the past century
- SM remarkably successful theory: no convincing deviations so far from its predictions



Some compelling questions



Some compelling questions



Some compelling questions



Super-Kamiokande observation of neutrino oscillations, 2004

A unique opportunity

- The Large Hadron Collider at CERN most powerful accelerator ever built
- Extremely successful Run I (7-8 TeV) and great performance at Run II (13-14 TeV)
- As luminosity increases, stronger probe on known processes (Higgs, Flavour anomalies...) & larger mass reach



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A new precision era in particle physics



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- Theoretical predictions to catch up with precision of experimental data



A new precision era in particle physics

- •Theoretical predictions to catch up with precision of experimental data



The precision ingredients

$$\sigma^{\text{th}} = \hat{\sigma}[\mathcal{O}(1) + \mathcal{O}(\alpha_s) + \mathcal{O}(\alpha_s^2) + ...] \otimes f_1 \otimes f_2 + \mathcal{O}\left(\frac{\Lambda^2}{Q^2}\right)$$
• Hard scattering of partons or Partonic cross section (Perturbative QCD+EW)
• Parton Distribution Functions
• Parton Showering and Hadronization
• Multiple Parton Interaction, Underlying Events





Gavin Salam lectures, Quy Nhon Vietnam 2018

Slide from Gavin Salam lectures Quy Nhon Vietnam 2018

$$\sigma(pp \to H) = (961 \text{ pb}) \times (\alpha_s^2 + 10.4\alpha_s^3 + 38\alpha_s^4 + 48\alpha_s^5 + \cdots)$$
$$\alpha_s \equiv \alpha_s(M_H/2)$$
$$\sqrt{s_{pp}} = 13 \text{ TeV}$$

Anastasiou et al., 1602.00695 (ggF, hEFT)

pp→H (via gluon fusion) is one of only two hadron-collider processes known at N3LO (the other is pp→H via weak-boson fusion)

The series does not converge well (explanations for why are only moderately convincing)

- On previous page, we wrote the series in terms of powers of $\alpha_{\rm S}(M_{\rm H}/2)$
- But we are free to rewrite it in terms of $\alpha_{\rm S}(\mu)$ for any choice of renormalisation scale μ





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Convention: "theory uncertainty" (i.e. from missing higher orders) is estimated by change of cross section when varying μ in range 1/2 \rightarrow 2 around central value ₇₄



Here, only the renorm. scale $\mu(=\mu_R)$ has been varied. In real life you need to change renorm. and factorisation (μ_F) scales.

Scale dependence as the <u>theory uncertainty</u> or <u>Missing Higher Order</u> <u>Uncertainty (MHOU)</u>

Convention: "theory uncertainty" (i.e. from missing higher orders) is estimated by change of cross section when varying µ in range 1/2 → 2 around central value



- LO: almost all processes
- NLO: most processes (automated calculations)
- NNLO: all $2 \rightarrow 1$, most $2 \rightarrow 2$ (explosion of calculations in the past few years)
- N3LO: Higgs gluon fusion and Higgs via vector boson fusion

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Yellow Report 3 (2013)



PDF uncertainties limiting factor in the accuracy of theoretical predictions

Higgs physics

Yellow Report 4 (2016)



Reduced (still often dominant) PDF uncertainties

Determination of SM parameters



ATLAS collaboration, EPJC 78 (2018) 110

 $\eta = -\ln \tan(\theta/2)$

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Channel	$m_{W^+} - m_{W^-}$ [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
$W \rightarrow ev$	-29.7	17.5	0.0	4.9	0.9	5.4	0.5	0.0	24.1	30.7
$W \to \mu \nu$	-28.6	16.3	11.7	0.0	1.1	5.0	0.4	0.0	26.0	33.2
Combined	-29.2	12.8	3.3	4.1	1.0	4.5	0.4	0.0	23.9	28.0



PDF uncertainties are a limiting factor in the accuracy of theoretical predictions, both within **SM** and **beyond**



Historia magistra vitae est

Discrepancy between QCD calculations and CDF jet data (1995)

At that time there was no information on PDF uncertainties and the theoretical prediction strongly depends on gluon shape at x>0.1

FINAL CTEQ FIT (1998)



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The parton model and QCD

Historic overview

 <u>1955</u>: Hofstadter et al observed first deviations in scattering of electron off proton from simple point-like Mott scattering → Finite radius of proton ~ 0.7 fm



Historic overview

 <u>1964</u>: Zweig and Gell-Mann independently postulated existence of three aces (Zweig) or quarks (Gell-Mann) with fractional electric charge and spin-1/2 to explain proliferation of mesons and baryons in nucleon collision experiments. More of a mathematical model rather than particles! How could such objects be bound so tightly together?



Historic overview

 <u>1967</u>: First deep-inelastic scattering experiments at SLAC 20 GeV linear accelerator gave first evidence of point-like elementary constituents which were later identified as quarks (Bjorken scaling)











Bosons	k_V	V_{lV}	A_{lV}
γ	e_l	1	0
	$1/(2\sin\theta_W\cos\theta_W)$	$I_3^l - 2e_l \sin^2 \theta_W$	$-I_3^l$
W^{\pm}	$V_{ll'}/(2\sqrt{2}\sin heta_W)$	1	-1

Table 1.1: Coupling of fermions to the weak bosons. Here e_l is the electric charge measured in unit of the positron charge, I_3^l is the third component of the weak isospin, +1/2 for up-type quarks or neutrinos and -1/2 for down-type quarks or charged leptons. For charged current interactions involving quarks, the coefficients $V_{ll'}$ of the Cabibbo-Kobayashi-Maskawa matrix [18]-[19] are involved. The parameter $\sin \theta_W$ is the Weinberg mixing angle.









The surprising results at SLAC was that F1,2 did not vanish as Q2 increased, rather they remained finite and constant and depended only on xB - Bjorken scaling (1969)



Such scaling demonstrated that the exchanged vector boson (photon) scatters off point-like objects that have no mass or scale associated. The lepton scatters off charged spin 1/2 constituents (partons) that carry a fraction x of proton momentum











Exercise I: Z contribution

 Show that, in the Parton model, considering also the contribution of a virtual Z boson and its interference with the photon one obtains:

$$F_2^{\gamma,Z}(x) = x \sum_{\substack{i=1\\n_f}}^{n_f} c_i [q_i(x) + \bar{q}_i(x)]$$
$$F_3^{\gamma,Z}(x) = \sum_{\substack{i=1\\i=1}}^{n_f} d_i [q_i(x) - \bar{q}_i(x)]$$

Where

$$c_{i} = e_{i}^{2} - 2e_{i}V_{eZ}V_{iZ}P_{Z} + (V_{eZ}^{2} + A_{eZ}^{2})(V_{iZ}^{2} + A_{iZ}^{2})P_{Z}^{2}$$

$$d_{i} = -2e_{i}A_{eZ}A_{iZ}P_{Z} + 4V_{eZ}A_{eZ}V_{iZ}A_{iZ}P_{Z}^{2}$$

$$P_{Z} = \frac{Q^{2}}{(Q^{2} + M_{Z}^{2})(4s_{w}^{2}c_{w}^{2})} \xrightarrow{c_{w} = \cos\theta_{w}} s_{w} = \sin\theta_{w}$$

Exercise II: Paschos-Wolfenstein relation

• Show that, in the Parton model, considering a (anti)neutrino-initiated DIS process on a deuteron target – assuming SU(2) isospin symmetry $u_n(x)=d_p(x)$ and $d_n(x)=u_p(x)$ – the ratio R

$$R = \frac{\sigma_{\rm NC}(\nu) - \sigma_{\rm NC}(\bar{\nu})}{\sigma_{\rm CC}(\nu) - \sigma_{\rm CC}(\bar{\nu})}$$

NC (mediated by Z) and CC (mediated by W^{+/-}), assuming strange and anti-strange to be equal in the target, is independent of Parton Distribution Functions and can be used to determined the Weinberg angle θ_W

$$R = \frac{1}{2} \left(\frac{1}{2} - \sin \theta_w^2 \right)$$

You may use (without deriving it) the result (and set c, cbar = 0)

$$F_{2}^{W^{-}} = 2x(u + \bar{d} + \bar{s} + c),$$

$$F_{3}^{W^{-}} = 2x(u - \bar{d} - \bar{s} + c),$$

$$F_{2}^{W^{+}} = 2x(d + \bar{u} + \bar{c} + s),$$

$$F_{3}^{W^{+}} = 2x(d - \bar{u} - \bar{c} + s),$$



The structure of the proton has been a crucial ingredient to test and verify perturbative QCD and it is now key to the precision challenge that we are facing at the LHC

➡ Today's lecture

Parametrisation of the proton in terms of structure functions

✓ Parton model picture

✓ (QCD - Improved parton model)

✓ (DGLAP evolution equations)

✓ (Collinear Factorisation Theorem)

Extra material

Slide from F Olness lectures CTEQ school 2017

Slide from Gavin Salam lectures Quy Nhon Vietnam 2018

$$\frac{\sigma(e^+e^- \to \text{hadrons})}{\sigma(e^+e^- \to \mu^+\mu^-)} = [\alpha_s \equiv \alpha_s(\sqrt{s_{e^+e^-}})]$$
$$= R_0 \left(1 + 0.32\alpha_s + 0.14\alpha_s^2 - 0.47\alpha_s^3 - 0.59316\alpha_s^4 + \cdots\right)$$
Baikov et al., 1206.1288
(numbers for γ -exchange only)

This is one of the few quantities calculated to N4LO Good convergence of the series at every order (at least for $\alpha_s(M_z) = 0.118$)