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UNIVERSITÀ DI MILANO & INFN



UNIVERSITÀ DEGLI STUDI DI MILANO
DIPARTIMENTO DI FISICA



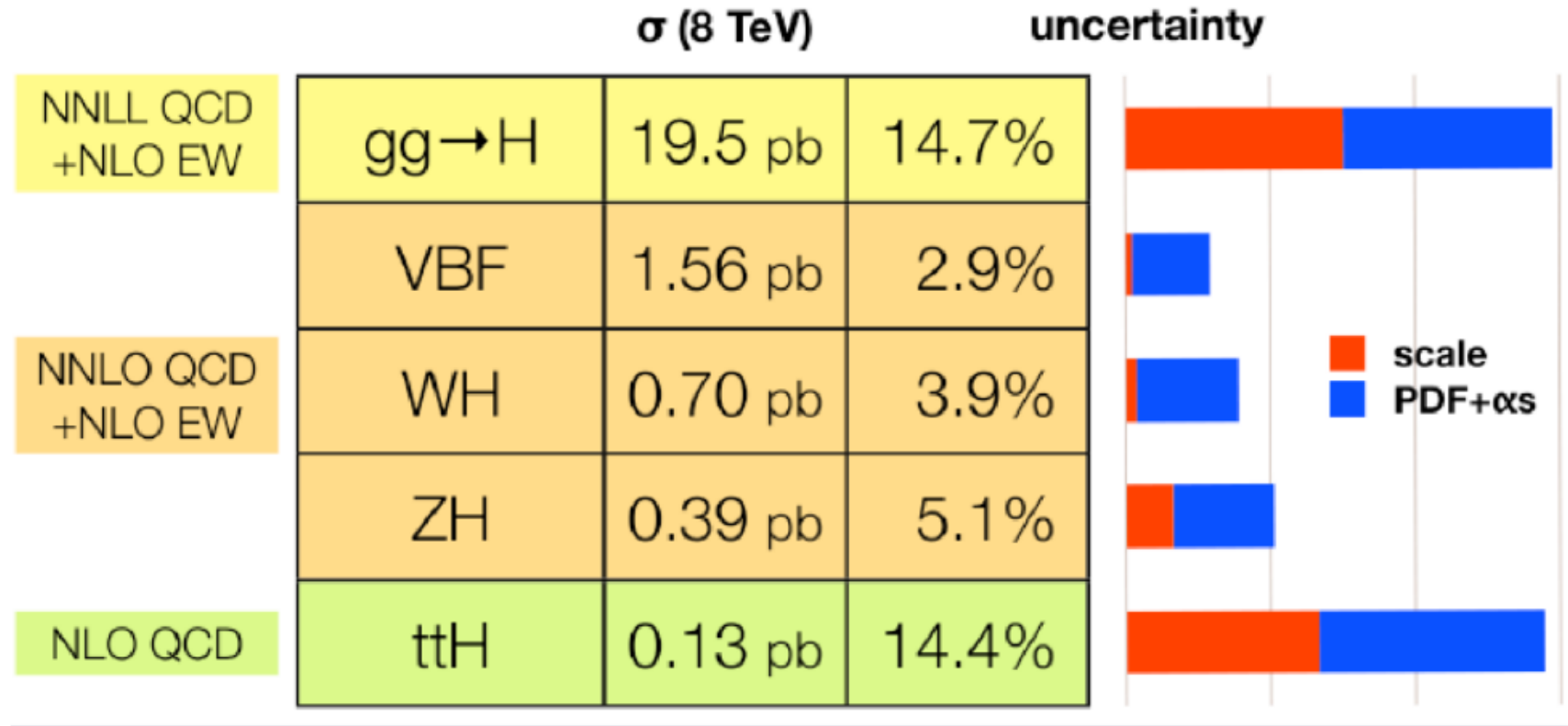
UNIVERSITÄT FREIBURG

JANUARY 10, 2018

PROLOGUE

PAST (NOT SO LONG AGO)

HIGGS PRODUCTION

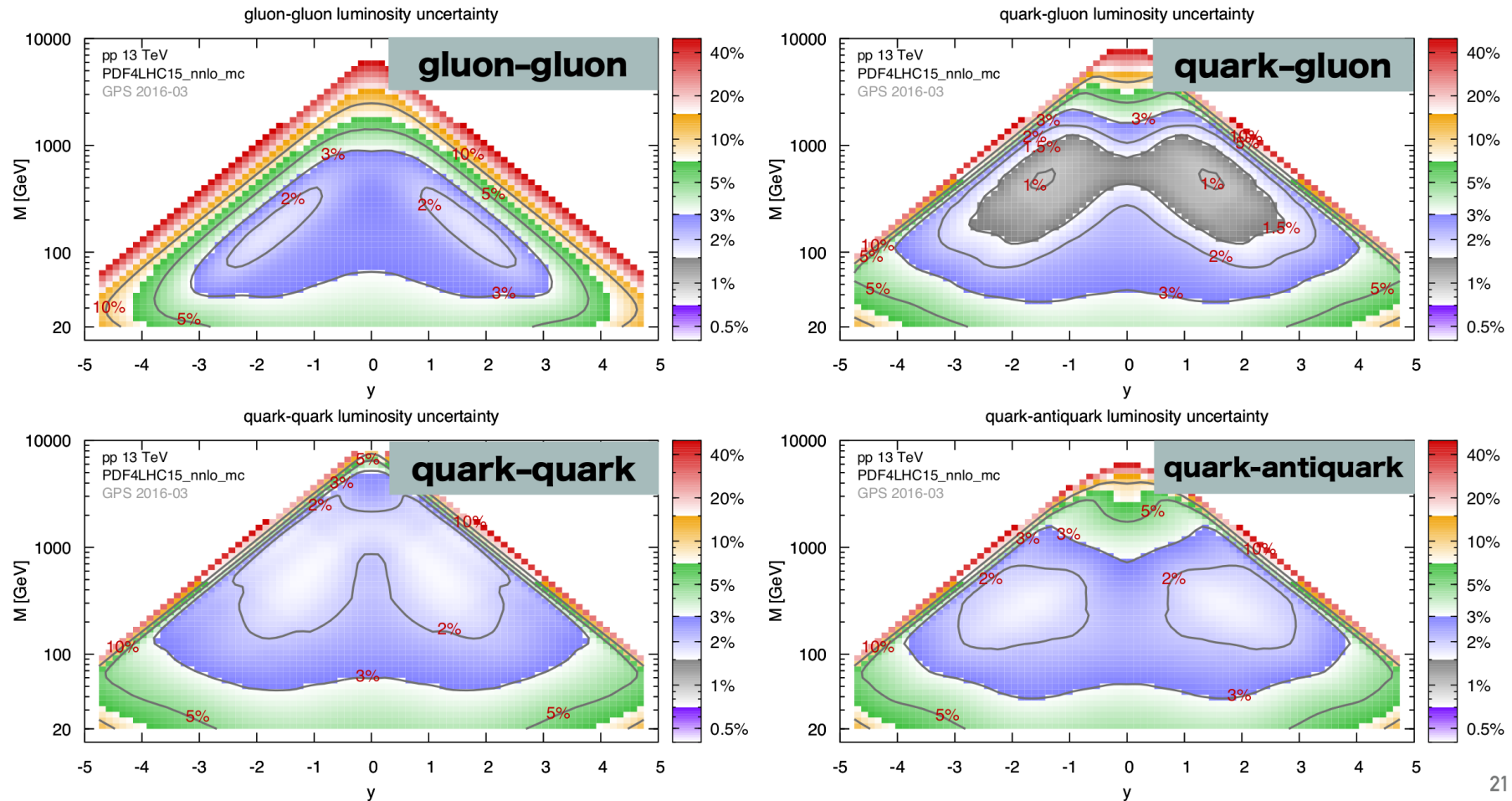


(J. Campbell, 2012)

PDF UNCERTAINTY EITHER DOMINANT, OR VERY LARGE, OR BOTH
 TYPICAL PDF UNCERTAINTY $\sim 5 - 10\%$

PRESENT: THE PDF4LHC SET

LUMINOSITY UNCERTAINTIES VS RAPIDITY & MASS



21

G.P. Salam, 2016

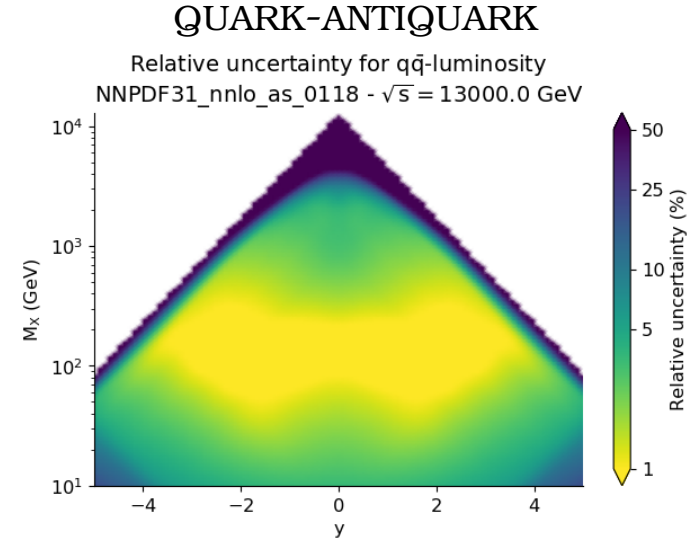
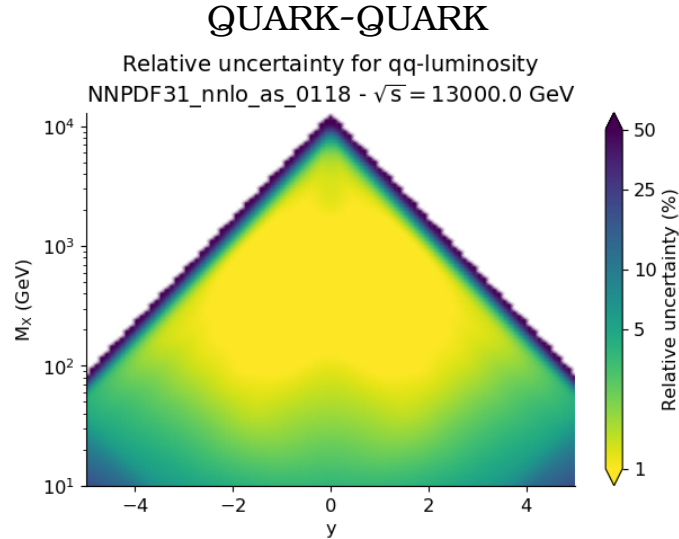
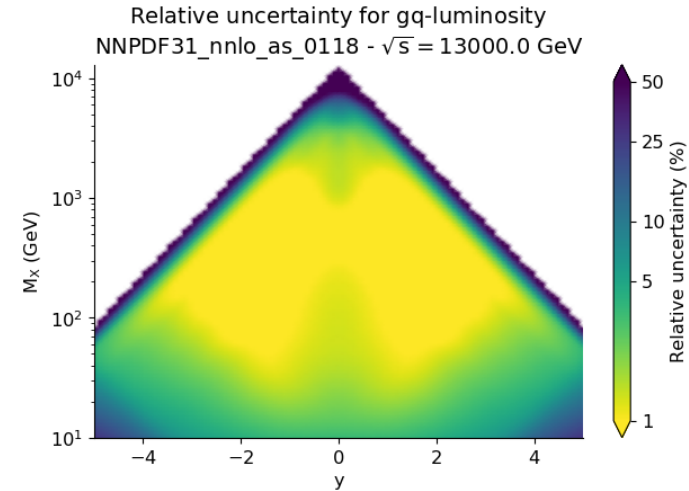
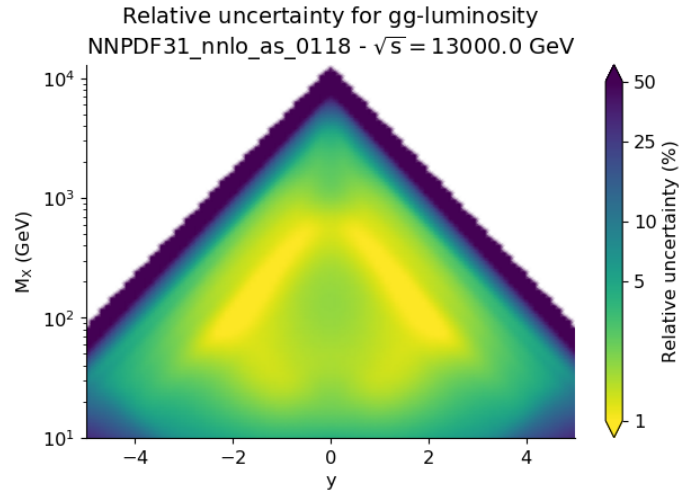
TYPICAL PDF UNCERTAINTY DOWN TO $\sim 2 - 5\%$
TOWARDS 1% PDF UNCERTAINTIES?

FUTURE: NNPDF3.1

LUMINOSITY UNCERTAINTIES VS RAPIDITY & MASS

GLUON-GLUON

QUARK-GLUON



TYPICAL PDF UNCERTAINTY IN DATA REGION OF ORDER 1% !!
CAN WE BELIEVE IN 1% PDF UNCERTAINTIES? WHAT ARE THE CONSEQUENCES?

SUMMARY

THE IMPACT OF DATA

- WIDENING OF THE DATASET AND THE IMPACT OF LHC
- PDF UNCERTAINTIES
- FLAVOR SEPARATION & THE GLUON

METHODOLOGICAL ISSUES

- MONTE CARLO VS. HESSIAN
- PARAMETRIZATION ISSUES
- MINIMIZATION EFFICIENCY AND STATISTICAL TESTS
- CONTROLLING THE COVARIANCE MATRIX

THEORY ISSUES

- THE NNLO FRONTIER
- SMALL AND LARGE x RESUMMATION
- THE PHOTON PDF
- THE TREATMENT OF HEAVY QUARKS

THE IMPACT OF LHC DATA

CONTEMPORARY PDF TIMELINE (ONLY PUBLISHED GLOBAL)

	2008		2009		2010		2011	2012		2013		2014		2015	2017	
SET	CTEG6.6	NNPDF1.0	MSTW	ABKM09	NNPDF2.0	CT10 (NLO)	NNPDF2.1 (NNLO)	ABM11	NNPDF2.3	CT10 (NNLO)	ABM12	NNPDF3.0	MMHT	CT14	ABMP16	NNPDF3.1
MONTH	(02)	(08)	(01)	(08)	(02)	(07)	(07)	(02)	(07)	(02)	(10)	(10)	(12)	(06)	(01)	(06)
F. T. DIS	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
ZEUS+H1-HI	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
COMB. HI	✗	✗	✗	✗	✓	✗	some	✗	✓	✗	✓	✓	✗	✗	✓	✓
ZEUS+H1-HII	✗	✗	✗	✗	✗	✗		✗	✗	some	✗	✓	✗	✗	✓	✓
HERA JETS	✗	✗	✓	✗	✗	✗	✗	✗	✗	✗	✗	✗	✓	✗	✗	✗
F. T. DY	✓	✗	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
TEV W+Z	✓	✗	✓	✗	✓	✓	✓	✗	✓	✓	✗	✓	✓	✓	✗	✓
LHC W+Z	✗	✗	✗	✗	✗	✗	✗	✗	✓	✗	some	✓	✓	✓	some	✓
TEV JETS	✓	✗	✓	✗	✓	✓	✗	✓	✓	✓	✗	✓	✓	✓	✗	✓
LHC JETS	✗	✗	✗	✗	✗	✗	✗	✗	✓	✗	✗	✓	✓	✓	✗	✓
TOP TOTAL	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✓	✓	✗	✗	✓	✓
SINGLE TOP TOTAL	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✓	✗
TOP DIFFERENTIAL	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✓
$W p_T$	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✓	✗	✗	✗	✗
W+C	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✓	✗	✗	✗	✗
$Z p_T$	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✗	✓

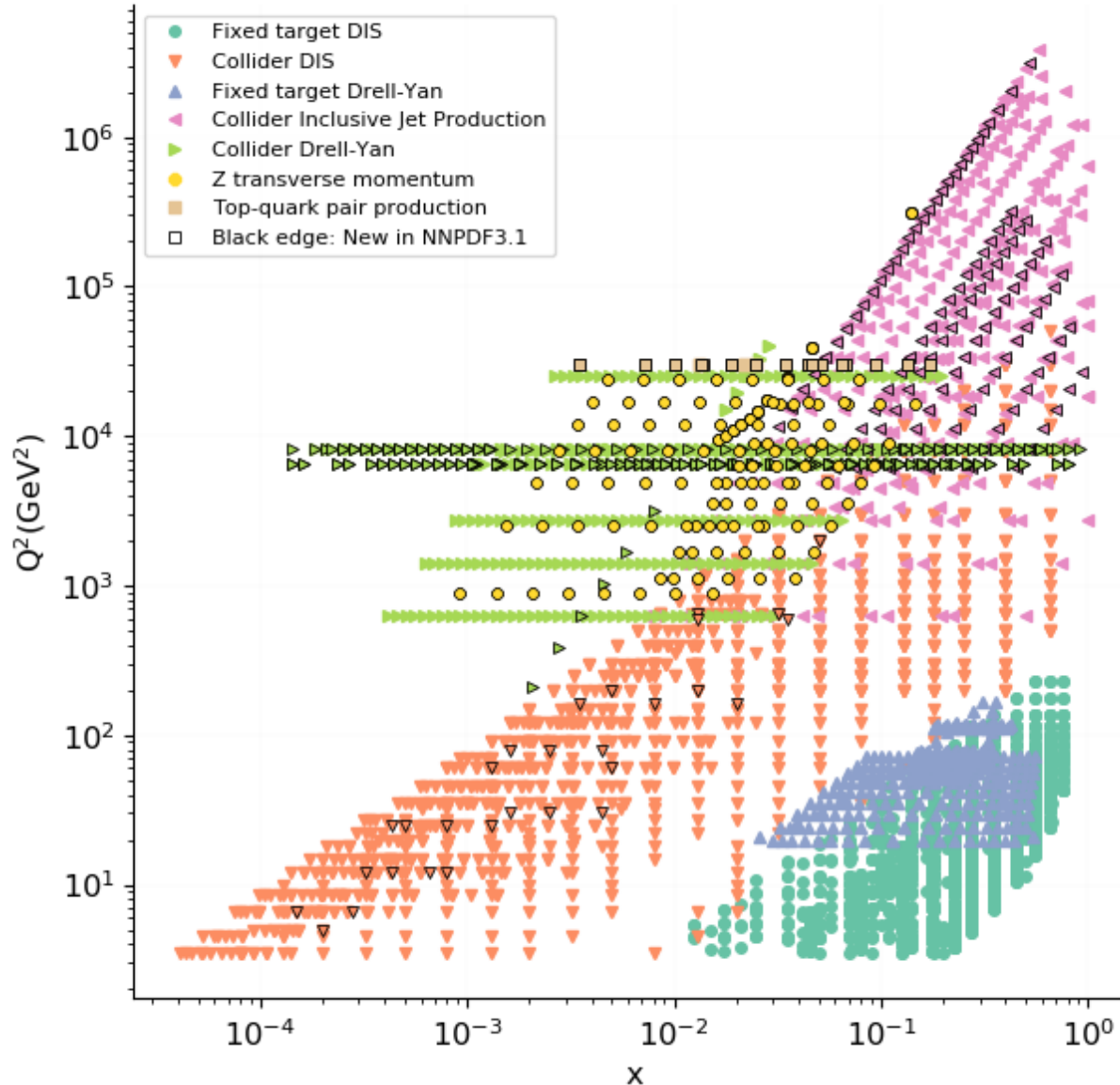
THEORY PROGRESS:

- **MSTW**, **ABKM**: all NNLO; **NNPDF** NNLO since 07/11 (2.1), **CT** since 02/13 (**CT10**); **NNPDF** THRESHOLD RESUMMATION (3.0RESUM, 07/15), SMALL x RESUMMATION (3.1SX, 10/17)
- **MSTW**, **CT**, **NNPDF** all GM-VFN; **NNPDF** since 01/11 (2.1); **ABM** FFN+ZM-VFN since 01/17 (**ABMP16**)
- **NNPDF** FITTED CHARM since 05/16 (**NNPDF3IC**)
- PHOTON PDF: (**mrst2004qed**), **NNPDF2.3QED** (08/13), **NNPDF3.0QED** (06/16), **NNPDF3.1LUXQED** (12/17)

DATASET WIDENING

NNPDF3.0 vs NNPDF3.1

Kinematic coverage



NEW DATA: (BLACK EDGE)

- HERA COMBINED F_2^b
- D0 W LEPTON ASYMMETRY
- ATLAS W, Z 2011, HIGH & LOW MASS DY 2011;
CMS $W^\pm$ RAPIDITY 8TeV
LHCb W, Z 7TeV & 8TeV
- ATLAS 7TeV JETS 2011, CMS 2.76TeV JETS
- ATLAS & CMS TOP DIFFERENTIAL RAPIDITY
- ATLAS Z p_T DIFFERENTIAL RAPIDITY & INVARIANT MASS 8TeV,
CMS Z p_T DIFFERENTIAL RAPIDITY 8TeV

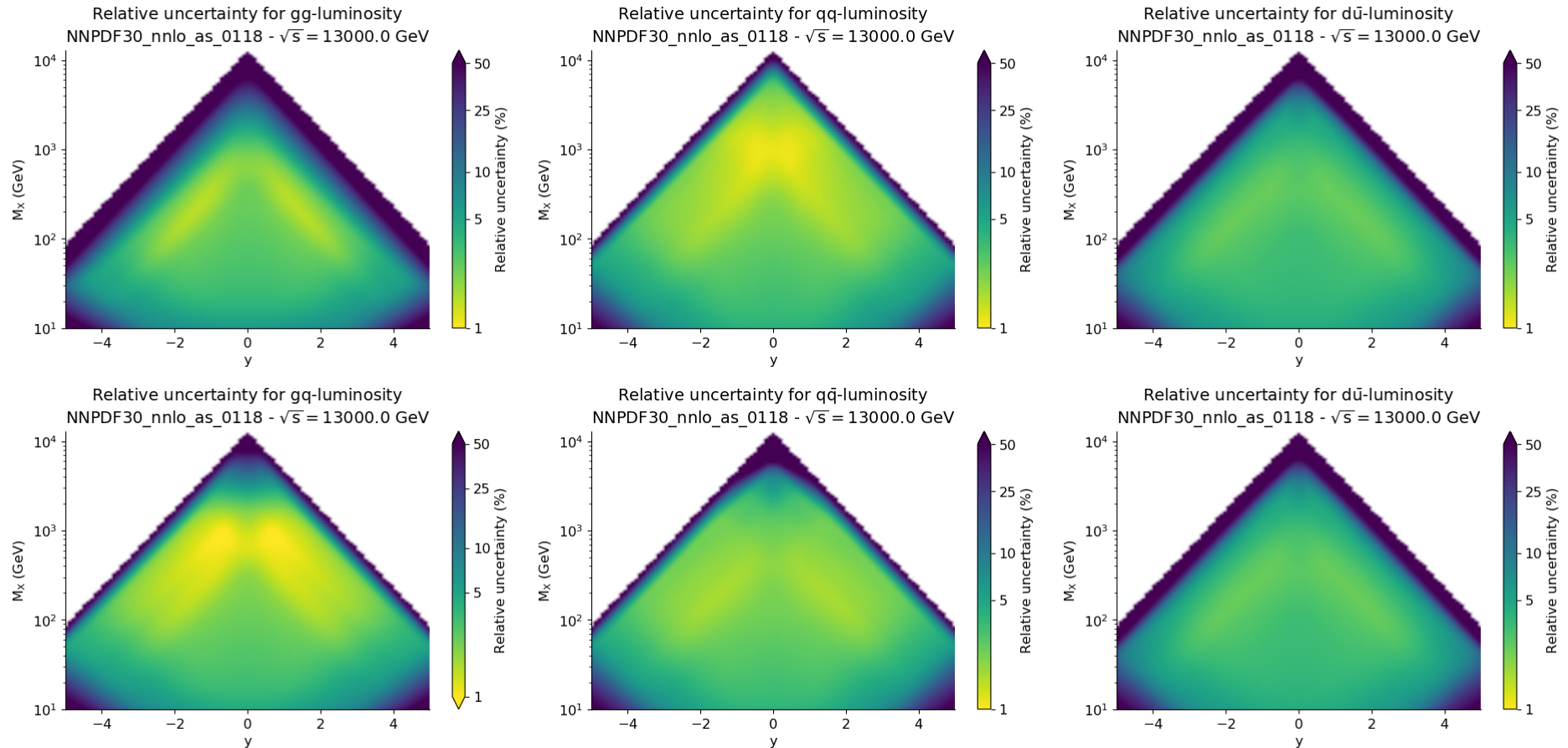
THE IMPACT OF LHC DATA

PDF UNCERTAINTIES IN DETAIL: NNPDF3.0 (NNLO)

GLUON

SINGLET

FLAVORS



- GLUON BETTER KNOWN AT SMALL x , VALENCE QUARKS AT LARGE x , SEA QUARKS IN BETWEEN
- TYPICAL UNCERTAINTIES IN DATA REGION $\sim 3 - 5\%$
- SWEET SPOT: VALENCE Q - G; DOWN TO 1%
- UP BETTER KNOWN THAN DOWN; FLAVOR SINGLET BETTER THAN INDIVIDUAL FLAVORS

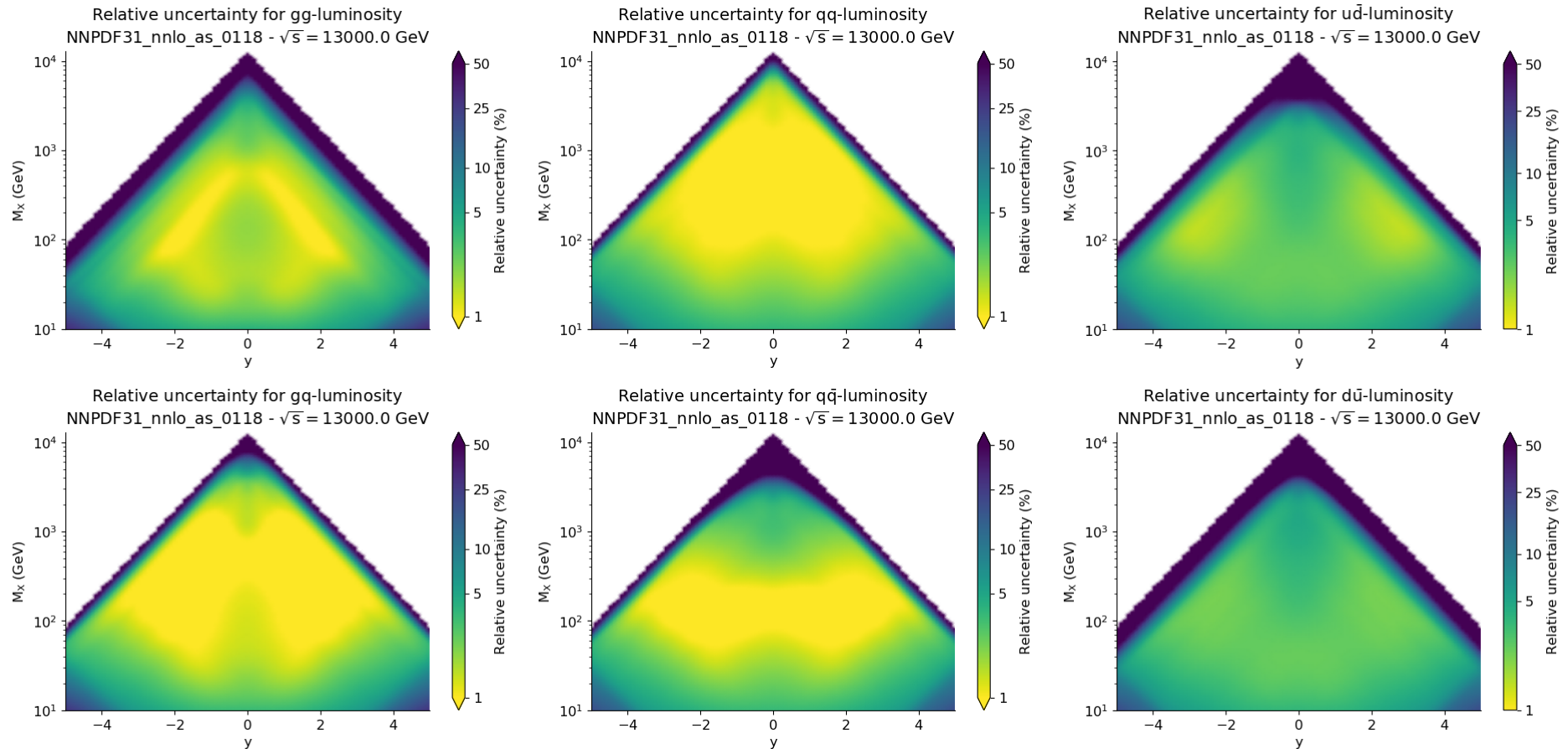
THE IMPACT OF LHC DATA

PDF UNCERTAINTIES IN DETAIL: **NNPDF3.1** (NNLO)

GLUON

SINGLET

FLAVORS



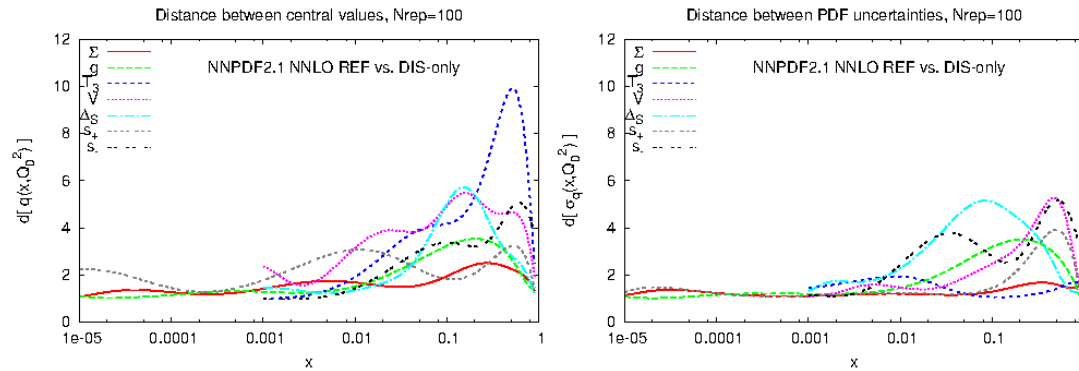
- **GLUON** BETTER KNOWN AT SMALL x , **VALENCE** QUARKS AT LARGE x , SEA QUARKS IN BETWEEN
- **TYPICAL** UNCERTAINTIES IN DATA REGION $\sim 1 - 3\%$
- **SWEET SPOT**: VALENCE $q - g$; 1% OR BELOW
- UP BETTER KNOWN THAN DOWN; FLAVOR SINGLET BETTER THAN INDIVIDUAL FLAVORS
- **NEW LHC DATA** $\Rightarrow$ **SIZABLE REDUCTION IN UNCERTAINTIES**

THE IMPACT OF LHC DATA

BEFORE LHC: PDFs **MOSTLY DETERMINED BY DIS DATA**

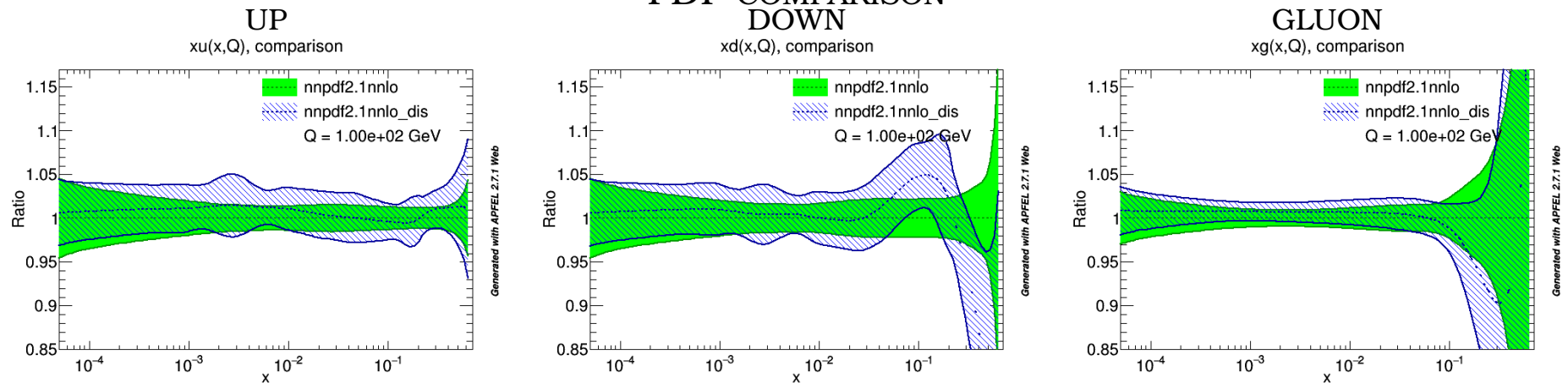
NNPDF2.1 vs NNPDF2.1 DIS ONLY

DISTANCES (difference in units of st. dev.)



$d = 10 \Leftrightarrow$ one sigma difference

PDF COMPARISON



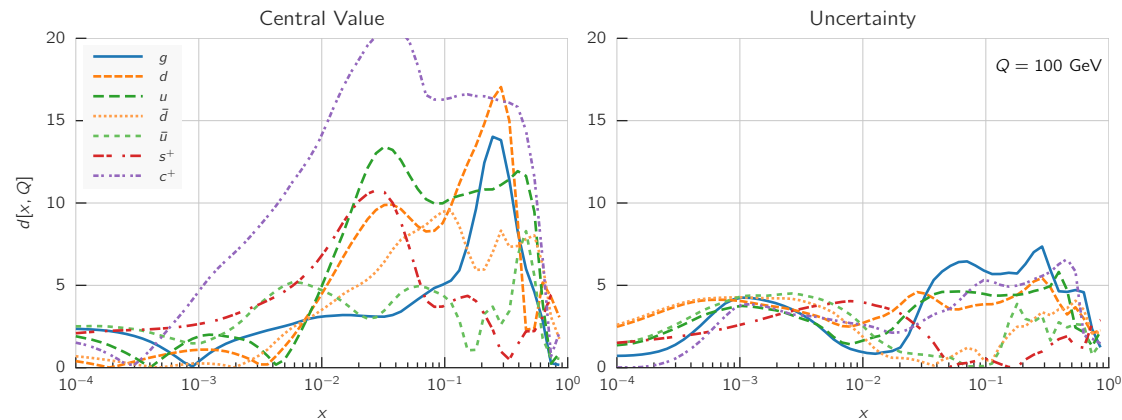
- ALL DIFFERENCES **BELOW ONE SIGMA**
- ONLY **UP-DOWN SEPARATION** SIGNIFICANTLY AFFECTED

THE IMPACT OF LHC DATA

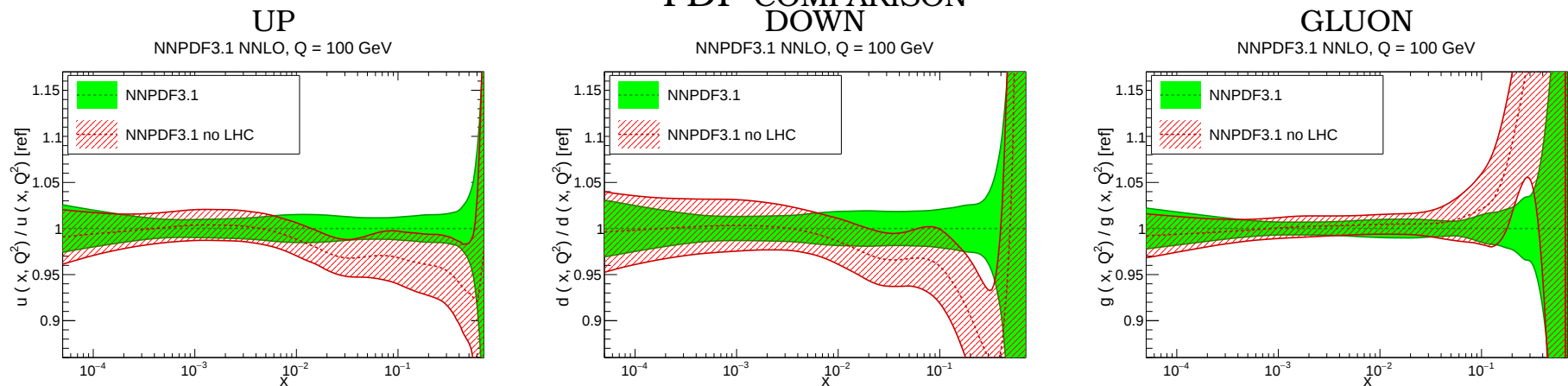
NOW: PDFs **LARGELY DETERMINED BY LHC** DATA

NNPDF3.1 vs NNPDF3.1 no LHC DISTANCES (difference in units of st. dev.)

NNPDF3.1 NNLO, Impact of LHC data



$d = 10 \Leftrightarrow$ one sigma difference
PDF COMPARISON
DOWN

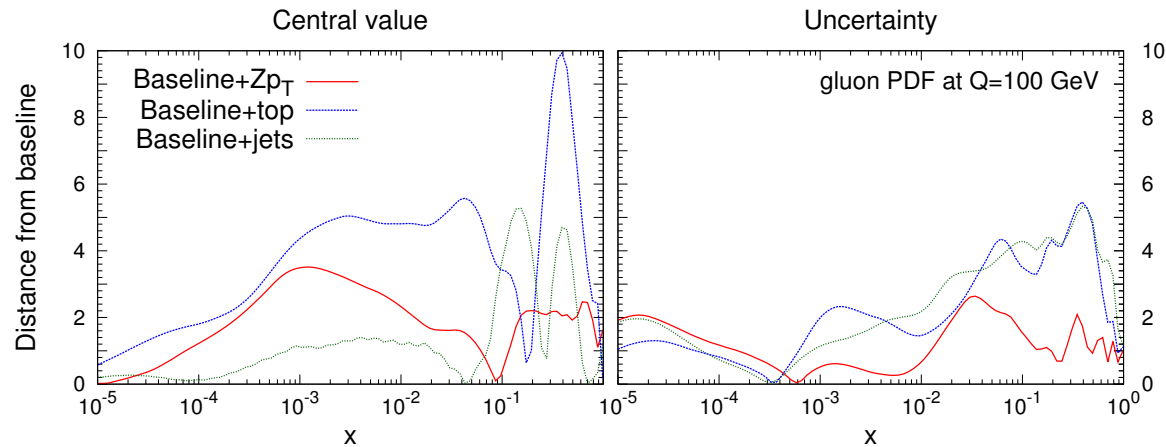


- MANY PDFs CHANGE BY MORE THAN ONE SIGMA
- BOTH **FLAVOR SEPARATION & GLUON** SIGNIFICANTLY AFFECTED

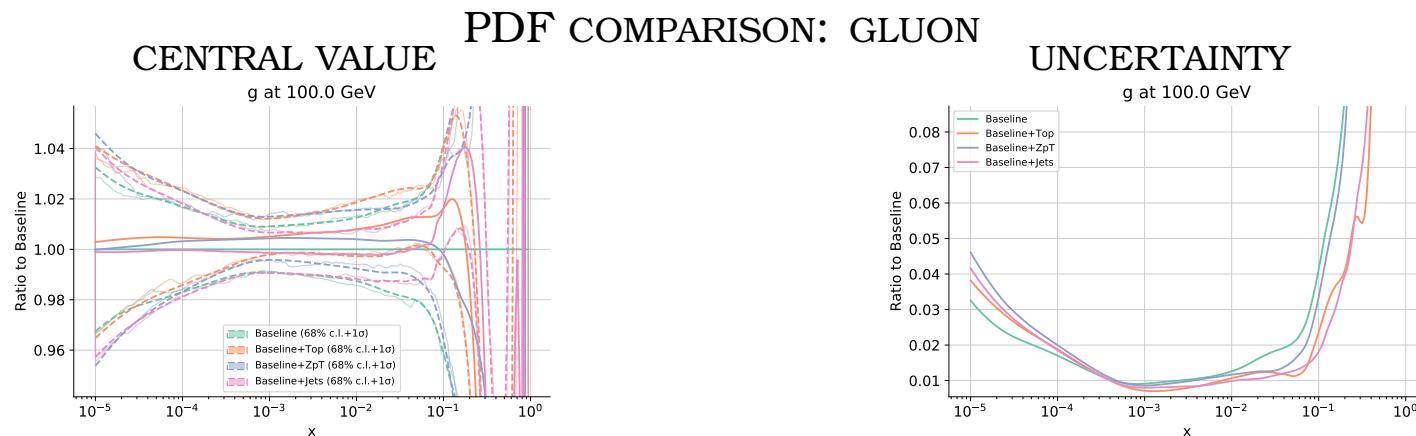
THE IMPACT OF LHC DATA THE GLUON

- BEFORE LHC $\Rightarrow$ DIS SCALING VIOLATIONS, TEV JETS AT LARGE X
- AFTER LHC $\Rightarrow$ JETS; Z p_t , TOP

DISTANCES (difference in units of st. dev.)



(Nocera, Ubiali, 2017)



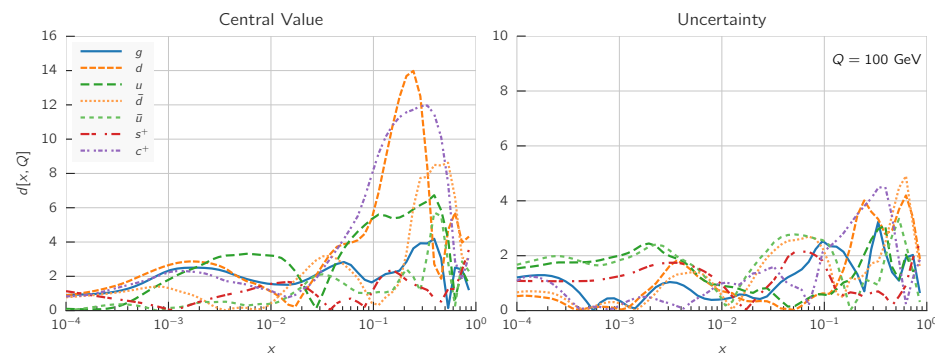
- TOP HAS LARGEST IMPACT, FOLLOWED BY JETS
- ALL LHC DATA PULL CENTRAL VALUE IN SAME DIRECTION!

THE IMPACT OF LHC DATA FLAVOR SEPARATION

- BEFORE LHC $\Rightarrow$ CC DIS, TeV FIXED-TARGET DY, W ASYM.
- AFTER LHC $\Rightarrow$ WIDE RANGE OF W , Z PRODUCTION DATA

IMPACT OF LHCb DISTANCES (difference in units of st. dev.)

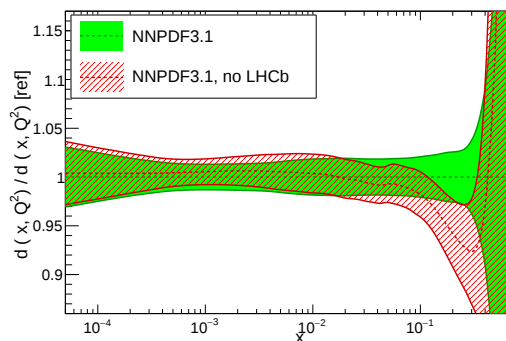
NNPDF3.1 NNLO, Impact of LHCb data



PDF COMPARISON: DOWN

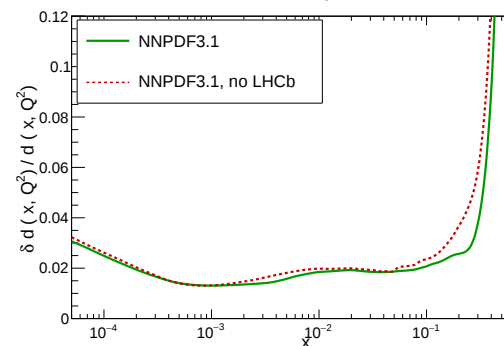
CENTRAL VALUE

NNPDF3.1 NNLO, $Q = 100$ GeV



UNCERTAINTY

NNPDF3.1 NNLO, $Q = 100$ GeV



- SIZABLE SHIFT OF CENTRAL VALUE BY ALMOST ONE SIGMA
- LARGE x UNCERTAINTY DOWN BY LARGE FACTOR!

NEW DATA: SUMMARY

- LHC DATA NOW HAVE THE DOMINANT IMPACT ON PDFs
- METHODOLOGY AND THEORY MUST ACCORDINGLY ADAPT

THE LIMITS OF METHODOLOGY

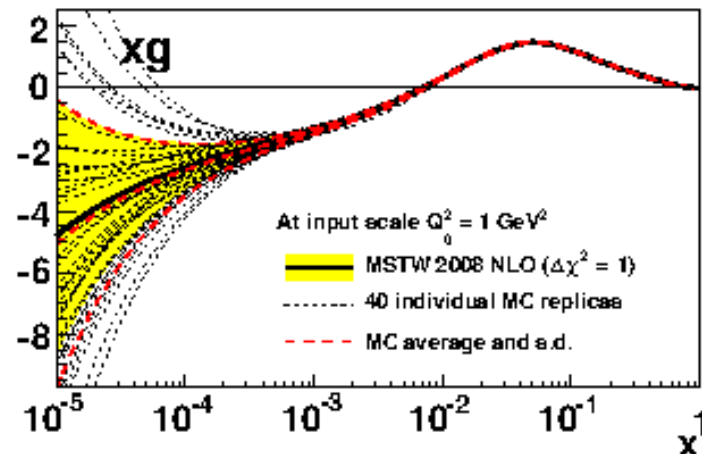
PDF PARAMETRIZATION & DELIVERY

- TRADITIONALLY, TWO DELIVERY METHODS FOR PDFs
- **HESSIAN** A CENTRAL PDF SET, & ERROR SETS CORRESPONDING TO EIGENVECTORS OF THE COVARIANCE MATRIX IN PARAMETER SPACE
ADVANTAGE: EFFICIENT REPRESENTATION OF UNCERTAINTY
DISADVANTAGES: ASSUMES GAUSSIANTY
- **MONTECARLO** A SET OF PDF REPLICAS WHICH REPRESENTS THE PROBABILITY IN PDF SPACE (SO THE MEAN UNBIASEDLY ESTIMATES THE CENTRAL VALUE &C)
ADVANTAGE: FAITHFUL REPRESENTATION OF PROBABILITY
DISADVANTAGES: MAY NEED LARGE NUMBER OF REPLICAS
- TRADITIONALLY, DELIVERY $\Leftrightarrow$ PARAMETRIZATION/MINIMIZATION
HESSIAN USED WITH RELATIVELY SIMPLE FUNCTIONAL FORMS (SMALL NUMBERS OF PARAMETERS) $\Leftrightarrow$ HESSIAN MINIMIZATION

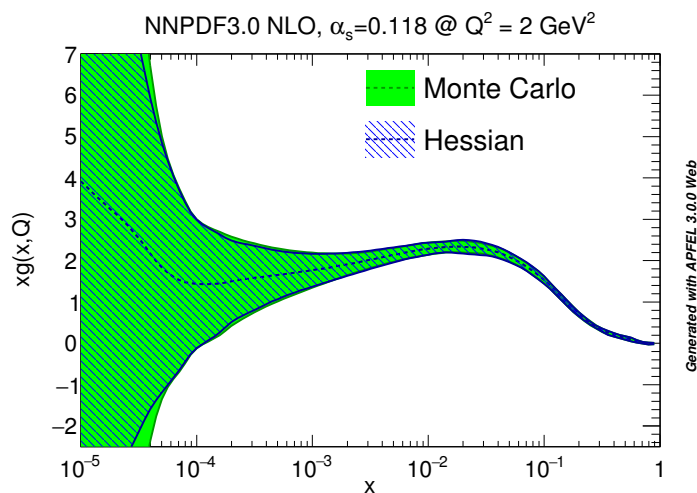
PROGRESS I

MC $\Leftrightarrow$ HESSIAN

- TO CONVERT HESSIAN INTO MONTECARLO
GENERATE MULTIGAUSSIAN REPLICAS
IN PARAMETER SPACE
- ACCURATE WHEN NUMBER OF REPLICAS
SIMILAR TO THAT WHICH REPRODUCES DATA



(Thorne, Watt, 2012)

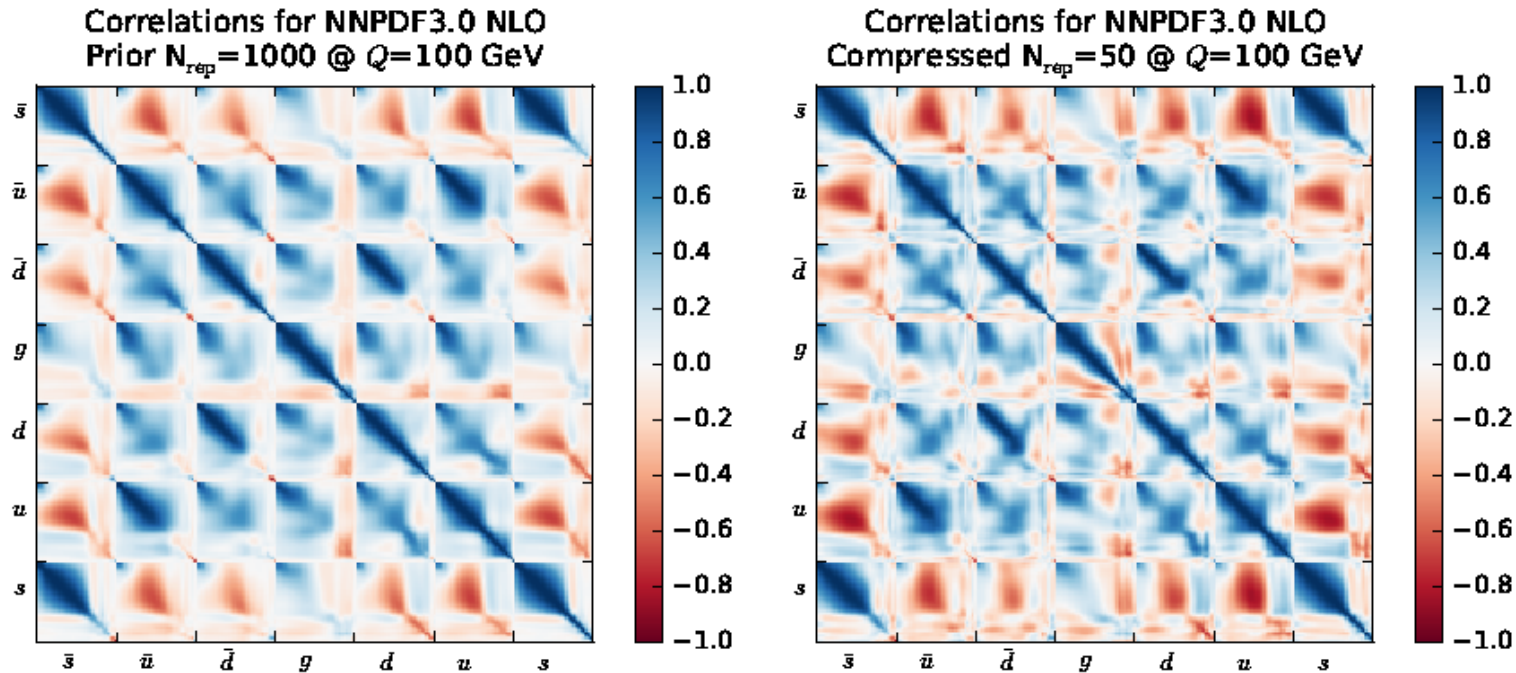


(Carrazza, SF, Kassabov, Rojo, 2015)

- TO CONVERT MONTE CARLO INTO HESSIAN, SAMPLE
THE REPLICAS $f_i(x)$ AT A DISCRETE SET OF POINTS &
CONSTRUCT THE ENSUING COVARIANCE MATRIX
- EIGENVECTORS OF THE COVARIANCE MATRIX AS A
BASIS IN THE VECTOR SPACE SPANNED BY THE REPLICAS
BY SINGULAR-VALUE DECOMPOSITION
- NUMBER OF DOMINANT EIGENVECTORS SIMILAR TO
NUMBER OF REPLICAS $\Rightarrow$ ACCURATE REPRESENTATION

PROGRESS II

MONTECARLO COMPRESSION

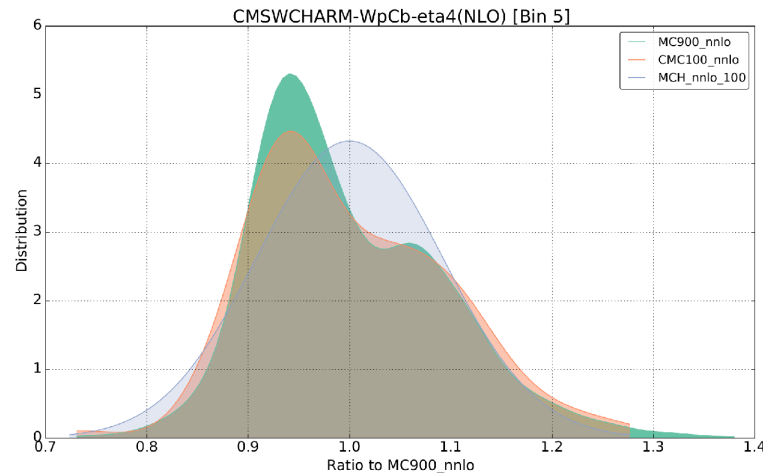


(Carrazza, Latorre, Kassabov, Rojo, 2015)

- CONSTRUCT A **VERY LARGE REPLICA SAMPLE**
- **SELECT** (BY GENETIC ALGORITHM) A **SUBSET OF REPLICAS** WHOSE STATISTICAL FEATURES ARE **AS CLOSE AS POSSIBLE** TO THOSE OF THE **PRIOR**
- $\Rightarrow$ **FOR ALL PDFs ON A GRID OF POINTS// MINIMIZE DIFFERENCE** OF: FIRST FOUR MOMENTS, CORRELATIONS; OUTPUT OF KOLMOGOROV-SMIRNOV TEST (NUMBER OF REPLICAS BETWEEN MEAN AND σ , 2σ , INFINITY)
- 50 COMPRESSED REPLICA REPRODUCE 1000 REPLICA SET TO PRECENT ACCURACY

NONGAUSSIAN BEHAVIOUR

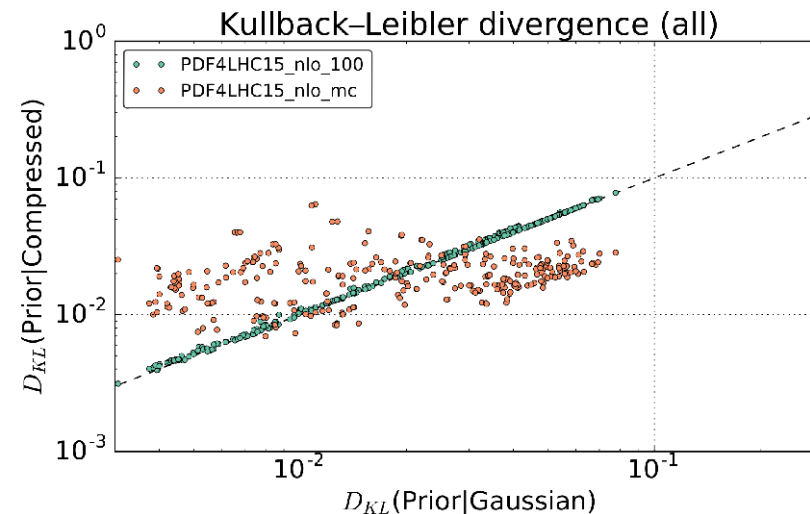
MONTE CARLO COMPARED TO HESSIAN CMS $W + c$ production



- DEFINE **KULLBACK-LEIBLER DIVERGENCE**

$$D_{\text{KL}} = \int_{-\infty}^{\infty} P(x) \frac{\ln P(x)}{\ln Q(x)} dx$$
 BETWEEN A PRIOR P AND ITS REPRESENTATION Q
- D_{KL} BETWEEN PRIOR AND HESSIAN
 DEPENDS ON DEGREE OF GAUSSIANTY
- D_{KL} BETWEEN PRIOR AND COMPRESSED
 MC DOES NOT

- DEVIATION FROM GAUSSIANTY E.G. AT LARGE x DUE TO LARGE UNCERTAINTY + POSITIVITY BOUNDS
 $\Rightarrow$ **RELEVANT FOR SEARCHES**
- **CANNOT BE REPRODUCED IN HESSIAN FRAMEWORK**
- **WELL REPRODUCED BY COMPRESSED MC**



CAN (A) GAUGE WHEN MC IS MORE ADVANTAGEOUS THAN HESSIAN;
 (B) ASSESS THE ACCURACY OF COMPRESSION

PDF PARAMETRIZATION ISSUES

- **Q: WHY ARE PDF UNCERTAINTIES ON GLOBAL FITS OF SIMILAR SIZE?**
 - SIMILAR DATASETS
 - BUT DIFFERENT PROCEDURES
- **A: UNCERTAINTY TUNING**

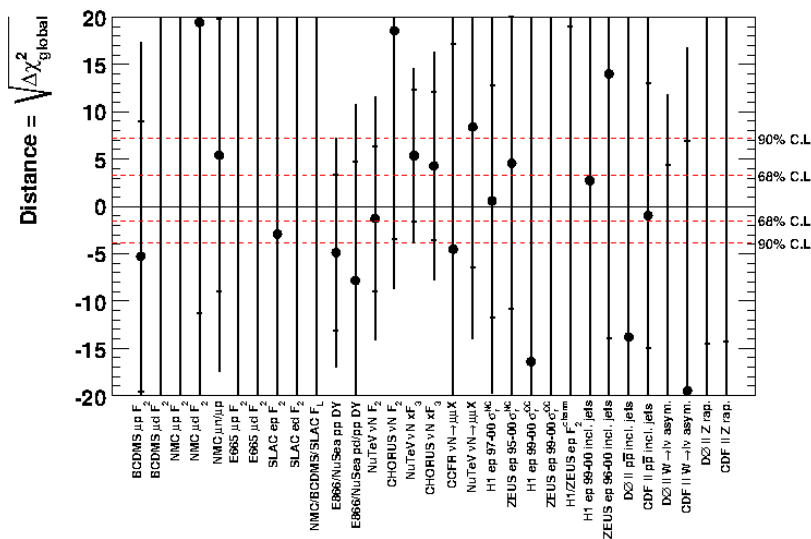
TOLERANCE (MMHT-CT)

GLOBAL MSTW TOLERANCE

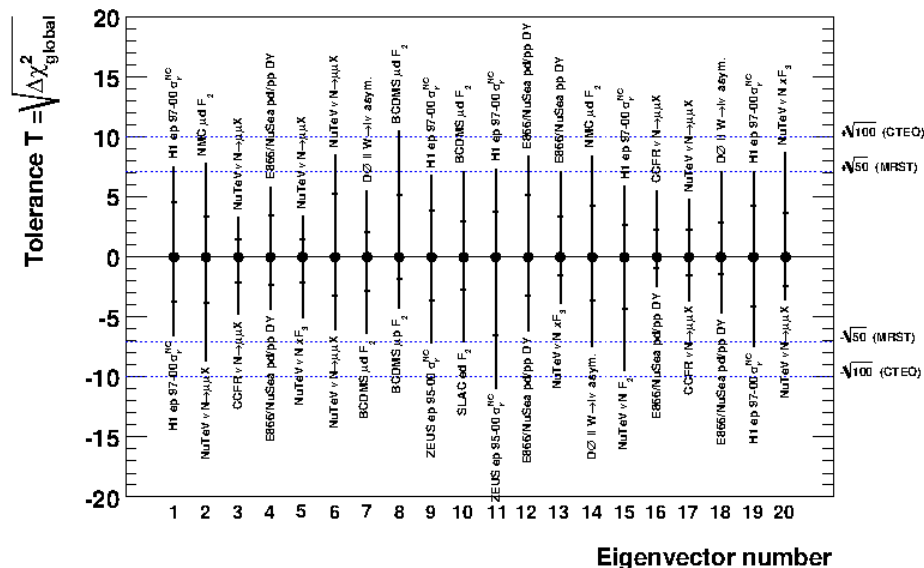
MSTW TOLERANCE PLOT FOR 13TH EIGENVEC.

Eigenvector number 13

MSTW 2008 NLO PDF fit



MSTW 2008 NLO PDF fit

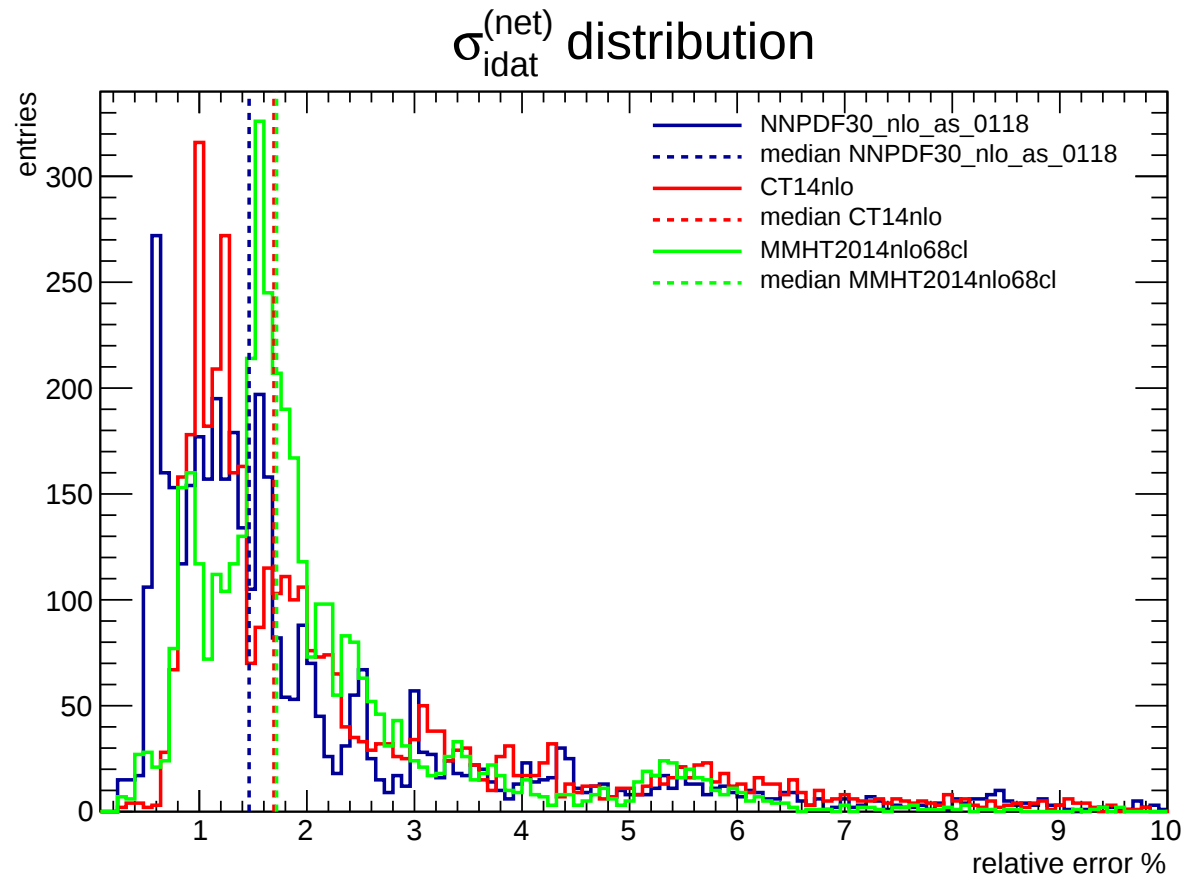


- (MSTW/MMHT) FOR EACH EIGENVECTOR IN PARAMETER SPACE DETERMINE CONFIDENCE LIMIT FOR THE DISTRIBUTION OF BEST-FITS OF EACH EXPERIMENT
- RESCALE $\Delta\chi^2 = T$ INTERVAL SUCH THAT CORRECT CONFIDENCE INTERVALS ARE REPRODUCED
- WHY DO WE NEED TOLERANCE?
- DO WE UNDERSTAND PDF UNCERTAINTIES?

PDF UNCERTAINTIES: HOW MUCH DO THEY VARY?

- COMPUTE **PERCENTAGE PDF UNCERTAINTY** ON ALL DATA INCLUDED IN GLOBAL FIT
- **COMPARE** GLOBAL FITS

PERCENTAGE PDF UNCERTAINTY ON PREDICTIONS



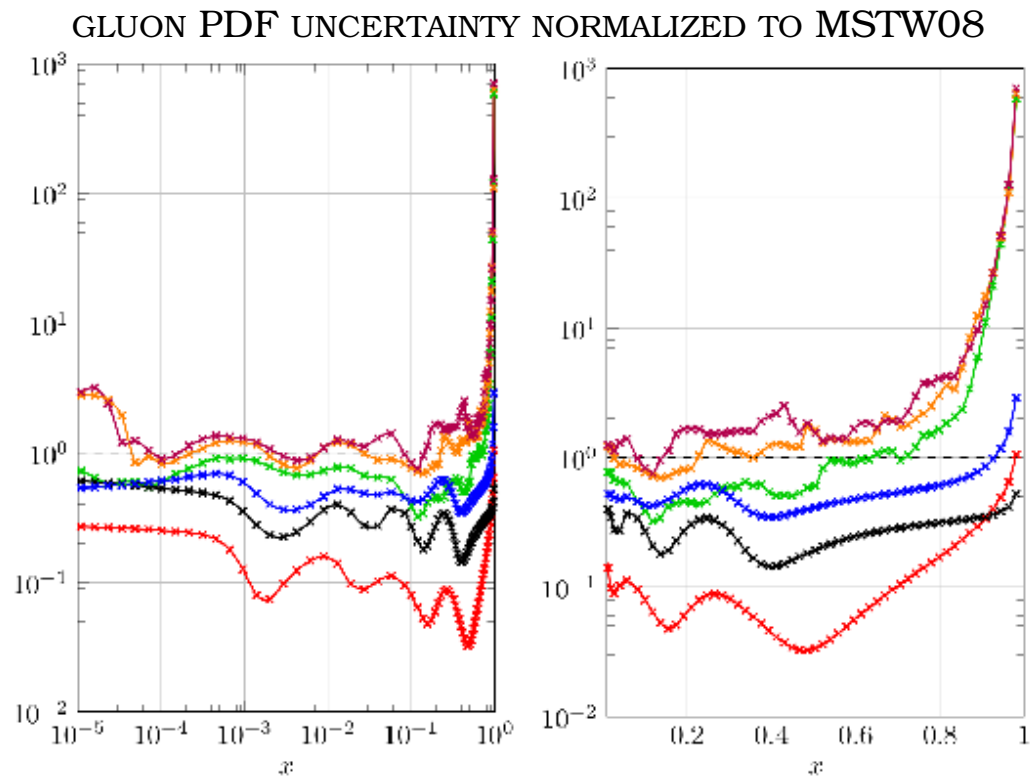
- **MEDIAN SIMILAR**
- **DISTRIBUTION VERY DIFFERENT!**
- **NNPDF: SMALLER MODE, BUT FAT TAIL $\Leftrightarrow$ GREATER FLEXIBILITY**

CLOSURE TESTING

BASIC IDEA

- ASSUME PDFs KNOWN: GENERATE FAKE EXPERIMENTAL DATA
- CAN DECIDE DATA UNCERTAINTY (ZERO, OR AS IN REAL DATA, OR . . .)
- FIT PDFs TO FAKE DATA:
 - LEVEL 0: ZERO UNCERTAINTY
 - * CHECK WHETHER MINIMIZATION EFFICIENT
 - * CHECK FOR INTERPOLATION UNCERTAINTY
 - LEVEL 1: DATA UNCERTAINTY, BUT NO REPLICAS
 - * CHECK FOR UNIQUENESS OF BEST FIT $\Rightarrow$ “FUNCTIONAL” UNCERTAINTY (Pumplin, 2010)
 - LEVEL 2: AS IN STANDARD PROCEDURE
 - * CHECK WHETHER TRUE VALUE GAUSSIANLY DISTRIBUTED ABOUT FIT
 - * CHECK WHETHER UNCERTAINTIES FAITHFUL

CLOSURE-TESTING: THE PARAMETRIZATION DEPENDENCE



(C. Mascaretti, 2016)

- CLOSURE TEST PERFORMED WITH DATA GENERATED BASED ON MST08 FUNCTIONAL FORM
- REFITTED EITHER WITH NNPDF OR MSTW FUNCTIONAL FORM
- LEVEL 0: VANISHING DATA UNCERTAINTY
 - MSTW-CT: FIT HAS ZERO UNCERTAINTY
 - NNPDF: ABOUT HALF OF TOTAL UNCERTAINTY
- LEVEL 1: NOMINAL DATA UNCERTAINTY, BUT REPLICAS FITTED W/O PSEUDODATA
 - MSTW-CT: FIT HAS SMALL UNCERTAINTY
 - NNPDF: ABOUT 2/3 OF FINAL UNCERTAINTY
- LEVEL 2
 - NNPDF UNCERTAINTY LARGER THAN MSTW-CT
 - NNPDF UNCERTAINTY SIMILAR TO TRUE MSTW

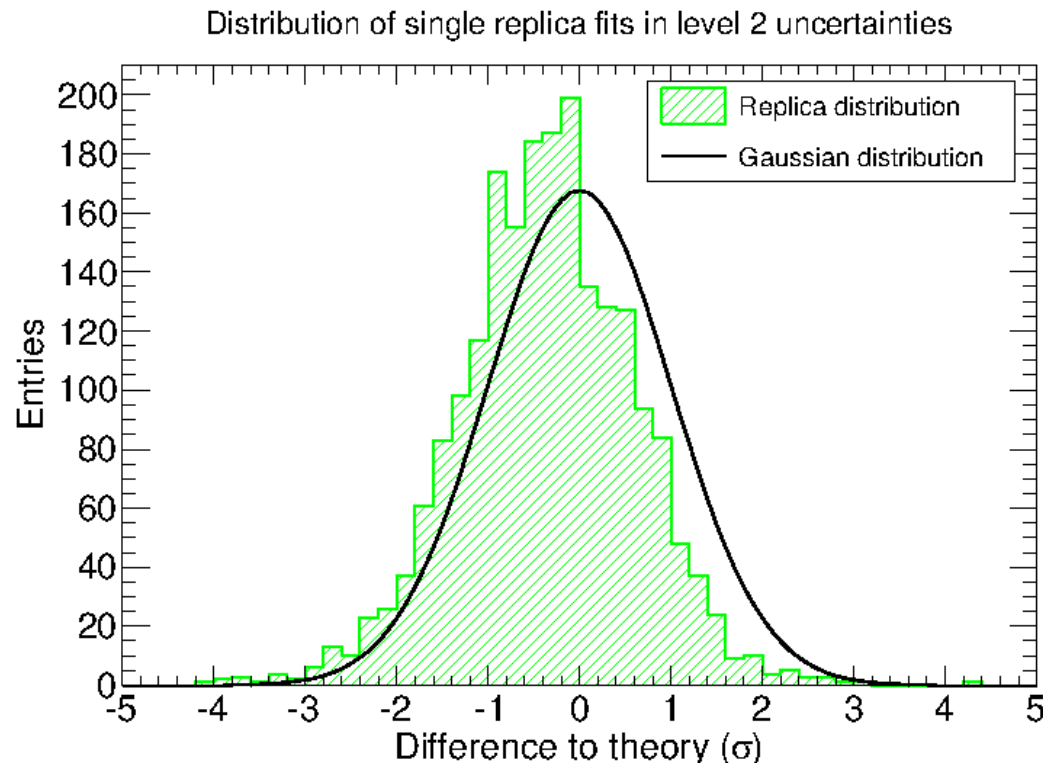
“STANDARD” PARAMETRIZATION
MISSES INTERPOLATION & FUNCTIONAL UNCERTAINTY?

THE $\Delta\chi^2$ PROBLEM

- TOLERANCE MIGHT COMPENSATE FOR MISSING FUNCTIONAL UNCERTAINTY
- BUT WHAT IS $\Delta\chi^2$ FOR AN NNPDF FIT?
- CAN ANSWER USING HESSIAN CONVERSION! $\Delta\chi^2 = 16 \pm 15$
 - NON-PARABOLIC BEHAVIOUR NEAR MINIMUM ON SCALE OF UNCERTAINTIES?
 - INEFFICIENCY OF THE MINIMIZATION PROCEDURE?

CLOSURE-TESTING THE PDF UNCERTAINTIES RESULTS

UNCERTAINTIES: DISTRIBUTION OF DEVIATIONS BETWEEN FITTED AND “TRUE” PDFs, SAMPLED AT 20 POINTS BETWEEN 10^{-5} AND 1

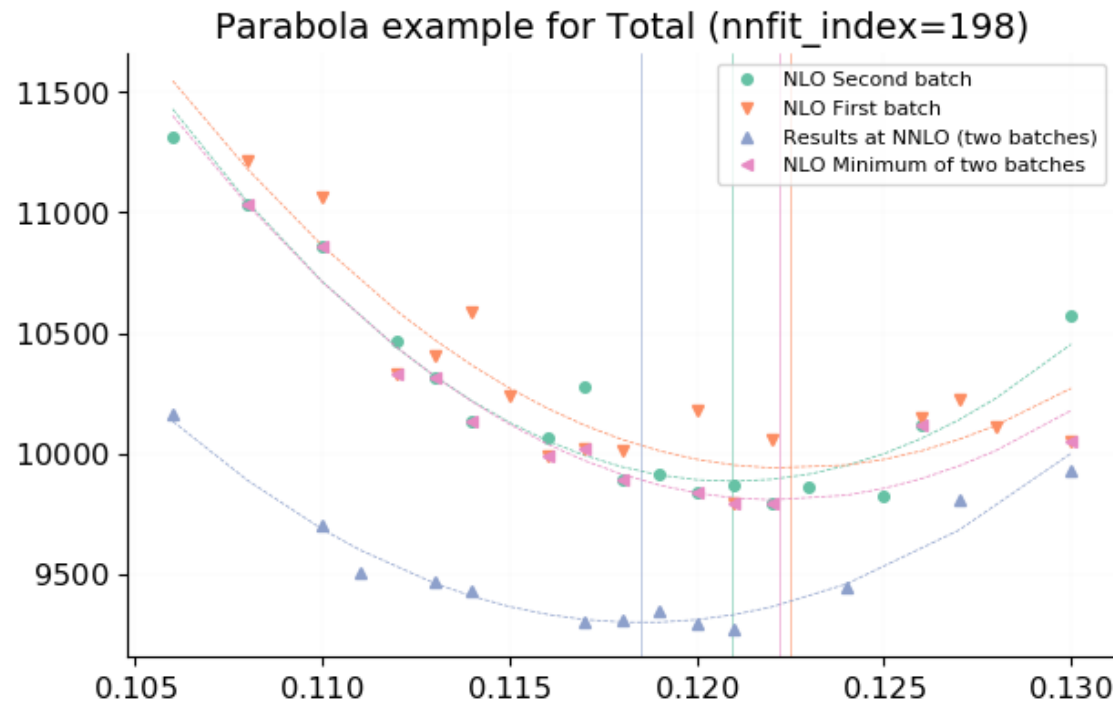


FIND 0.699% FOR ONE-SIGMA, 0.948% FOR TWO-SIGMA C.L.

- PDF UNCERTAINTIES ARE FAITHFUL
- BUT ARE THEY THE SMALLEST FROM GIVEN DATA?

MORE EFFICIENT MINIMIZATION?

- LOOK AT α_s DEPENDENCE (CORRELATED REPLICAS)
- **SIGNIFICANT FLUCTUATIONS** ABOUT PARABOLIC SHAPE
NOT DUE TO FINITE-SIZE MONTE CARLO SAMPLE



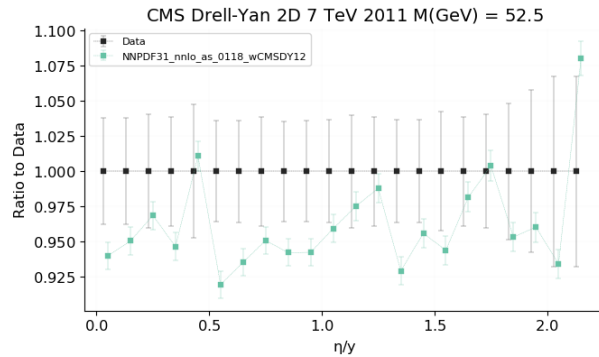
BATCH MINIMIZATION

- MINIMIZE EACH REPLICA MORE THEN ONCE & KEEP BEST RESULTS
- SIGNIFICANT **STABILIZATION**

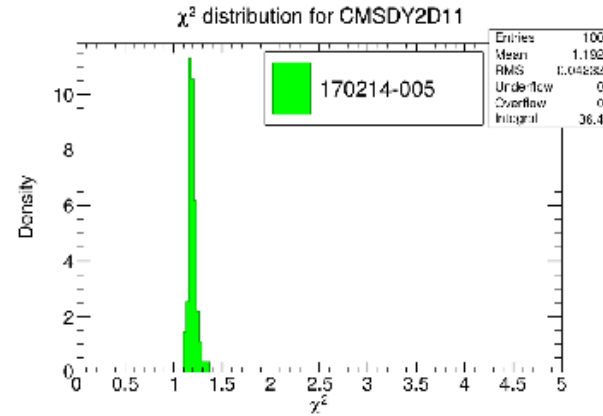
CORRELATIONS & THE COVARIANCE MATRIX

THE CMS DOUBLE-DIFFERENTIAL DRELL-YAN 2011

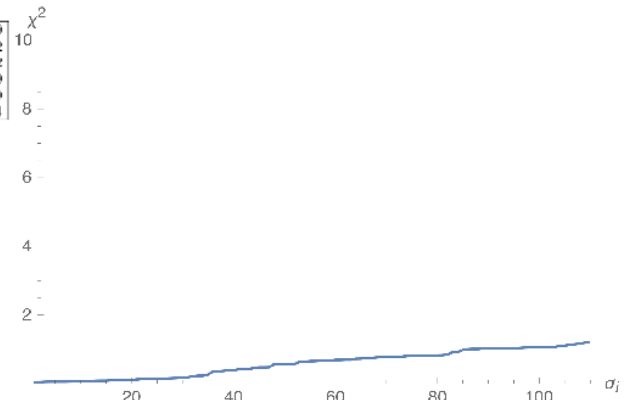
DATA/THEORY VS. DATA BIN



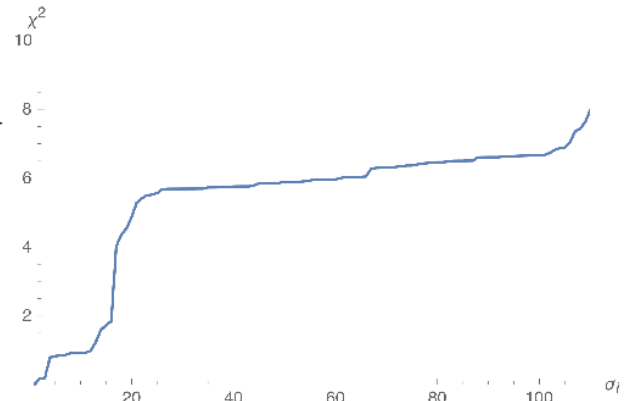
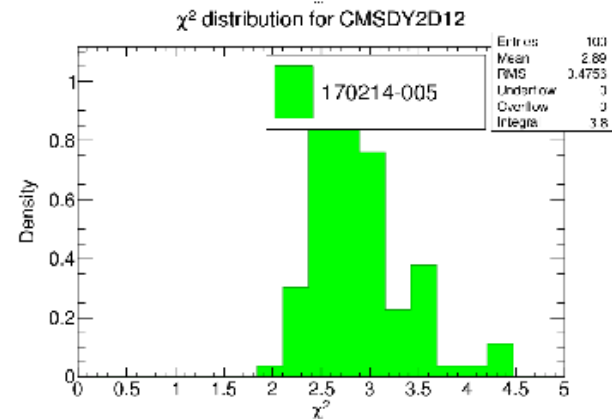
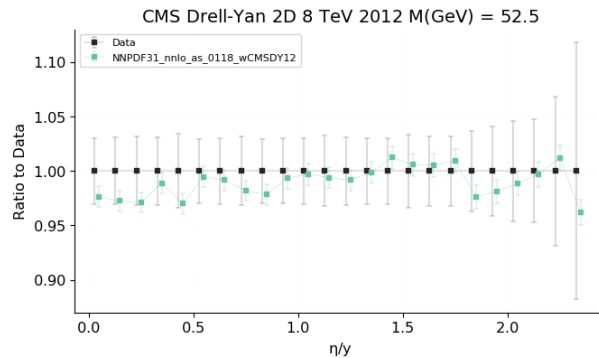
χ^2/dof HIST. OVER REPLICAS



χ^2 AS COVMAT EIGVECS ADDED



2012

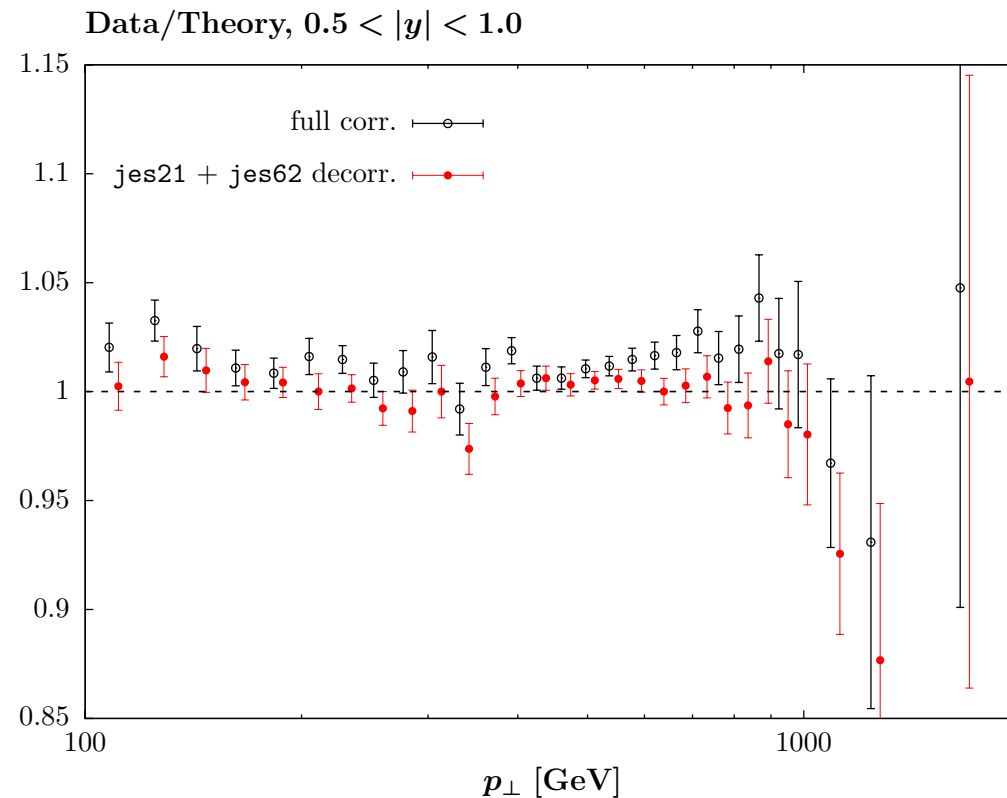


- FROM 2011 TO 2012, **UNCORRELATED UNCERTAINTIES DOWN TO SUB-PERMILLE**
- 2011: $\chi^2/dof \sim 1$; **2012: IMPOSSIBLE TO FIT** BETTER THAN $\chi^2/dof \sim 3$
- **PATHOLOGICAL BEHAVIOUR OF COVARIANCE MATRIX** $\Rightarrow$ WHAT IS THE UNCERTAINTY ON IT?

CORRELATIONS & THE COVARIANCE MATRIX

THE ATLAS 7TeV JETS

- EACH RAPIDITY BIN CAN BE FITTED WITH $\chi^2/dof \sim 1$
- EACH LEADS TO INDISTINGUISHABLE BEST-FIT PDFs
- IF ALL BINS FITTED SIMULTANEOUSLY, $\chi^2/dof \sim 3$

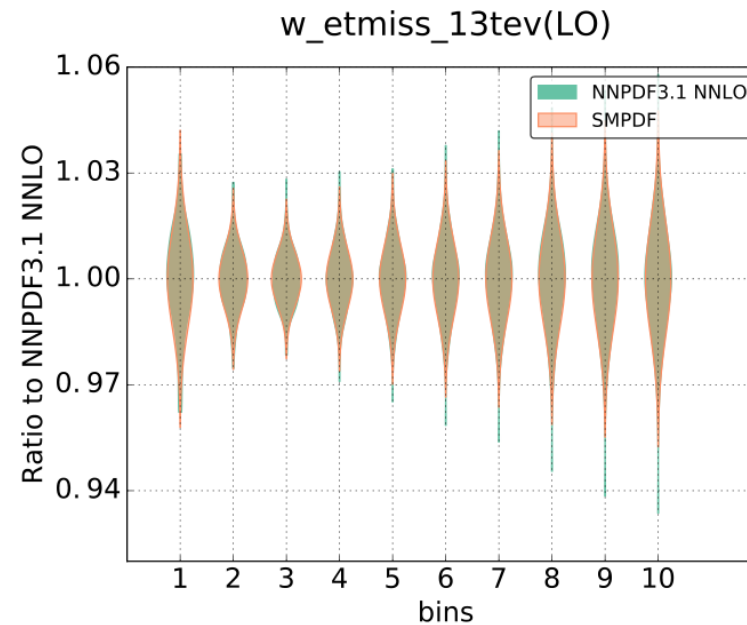
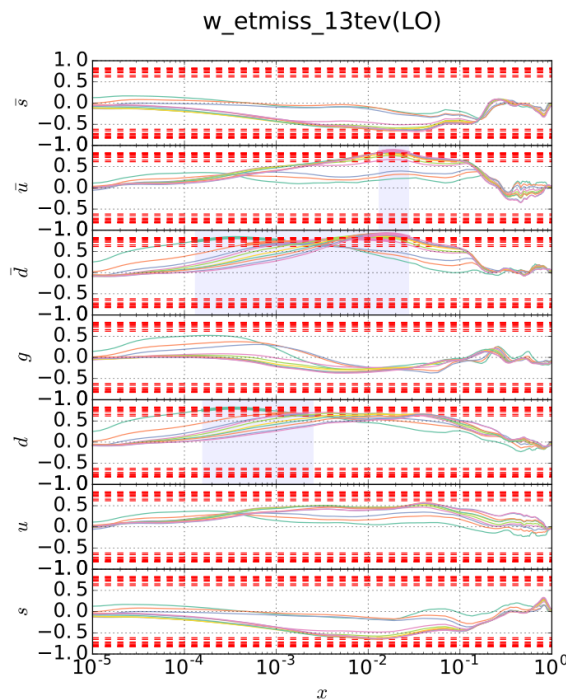


(Harland-Lang, Martin, Thorne, 1016)

- MISESTIMATED CORRELATIONS?
- CAN SINGLE OUT WHICH CORRELATION OUGHT TO BE REMOVED

SMPDF A POWERFUL TOOL

- OLD ASPIRATION: PDFs OPTIMIZED TO PROCESSES (Pumplin 2009)
- SELECT **SUBSET OF THE COVARIANCE MATRIX CORRELATED** TO A GIVEN SET OF PROCESSES
- PERFORM **SVD ON THE REDUCED COVARIANCE MATRIX**, SELECT DOMINANT EIGENVECTOR, **PROJECT OUT** ORTHOGONAL SUBSPACE
- ITERATE UNTIL DESIRED ACCURACY REACHED
- **CAN ADD PROCESSES TO GIVEN SET; CAN COMBINE DIFFERENT OPTIMIZED SETS**
- **WEB INTERFACE AVAILABLE**

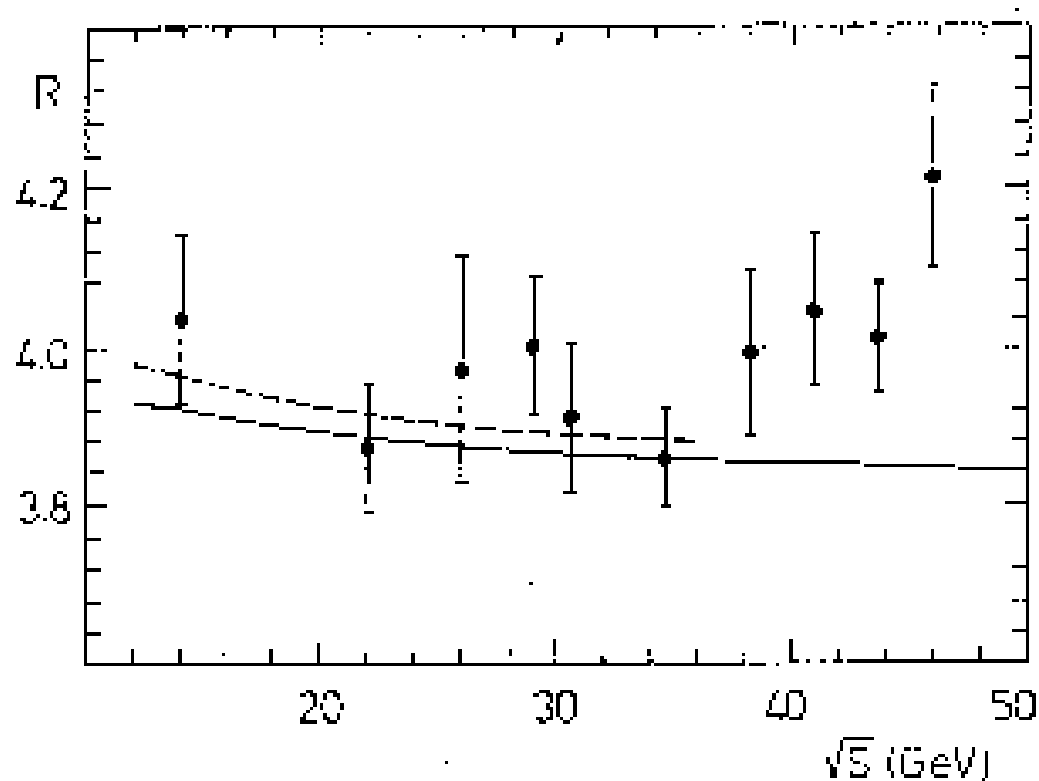


(Carrazza, SF, Kassabov, Rojo, 2016)

- EG $ggH, Hb\bar{b}, W E_T^{\text{miss}} \Rightarrow 11$ EIGENVECTORS
- STUDY **CORRELATIONS OF PDFs** TO DATA AND AMONG THEMSELVES!

AN OLD PROBLEM THE D'AGOSTINI BIAS

$$R = \frac{e^+e^- \rightarrow \text{hadrons}}{e^+e^- \rightarrow \mu^+\mu^-}$$



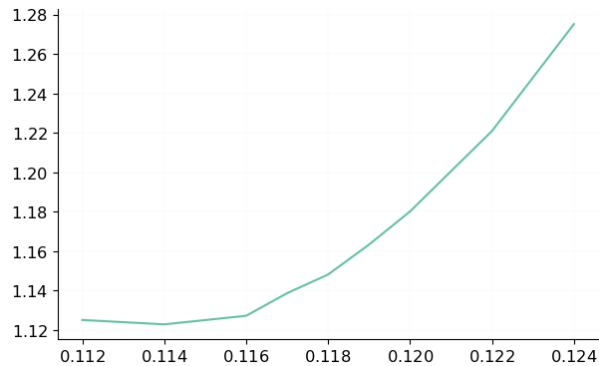
(CELLO collab., 1987)

- **MULTIPLICATIVE** UNCERTAINTIES IN **COVARIANCE MATRIX**
 $\Rightarrow$ FIT **BIASED DOWNWARDS** IF **DATA INCONSISTENT** (d'Agostini, 1994)
EQUIVALENT TO RESCALING DATA BUT NOT UNCERTAINTIES
- MUST USE **ITERATIVE PROCEDURE**
COVARIANCE MATRIX COMPUTED FROM PREVIOUS FIT (NNPDF, 2010)

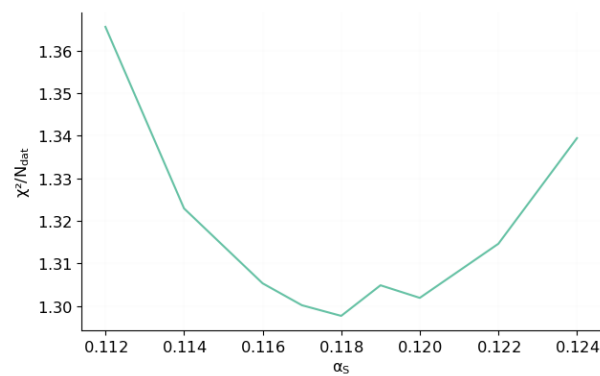
THE D'AGOSTINI BIAS

A SUBTLE EXAMPLE: α_s IN A PDF FIT

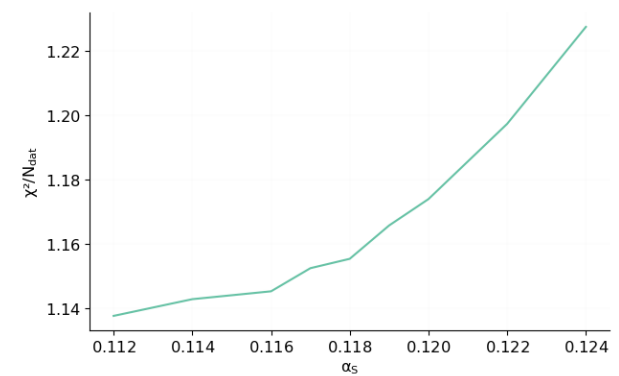
GLOBAL



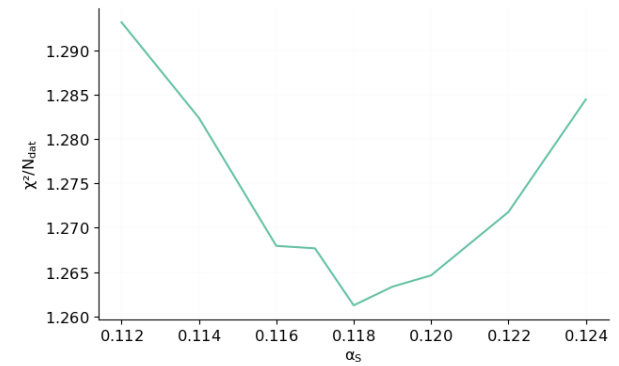
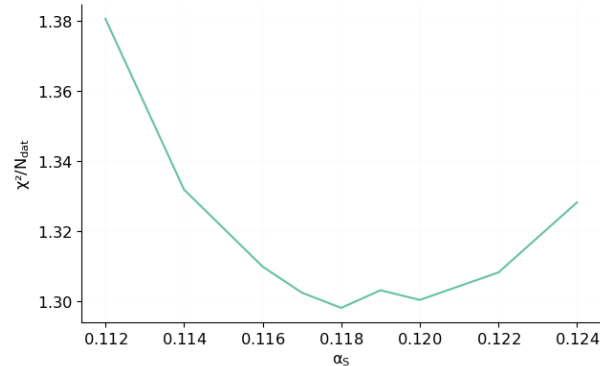
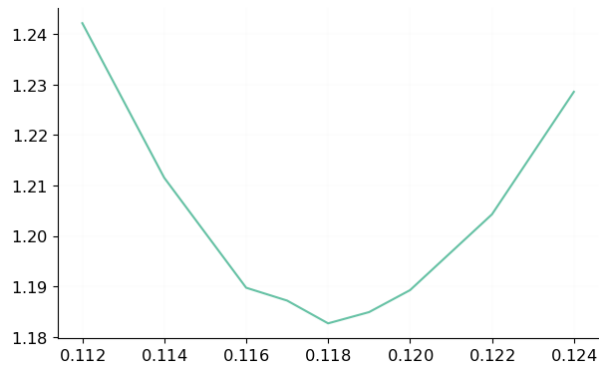
ADDITIVE (NMC, FT)



MULTIPLICATIVE (HERA, COLL)



CONSISTENT (ITERATIVE)



- χ^2 COMPUTED FROM COVARIANCE MATRIX $\Rightarrow$ **BIASED** LOW FIT FAVORED
- LESS EVOLUTION $\Leftrightarrow$ **LOW** α_s
- **ONLY** WHEN **MULTIPLICATIVE** UNCERTAINTIES DOMINATE
COLLIDER ONLY, NOT FIXED TARGET

METHODOLOGY: SUMMARY

- STATISTICAL ANALYSIS TOOLS NECESSARY TO COPE WITH DATA ACCURACY
- PDF UNCERTAINTIES ARE FAITHFUL, BUT NOT OPTIMAL

THE FRONTIER OF THEORY

NNLO

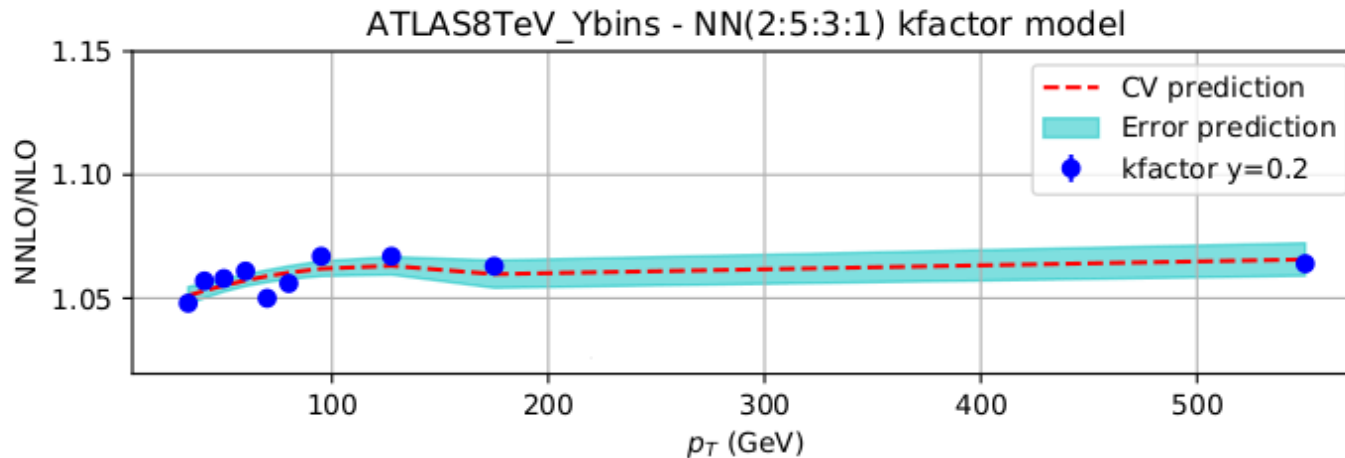


- NNLO CORRECTIONS NOW KNOWN AT INCREASINGLY EXCLUSIVE LEVEL (INCLUDING DECAYS)
- TYPICALLY LARGER THAN NAIVE SCALE VARIATION $\Rightarrow$ NEEDED FOR PRECISION PHENO
- NNLO PDF STANDARD SINCE ~ 2010 INCLUDE DIS, DRELL-YAN
- NEW GENERATION PDFs ALSO TOP, JETS, $Z p_t$
- FUTURE GENERATIONS: PROMPT PHOTON, DIBOSON...

THEORY CHALLENGES

THE UNCERTAINTY IN THEORY CALCULATIONS

AN EXAMPLE: ATLAS 7 TeV p_T DISTRIBUTION
THE NNLO/NLO K -FACTOR



(Boughezal, Liu, Petriello, 2016-2017)

- **UNCORRELATED STATISTICAL UNCERTAINTIES AT PERMILLE LEVEL**
- **LARGE NNLO** CORRECTIONS $\sim 10\%$
- NOMINAL K -FACTOR **UNCERTAINTIES** VERY SMALL: **UNDERESTIMATED?**
- FIT ONLY POSSIBLE WITH RELIABLE **ESTIMATE OF UNCERTAINTY ON THEORY PREDICTION**
- NNPDF3.1: EXTRA 1% THEORY UNCERTAINTY ESTIMATED BASED ON FLUCTUATIONS W.R. TO INTERPOLATION (SHADED IN PLOT)

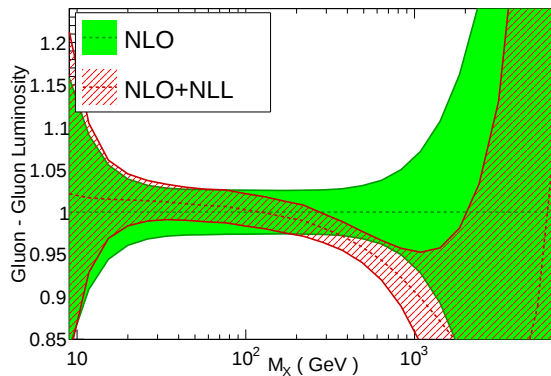
RESUMMED PDFs

- RESUMMATION NOT INCLUDED IN DEFAULT PDF SETS
- RESUMMED CALCULATIONS MUST USE RESUMMED PDFs! (M. Spira)
- KEPT UNDER CONTROL IN FITS BY CHOICE OF CUTS

PDFs WITH THRESHOLD (LARGE x) RESUMMATION

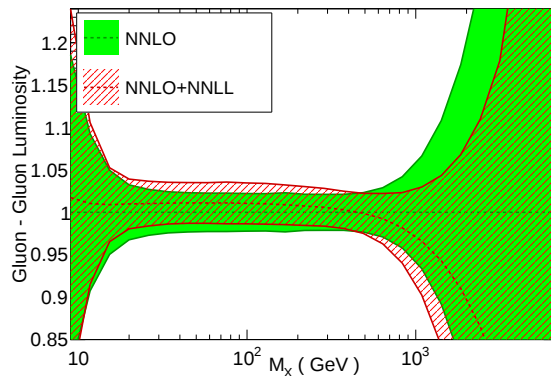
GLUON: NLO vs NLL

LHC 13 TeV, NNPDF3.0 DIS+DY+Top, $\alpha_s(M_Z)=0.118$



GLUON: NNLO vs NNLL

LHC 13 TeV, NNPDF3.0 DIS+DY+Top, $\alpha_s(M_Z)=0.118$

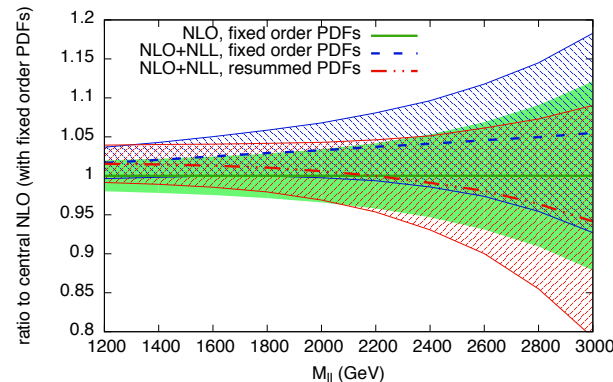


- FIRST SET: NNPDF3.0resum
- RESUMMATION INCLUDED IN FIT (DIS, DY, TOP DATA), EFFECTS NOT NEGLIGIBLE AT NNLO, LARGE x , MORE MODERATE AT NNLO
- EFFECT ON PDFs COMPARABLE TO EFFECT ON MATRIX ELEMENT, ANTICORRELATED TO IT
- RELEVANT FOR NEW PHYSICS SEARCHES

(Bonvini et al., 2015)

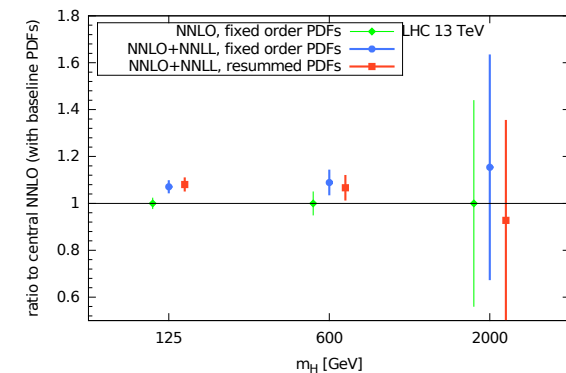
SLEPTON PAIR PRODUCTION

Slepton pair invariant mass, pp @ 13 TeV, $m_l = 564$ GeV.



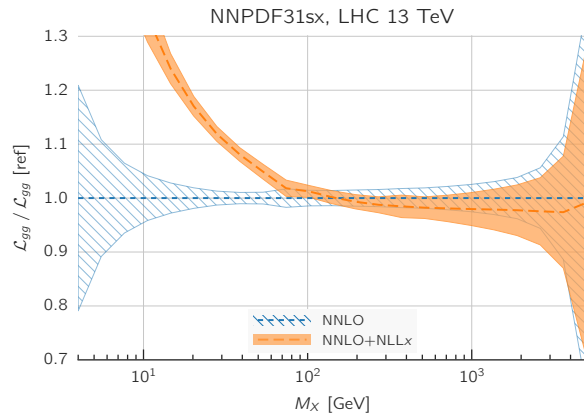
HIGGS IN GLUON FUSION VS m_H

Higgs cross section: gluon fusion



PDFs WITH HIGH ENERGY (SMALL x) RESUMMATION

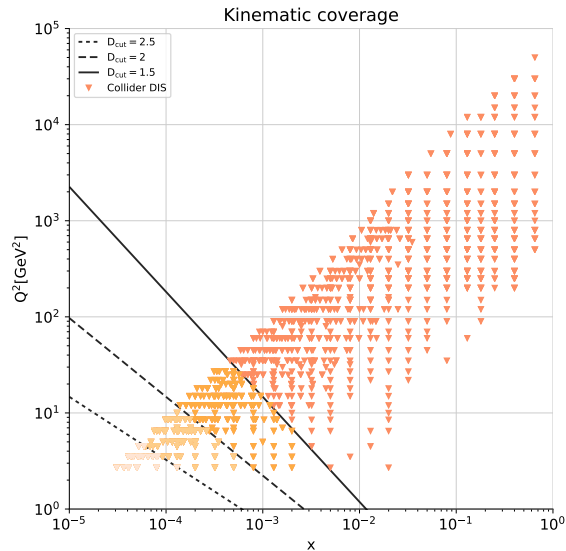
GLUON LUMINOSITY



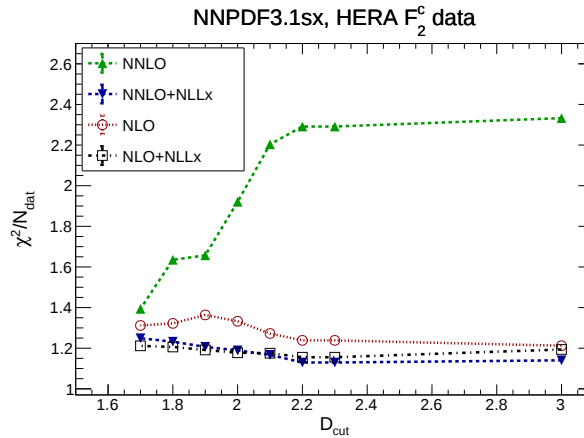
- FIRST SET: NNPDF3.0sx
- HIGH ENERGY RESUMMATION INCLUDED IN GLAP EVOLUTION& FOR DIS, EFFECTS
- STABILIZES PERTURBATIVE EXPANSION
- LARGE EFFECTS FOR FUTURE COLLIDERS, OR LIGHT FINAL STATES (b PRODUCTION AT LHC)

(Ball et al., 2017)

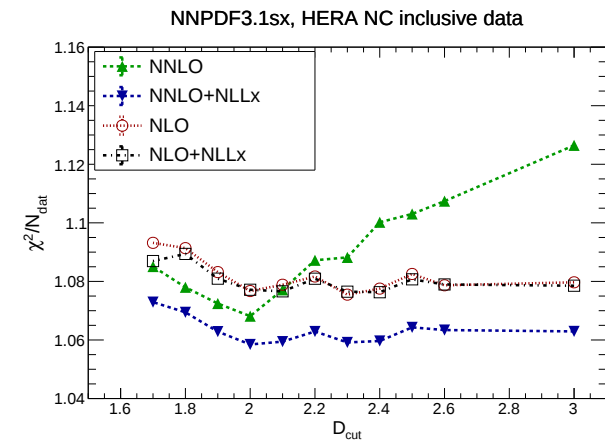
KINEMATIC CUTS



INCLUSIVE F_2 FIT QUALITY

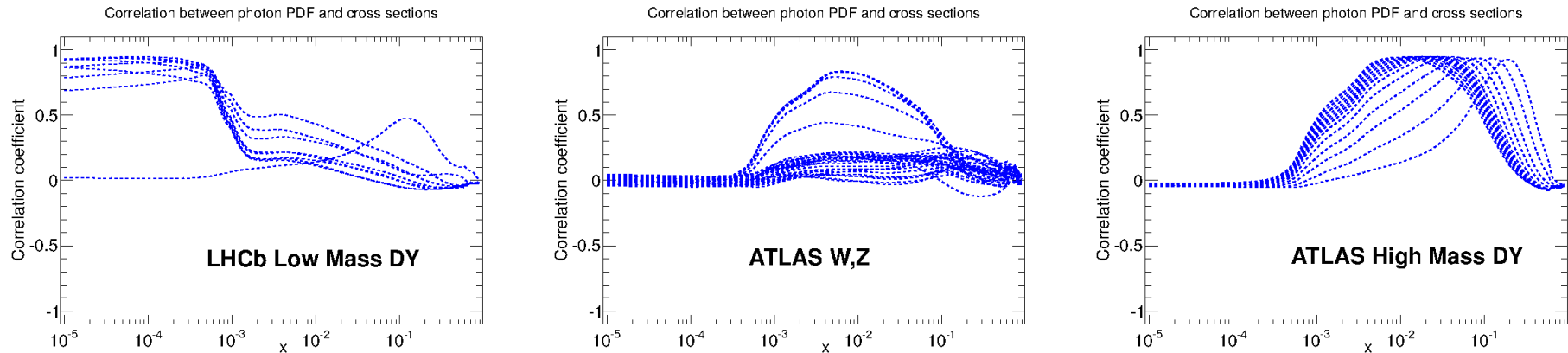


CHARM F_2^c FIT QUALITY



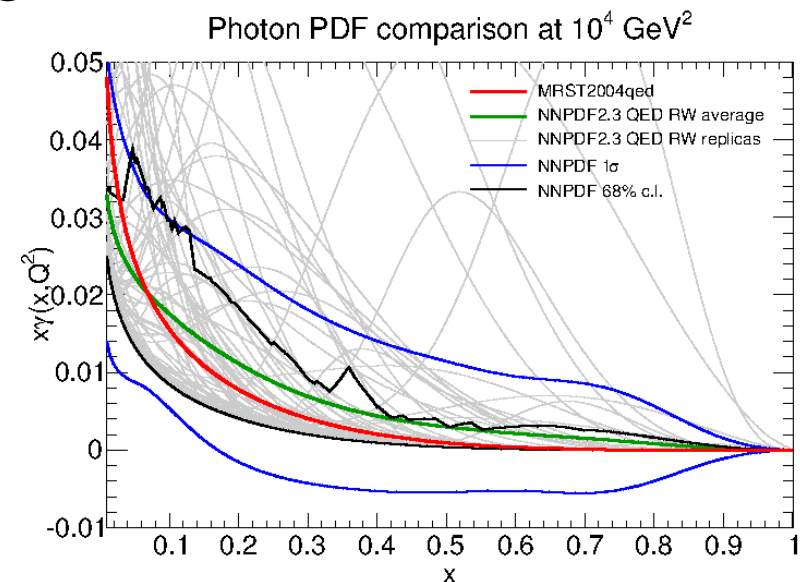
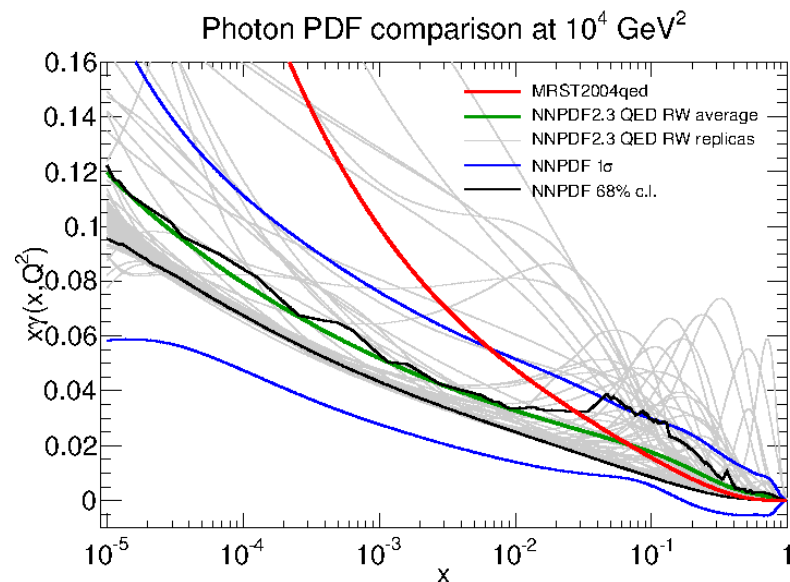
THE PHOTON PDF

CORRELATION BETWEEN DATA AND γ PDF



- **PHOTON-INDUCED** CONTRIBUTIONS CAN BE **SIZABLE**
- **PHOTON PDF** MODELED (MRST2004) OR **DETERMINED FROM DRELL-YAN** WITH **SIZABLE UNCERTAINTY** (NNPDF2.3-NNPDF3.0QED)
- **SIGNIFICANT UNCERTAINTY** EG ON SEARCHES

NNPDF2.3QED PHOTON



THE PHOTON PDF BREAKTHROUGH

(Manohar, Nason, Salam, Zanderighi, 2016)

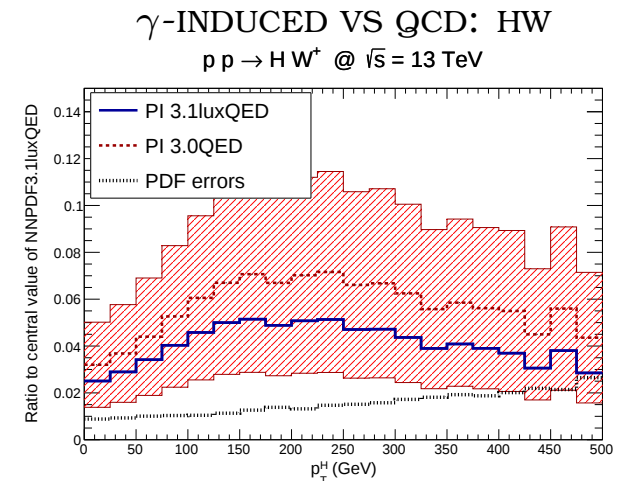
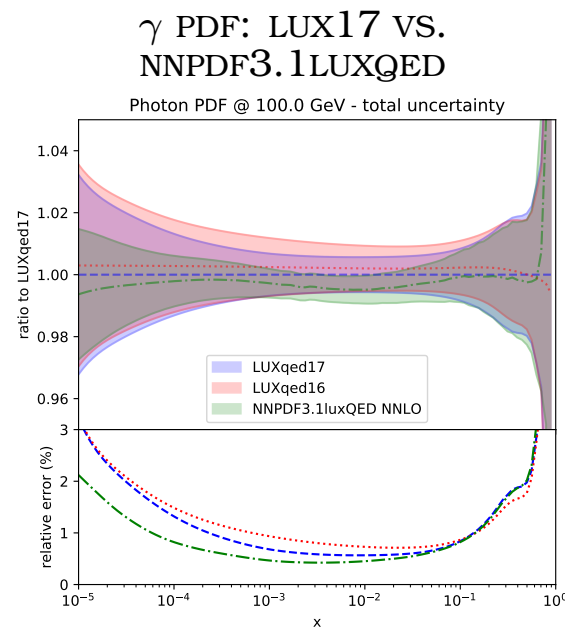
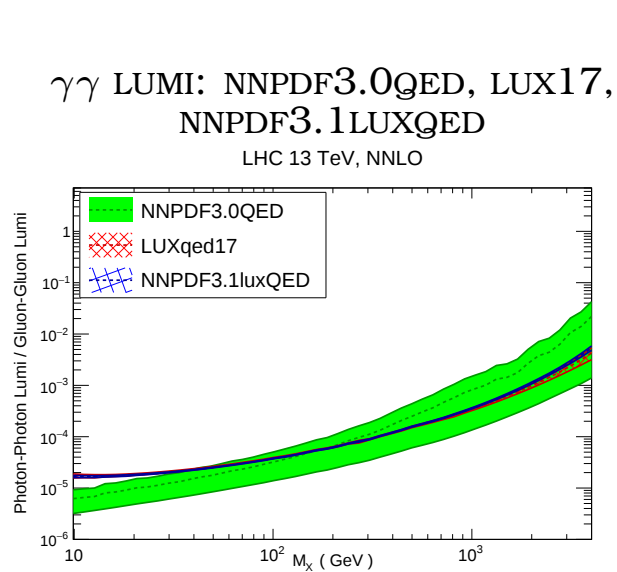
- **QED IS PERTURBATIVE** DOWN TO LOW SCALES $\Rightarrow$ THE **PHOTON PDF** MUST BE **COMPUTABLE** IF THE INPUT QUARK SUBSTRUCTURE IS KNOWN
- WRITE THE CROSS-SECTION FOR A CHOSEN PROCESS:
SUSY PRODUCTION IN EP COLLISION (Drees, Zeppenfeld, 1989)
- COMPUTE IT DIRECTLY, OR USING THE PHOTON PDF
- $\Rightarrow$ **PDF EXPRESSED IN TERMS OF THE STRUCTURE FUNCTION INTEGRATED OVER ALL SCALES**
- F_s AT HIGH Q^2 FROM PDFs, IN RESONANCE REGION FROM DATA, IN ELASTIC LIMIT FROM FORM FACTORS

$$x f_{\gamma/p}(x, \mu^2) = \frac{1}{2\pi\alpha(\mu^2)} \int_x^1 \frac{dz}{z} \left\{ \int_{\frac{x^2 m_p^2}{1-z}}^{\frac{\mu^2}{1-z}} \frac{dQ^2}{Q^2} \alpha^2(Q^2) \left[\left(z p_{\gamma q}(z) + \frac{2x^2 m_p^2}{Q^2} \right) F_2(x/z, Q^2) - z^2 F_L\left(\frac{x}{z}, Q^2\right) \right] - \alpha^2(\mu^2) z^2 F_2\left(\frac{x}{z}, \mu^2\right) \right\},$$

THE LUXQED PHOTON PDF

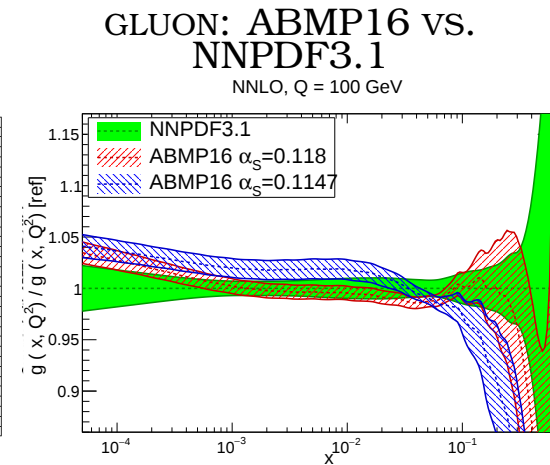
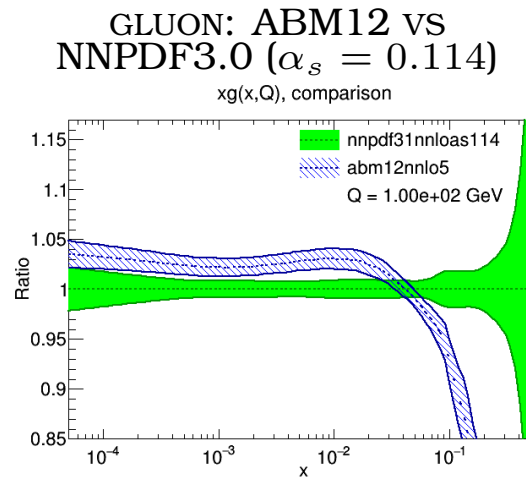
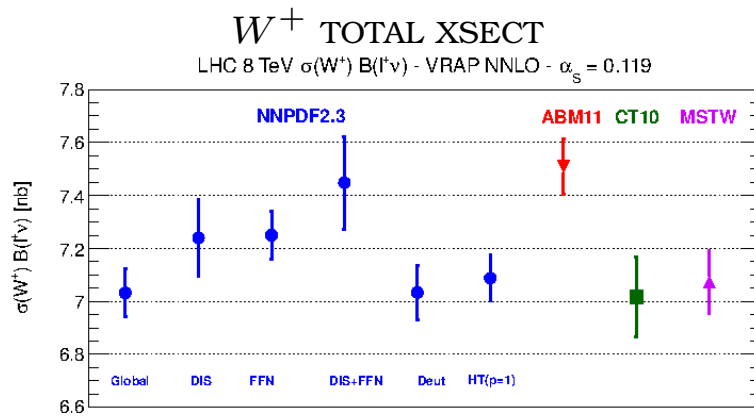
(Carrazza et al., 2017)

- LUX16/LUX17 SETS CONSTRUCTED FROM PDF4LHC15 $\Rightarrow$ AGREE WELL WITH NNPDF3.0 QED, MUCH SMALLER UNCERTAINTY
- FIRST PDF SET BASED ON CONSISTENT FIT WITH LUX CONSTRAINT: NNPDF3.0LUXQED
- NNPDF3.1LUXQED VS LUX17: GOOD AGREEMENT BUT SMALLER UNCERTAINTIES
- SIZABLE IMPACT ON PRECISION PHYSICS: EG ASSOCIATE HIGGS PROD. WITH W



HEAVY QUARKS DECOUPLING SCHEMES

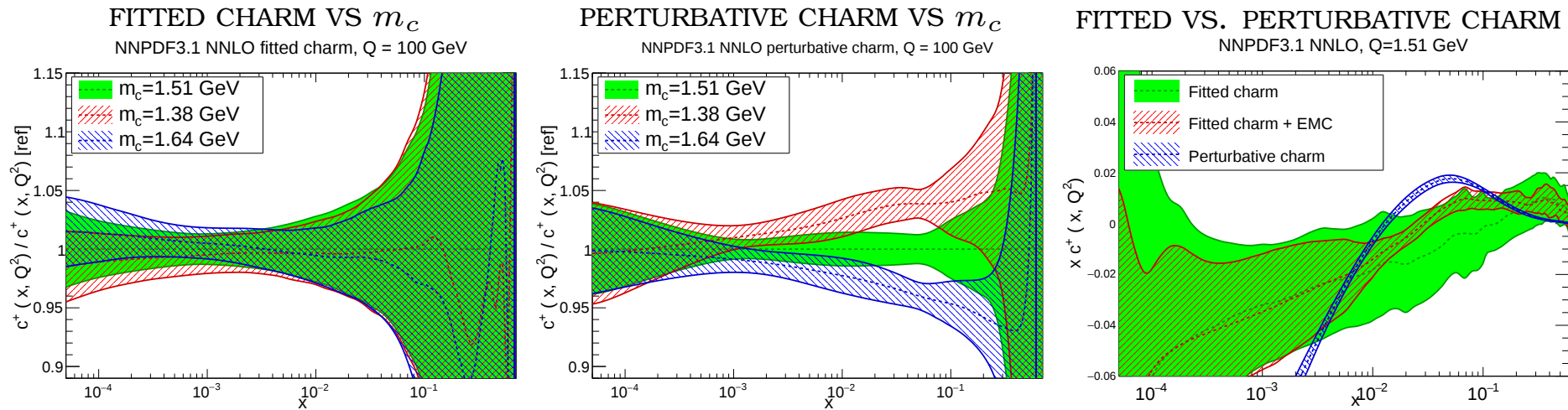
- ALL GLOBAL PDF SETS USE **MATCHED VARIABLE-FLAVOR HQ** SCHEMES
ACOT, FONLL, THORNE-ROBERTS EXTENSIVELY BENCHMARKED 2010-2014
- ABM USE MASSIVE FFN SCHEME
⇒ **SERIOUS DISCREPANCY**, BEST FIT $\alpha_s = 0.113$
- ABMP16 $n_3 f = 3$ FOR DIS, $n_f = 5$ FOR LHC ⇒ EFFECTIVELY, ZM-VFN
⇒ **DISCREPANCY REDUCED**, BEST FIT $\alpha_s = 0.115$



HEAVY QUARKS DETERMINING CHARM FROM THE DATA

WHY SHOULD THE CHARM PDF BE DETERMINED FROM THE DATA?

- BECAUSE ITS SIZE **SHOULD NOT DEPEND** STRONGLY ON THE **CHARM MASS**
- BECAUSE IT MIGHT HAVE A NONPERTURBATIVE COMPONENT

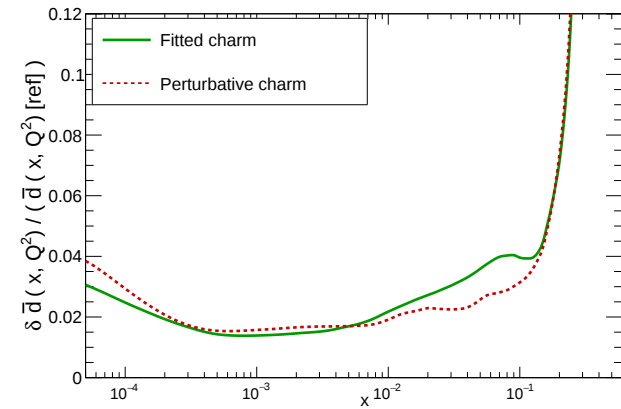
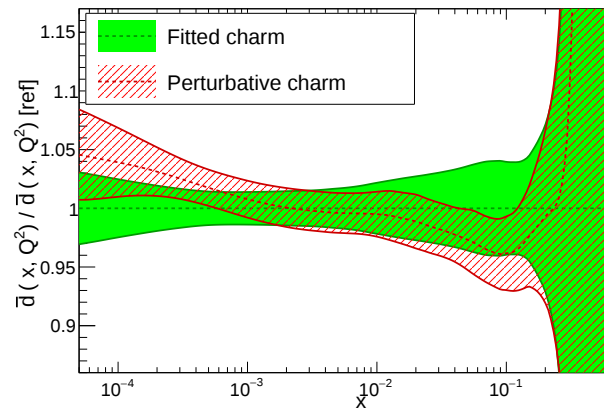
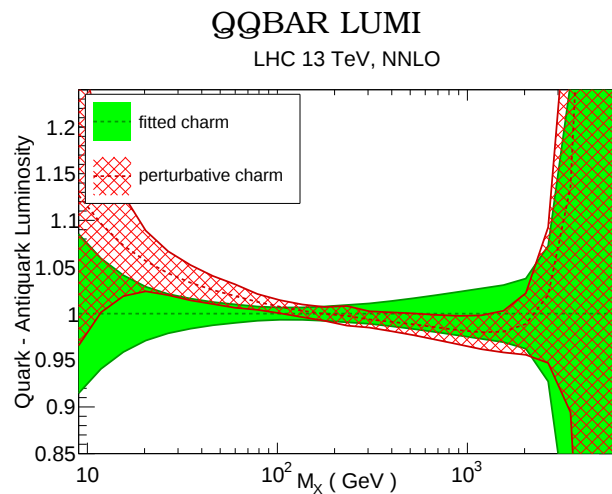


- BECAUSE ITS **SHAPE SHOULD NOT** BE DETERMINED BY **FIRST-ORDER MATCHING** (NO HIGHER NONTRIVIAL ORDERS KNOWN)
- $\Rightarrow$ SUPPRESSED AT MEDIUM-SMALL x , ENHANCED AT VERY SMALL, VERY LARGE x

HEAVY QUARKS IMPACT ON LIGHT QUARK PDFS

FITTED VS. PERTURBATIVE CHARM
ANTIDOWN PDF
NNPDF3.1 NNLO, $Q = 100$ GeV

ANTIDOWN PDF UNCERTAINTY
NNPDF3.1 NNLO, $Q = 100$ GeV

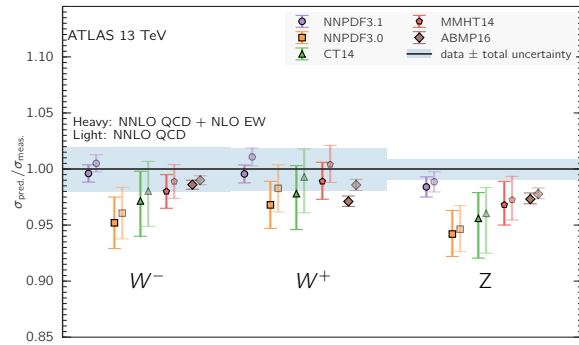


THE CHARM PDF FROM DATA...

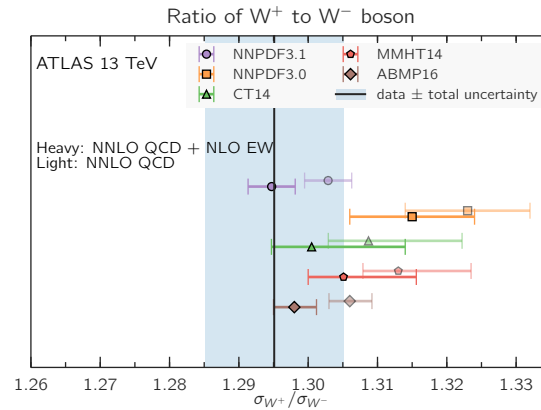
- QUARK (ESPECIALLY QUARK-ANTIQUARK) LUMI AFFECTED BECAUSE OF CHARM SUPPRESSION AT MEDIUM- x
- FLAVOR DECOMPOSITION ALTERED
- UNCERTAINTIES ON LIGHT QUARKS NOT SIGNIFICANTLY INCREASED

HEAVY QUARKS THE CHARM PDF & PRECISION LHC PHYSICS

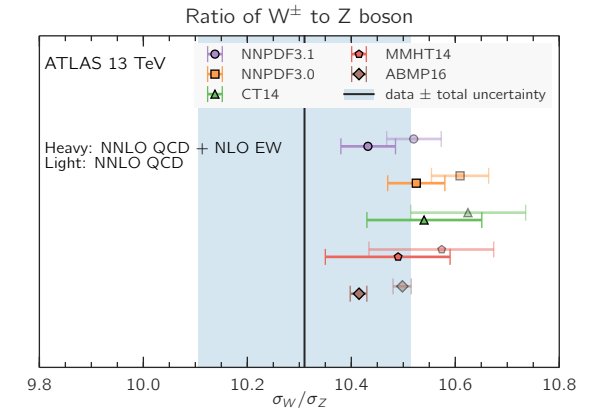
DRELL-YAN XESCTS



W^+/W^- XSECT RATIO



W/Z XSECT RATIO



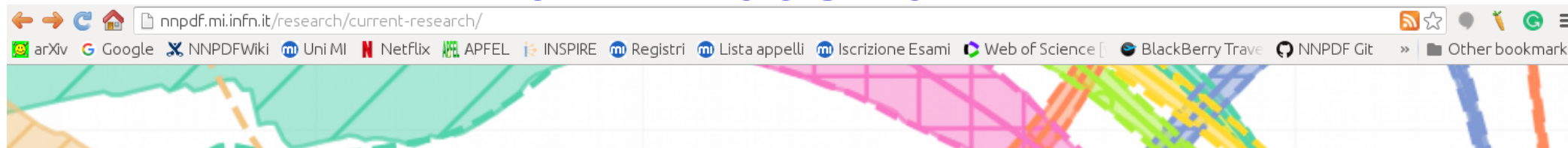
- W , Z CROSS-SECTIONS AT 13 TEV IN PERFECT AGREEMENT WITH DATA
DIFFICULT TO FIT WITH PERTURBATIVE CHARM
- ELECTROWEAK CORRECTIONS IMPORTANT
- NOTE ALSO SMALL- x RESUMMATION OF F_2^c REQUIRES FITTED CHARM

THEORY: SUMMARY

- WITH SUB-PERCENT DATA UNCERTAINTIES, THEORY UNCERTAINTIES
DOMINANT
- RESUMMATION ADVANTAGEOUS
- ELECTROWEAK CORRECTIONS MANDATORY

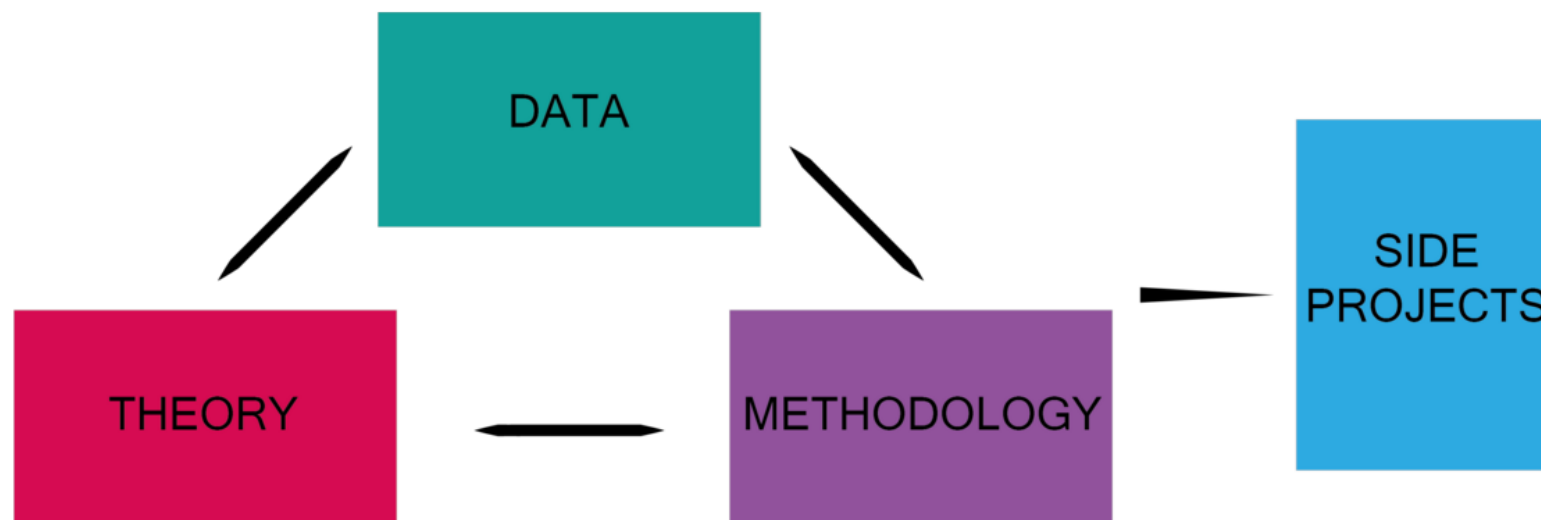
BEYOND THE FRONTIER

OPEN ISSUES



Current research

Click on individual topics for a roadmap with short-term and long-term goals:



DATA

nnpdf.mi.infn.it/research/current-research/data/

arXiv Google NNPdFWiki Uni MI Netflix APFEL INSPIRE Registri Lista appelli Iscrizione Esami Web of Science BlackBerry Travel NNPdF Git Other bookmarks

Data

All to be implemented including NNLO QCD, photon-induced, and NLO electroweak

Short-term goals

OLD DATASETS

- NNPdF3.1 wrap-up: full implementation, restoring data cut because of large PI or EW
 - ATLAS W, Z 7TeV
 - ATLAS high-mass Drell-Yan 8 TeV
 - Low-mass DY
- New datasets for processes already in NNPdF3.1:
 - LHCb 8, 13 TeV W, Z production
 - $t\bar{t}$ 5, 8, 13 TeV
 - jets 8TeV, 13 TeV

NEW DATASETS

- Prompt photons
- Single top
- Dijets

Medium-term goals

In rough order of priority:

NEW DATASETS

- Diboson production
- Z ϕ^* distribution
- Z+c
- Hera jets
- V+jets
- LHC D* production
- W+c



METHODOLOGY

Methodology

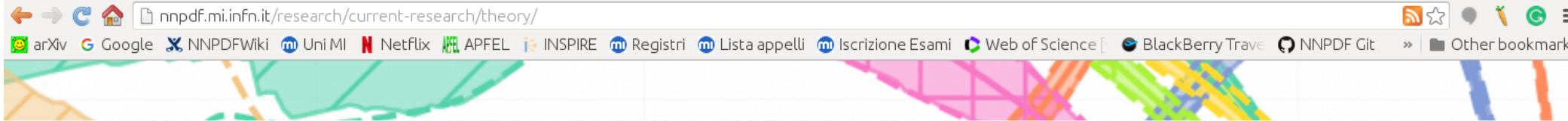
Short-term goals

- PDF parametrization
 - Fit preprocessing
 - Neural network architecture:
 - Single-layer for each PDF
 - One single (multilayer or perhaps deep) NN for all PDFs
- Minimization algorithms
 - CMA algorithm: validation
 - Closure test
 - Check against reweighting
 - Check of positivity
 - CMA algorithm: optimization
 - Grid search

Mid- to long-term goals

- Minimization algorithms
 - CMA algorithm: optimization
 - Gradient-based methods
 - Weight minimization + other new methods

THEORY



Theory

Short to Medium-term goals

- Missing Higher Order Corrections Uncertainties (MHOU)
 - Implementation of scale variation at NLO
 - Determination of the contribution to the covariance matrix due to MHOU estimated with scale variation
 - Fit with the MHOU uncertainty included in the covariance matrix
 - Fit with scale variation in the theory
 - Comparison of:
 - NNLO-NLO shift
 - shift due to scale variation in the fit
 - increase of PDF uncertainties due to MHOU included in covariance matrix
- Nuclear & deuterium corrections:
 - Fit with one or more models
 - Implementation in the covariance matrix as for MHOU
 - Fit with extra nuclear uncertainty
- Full computation for all processes in fit of NLO EW and PI
- Inclusion in the covariance matrix of further uncertainties in the NNLO QCD computation:
 - N³LO terms due to the use of K-factors
 - Uncertainties on NNLO corrections due to numerical instabilities, estimated by refitting

Medium to Long-term goals

- Implementation of scale variation at NNLO
- Alternative ways of estimating MHOU, including constrained partial dataset fitting
- Approximate N³LO PDFs



SIDE PROJECTS

arXiv Google NNPDFWiki Uni MI Netflix APPEL INSPIRE Registri Lista appelli Iscrizione Esami Web of Science BlackBerry Travel NNPDF Git Other bookmarks

NNPDF

Home

The collaboration

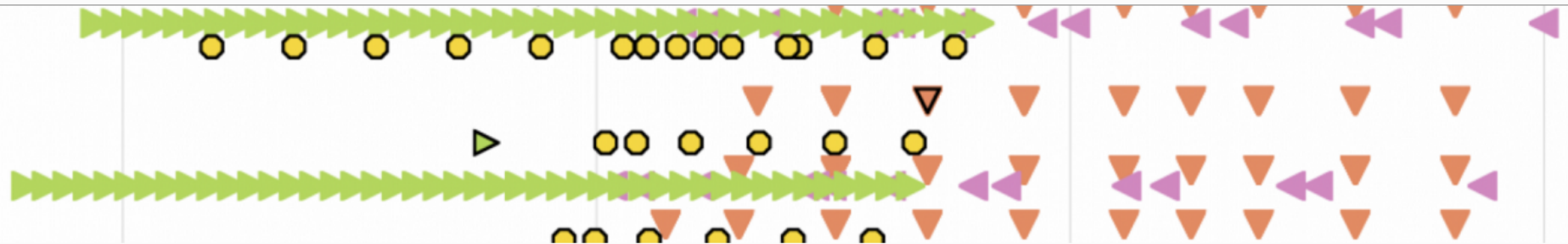
Research

For users

Documents

News

For the public



Side projects

Short-term goals

- Jets: choice of scale and comparison of theory predictions to data before inclusion in the fit
- Polarized PDFs
- Fragmentation functions

Medium-term goals

- Polarized PDFs
- Fragmentation functions
- Resummed PDF sets for LHC phenomenology
- PDFs at the LH-HE collider

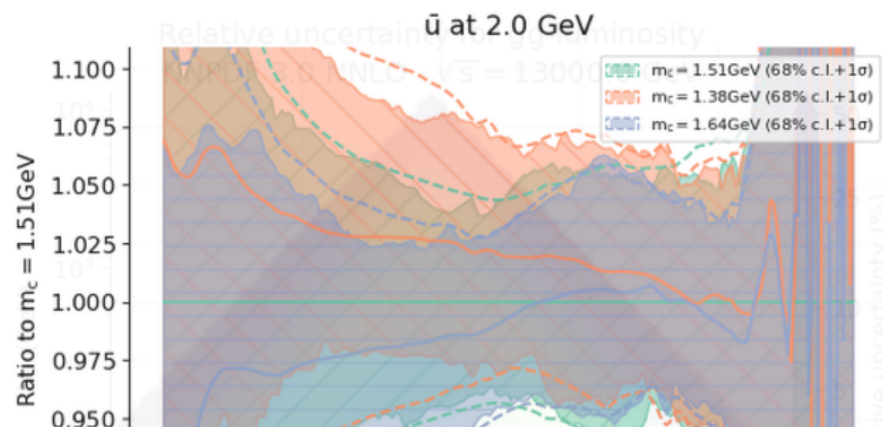
N³PDF

Machine Learning • PDFs • QCD



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The **N³PDF** project, led by PI **Stefano Forte**, aims at revolutionizing the theory of strong interactions and its application to the determination of the structure of the proton, by introducing extensively techniques of artificial intelligence (AI). The core of the project is the development of an AI agent for the determinations of the parton distributions which encode the quark and gluon structure of the proton, using machine learning techniques. The project also includes an integrated set of studies on higher-order computations and resummation in perturbative QCD, and the development of parton distributions interfaced to resummation and Monte Carlo generators. The project will work in synergy with the **NNPDF collaboration**, to which it will provide methods and tools, and from which it will gain physics input and insight.



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Jon Butterworth
@jonmbutterworth

After 40 years of studying the strong nuclear force, a revelation theguardian.com/science/life-a-...
Me at Life & #Physics on BFKL and all that.

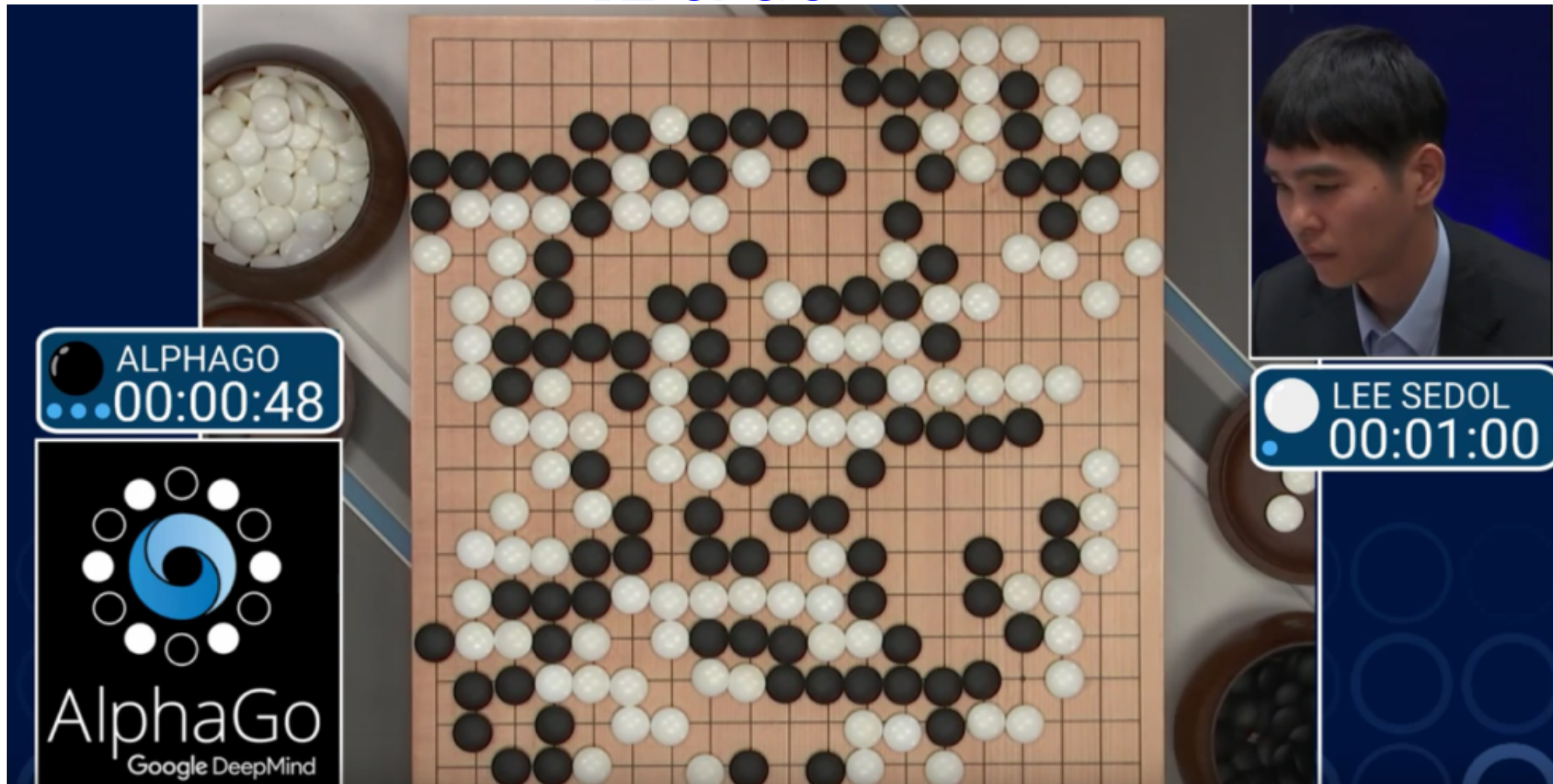
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JOBS

There are currently no positions available but we will be looking for two PhD students very soon!

AI & GO



AI & PDFs

