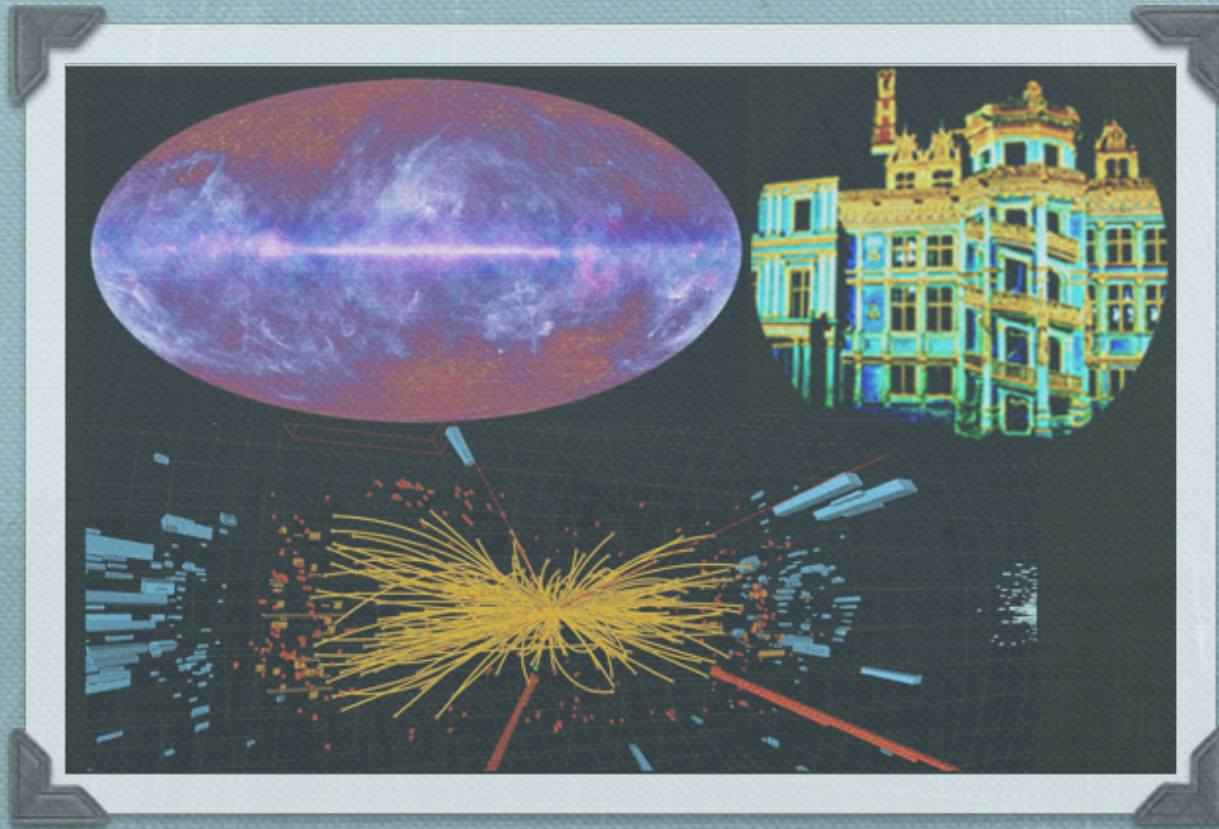


26th Rencontres de Blois, Particle Physics and Cosmology, Blois, France  
20th May 2014



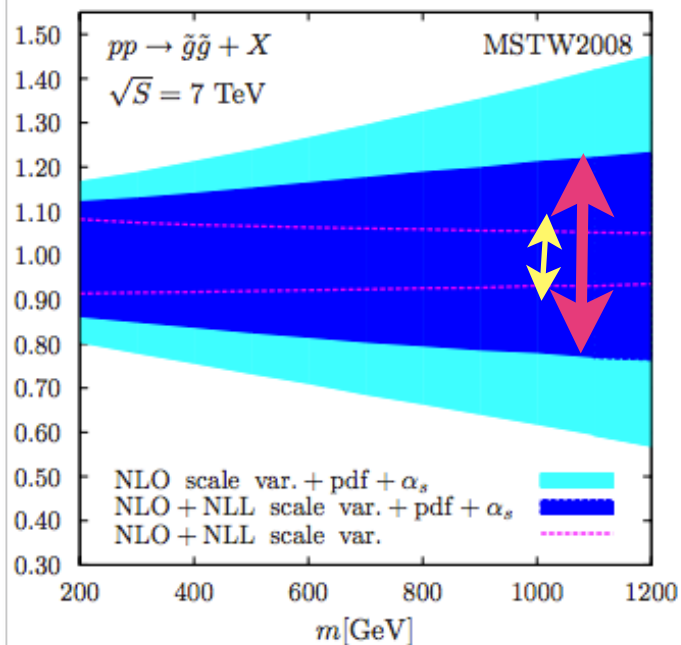
# The structure of the proton and the LHC



*Maria Ubiali*  
*University of Cambridge*



# PDFs: why bother?



Beenakker et al (2011)

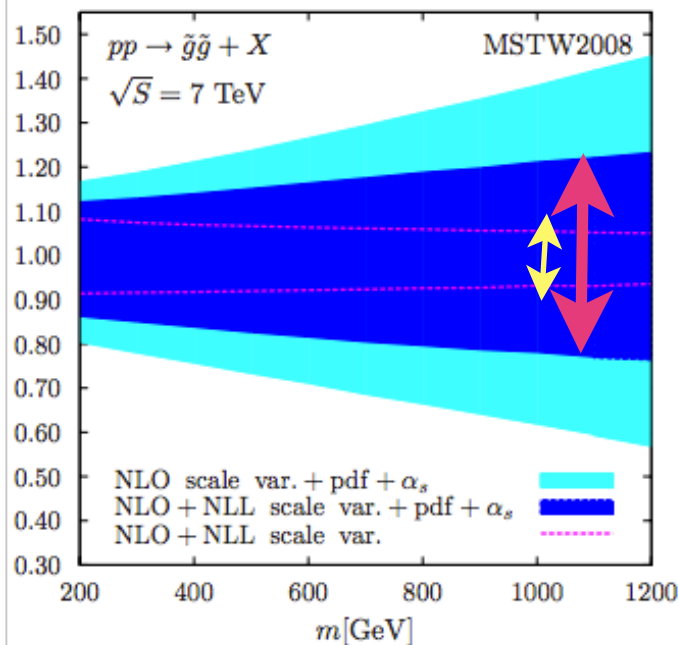
	$\sigma$ (8 TeV)	uncertainty	
gg $\rightarrow$ H	19.5 pb	14.7%	
VBF	1.56 pb	2.9%	
WH	0.70 pb	3.9%	
ZH	0.39 pb	5.1%	
ttH	0.13 pb	14.4%	

J. Campbell, ICHEP 2012

- ◆ PDF uncertainty dominant for many SM predictions
- ◆ Precision in predicting BSM heavy particles is limited by large quark-antiquark uncertainties at large x. Reduction of theoretical uncertainty achieved by using resummed predictions still has 15% uncertainty due to PDFs



# PDFs: why bother?



Beenakker et al (2011)

	$\sigma$ (8 TeV)	uncertainty	
gg $\rightarrow$ H	19.5 pb	14.7%	
VBF	1.56 pb	2.9%	
WH	0.70 pb	3.9%	
ZH	0.39 pb	5.1%	
ttH	0.13 pb	14.4%	

scale  
 PDF+ $\alpha_s$

J. Campbell, ICHEP 2012

## PDFs

PDFs uncertainties are a crucial input at the LHC, often being the limiting factor in the accuracy of theoretical predictions, both SM and BSM

## LHC

Exploit the power of precise LHC data to reduce PDF uncertainties and discriminate among PDF sets



# Outline

- ◆ Introduction

  - ◆ Parton Distribution Functions

- ◆ PDFs at the LHC

  - ◆ The state of the art

- ◆ LHC for PDFs

  - ◆ Constraints from data

- ◆ Conclusions and outlook



# Parton Distribution Functions

$$\frac{d\sigma_H^{pp \rightarrow ab}}{dX} = \sum_{i,j=1}^{N_f} f_i(x_1, \mu_F) f_j(x_2, \mu_F) \frac{d\sigma_H^{ij \rightarrow ab}}{dX}(x_1 x_2 S_{\text{had}}, \alpha_s(\mu_R), \mu_F) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^{2n}}{S_{\text{had}}^n}\right)$$

PDFs cannot be computed in perturbative QCD but they are universal and their evolution with the scale is predicted by pQCD

$$\mu^2 \frac{\partial f(x, \mu^2)}{\partial \mu^2} = \int_z^1 \frac{dz}{z} \frac{\alpha_s}{2\pi} P(z) f\left(\frac{x}{z}, \mu^2\right)$$

Dokshitzer, Gribov, Lipatov, Altarelli, Parisi  
renormalization group equations

**LO** - Dokshitzer; Gribov, Lipatov; Altarelli, Parisi, 1977

**NLO** - Floratos, Ross, Sachrajda; Floratos, Lacaze, Kounnas, Gonzalez-Arroyo, Lopez, Yndurain; Curci, Furmanski Petronzio, 1981

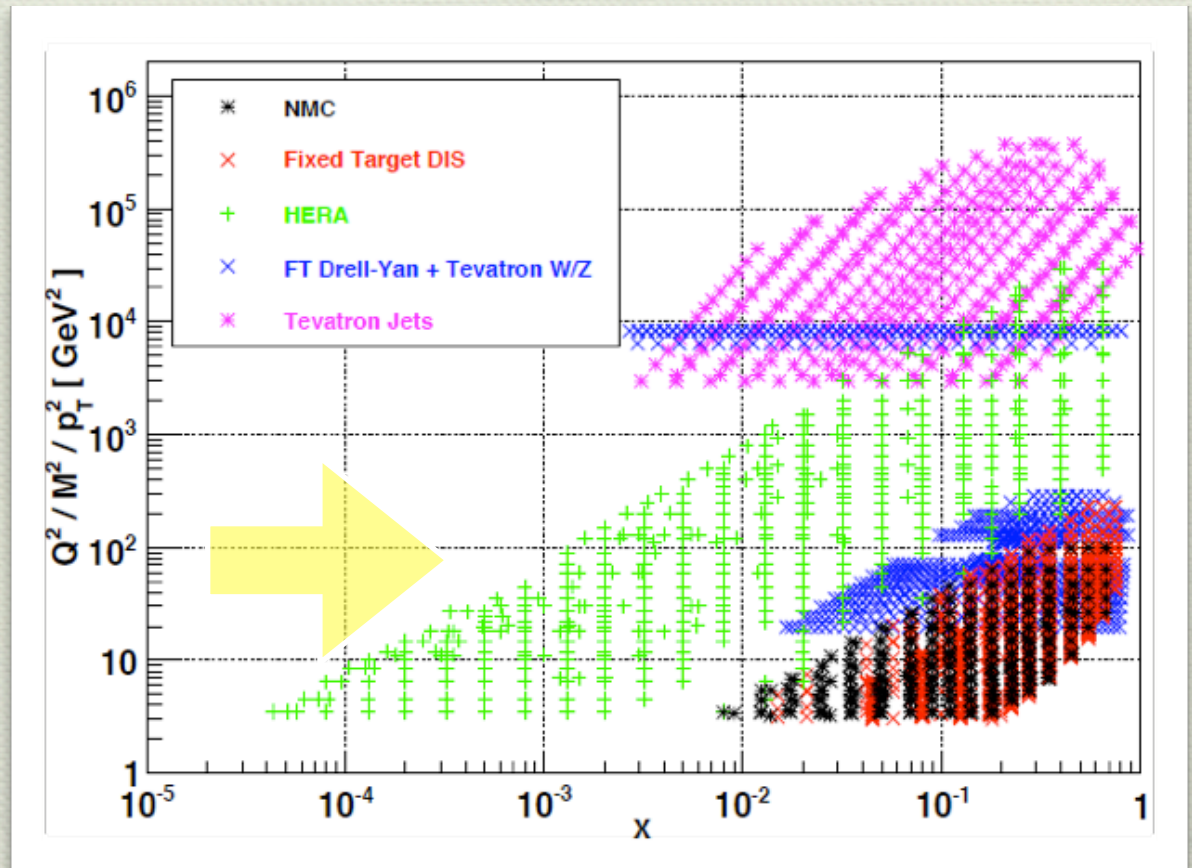
**NNLO** - Moch, Vermaseren, Vogt, 2004



# Parton Distribution Functions

$$\frac{d\sigma_H^{pp \rightarrow ab}}{dX} = \sum_{i,j=1}^{N_f} f_i(x_1, \mu_F) f_j(x_2, \mu_F) \frac{d\sigma_H^{ij \rightarrow ab}}{dX}(x_1 x_2 S_{\text{had}}, \alpha_s(\mu_R), \mu_F) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^{2n}}{S_{\text{had}}^n}\right)$$

- They can be extracted from available experimental data and used as phenomenological input for theory predictions
- Different data constrain different parton combinations at different  $x$

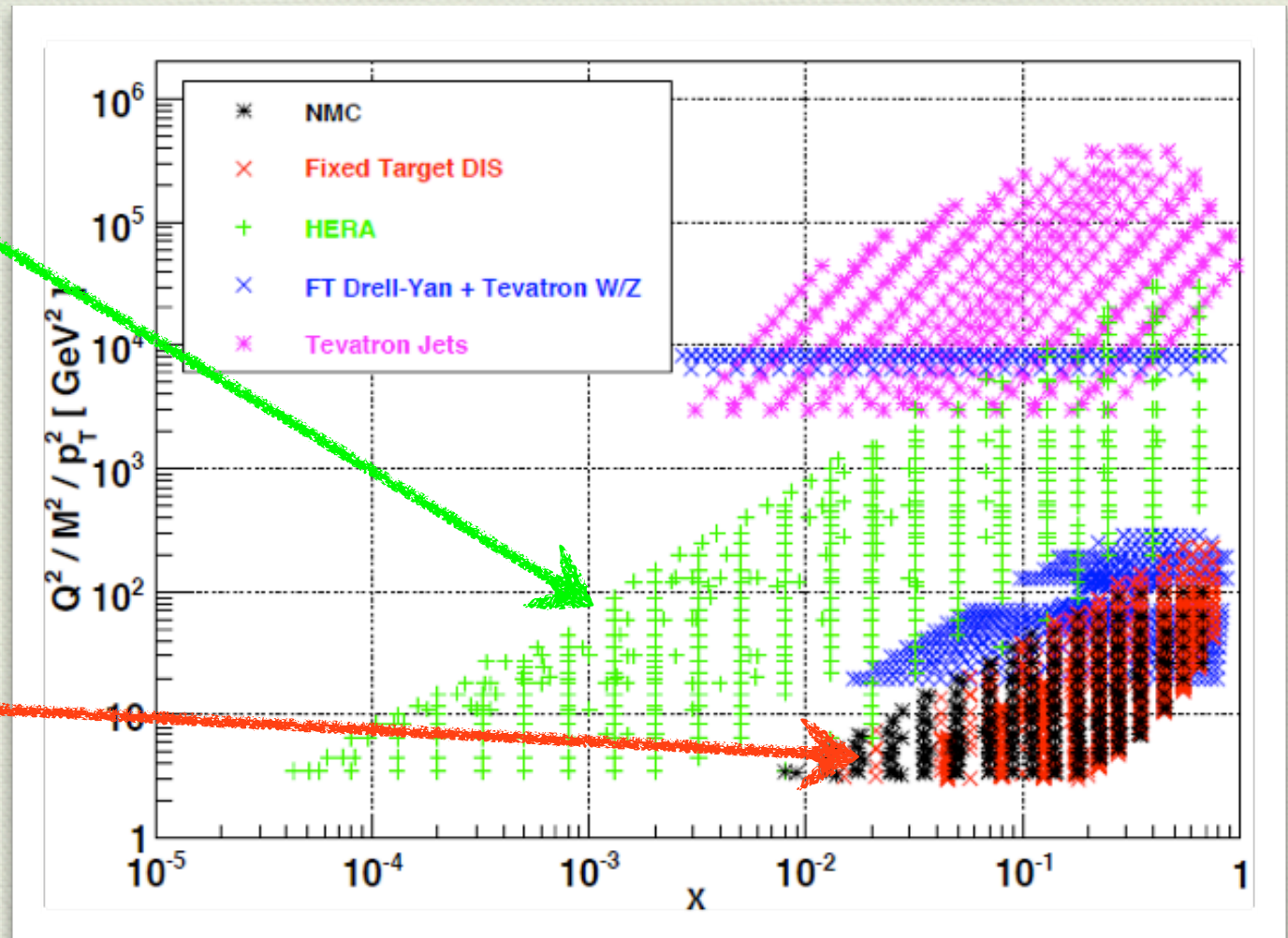




# Constraints from data (pre-LHC)

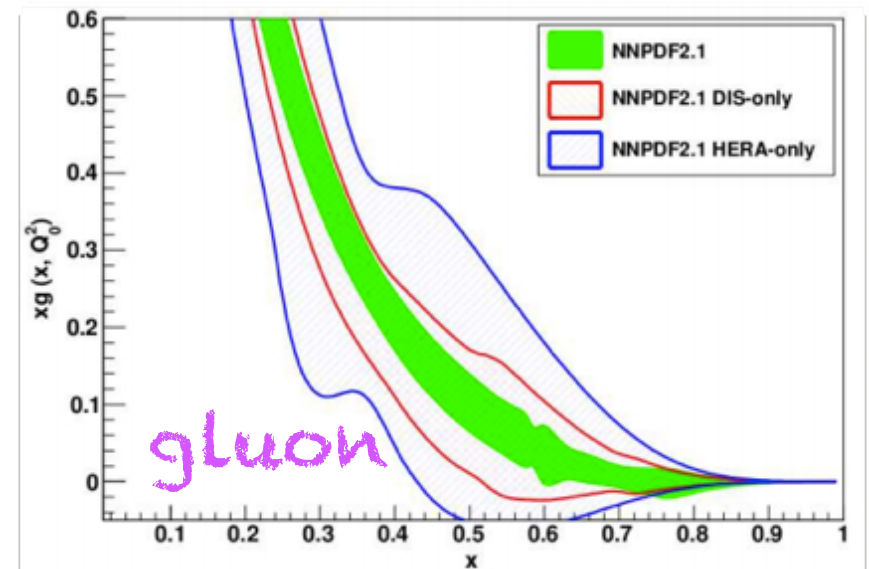
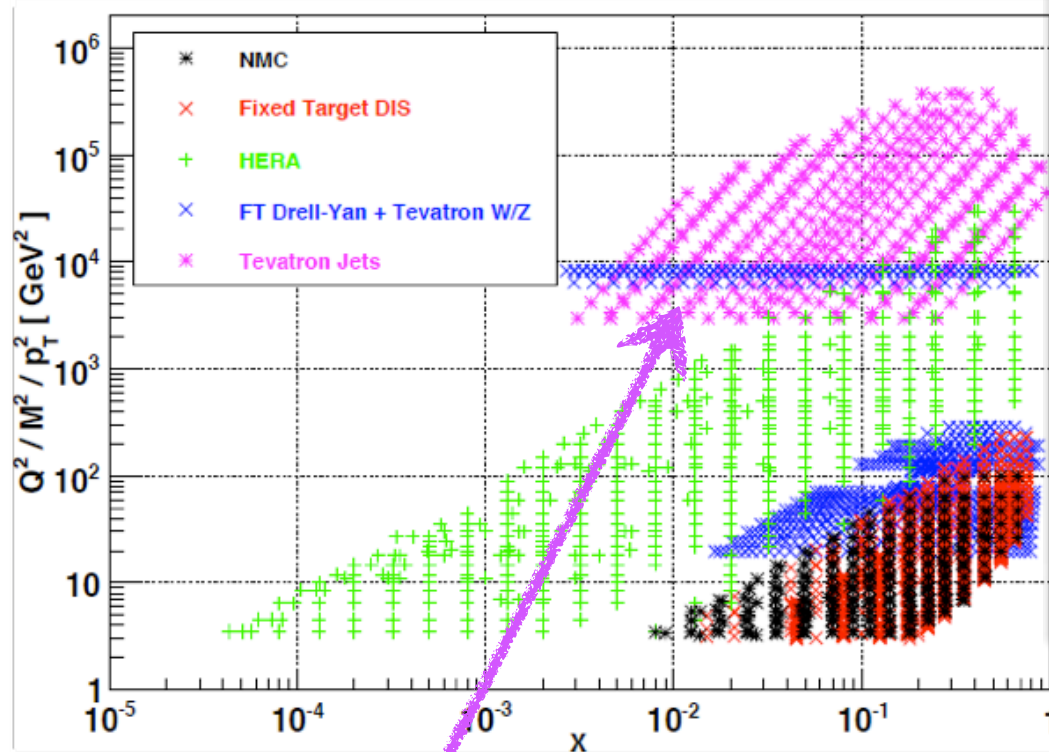
## DIS data

- ◆  $q, qbar$  at  $x > 10^{-4}$
- ◆  $g$  at small and medium  $x$
- ◆ deuteron data:  
disentangle isospin triplet  
and singlet contributions
- ◆ neutrino DIS data:  
handle on strange





# Constraints from data (pre-LHC)



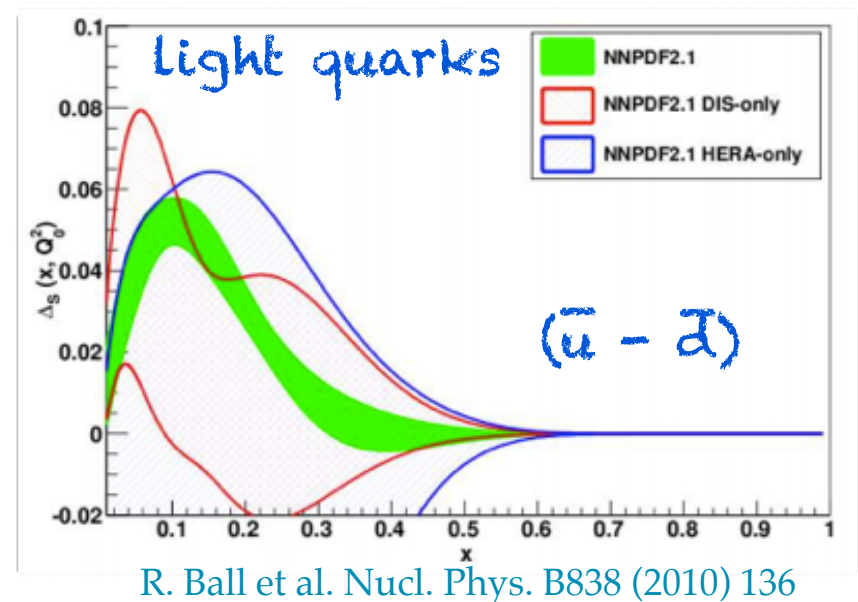
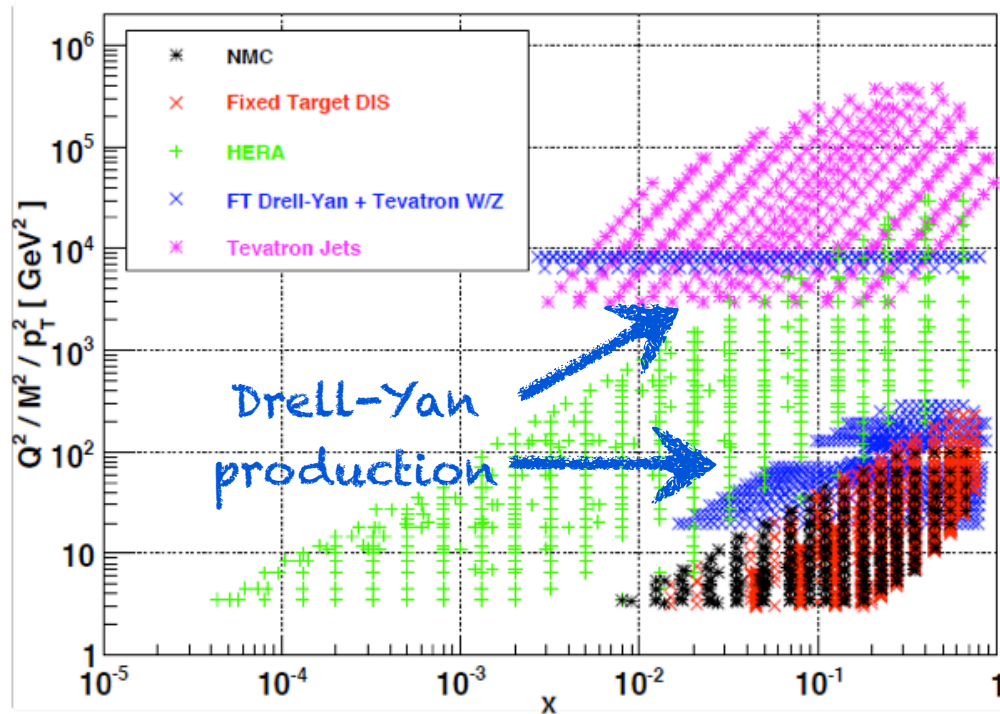
R. Ball et al. Nucl. Phys. B838 (2010) 136

## Tevatron jets

- ◆ Good consistency with DIS data, i.e. scaling violation
- ◆ Largest impact on large- $x$  gluon
- ◆ Significant improvements in accuracy, uncertainty reduced by factor of 2 for  $0.1 < x < 0.7$



# Constraints from data (pre-LHC)



$$\sigma^{\text{DY},p} \propto u(x_1)\bar{u}(x_2) + d(x_1)\bar{d}(x_2)$$

$$\sigma^{\text{DY},d} \propto u(x_1)(\bar{u} + \bar{d})(x_2) + d(x_1)(\bar{u} + \bar{d})(x_2)$$

Old fixed-target **DY** and Tevatron vector boson production data constrain light quark separation and disentangle quark-antiquark distributions



PDFs: state of the art



# Progress in PDF determination

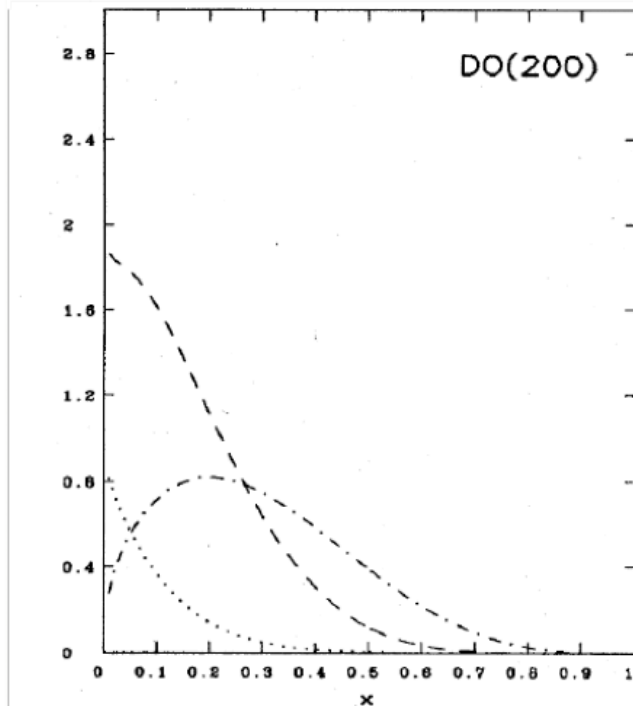
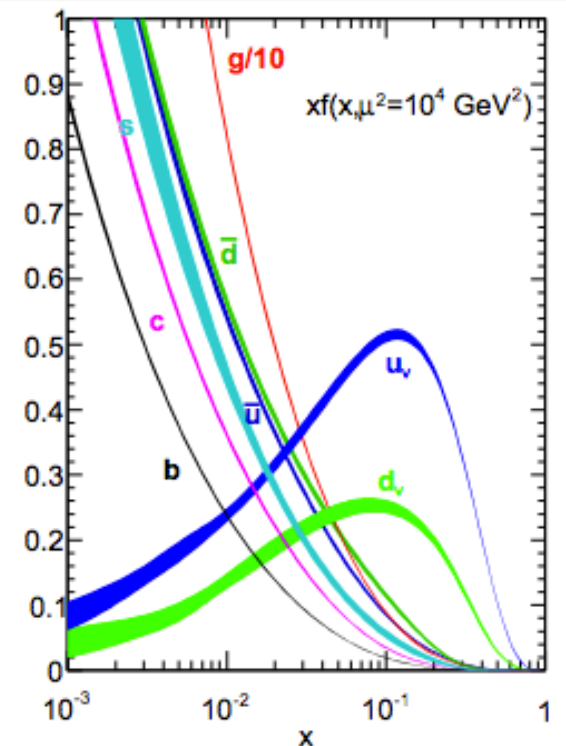
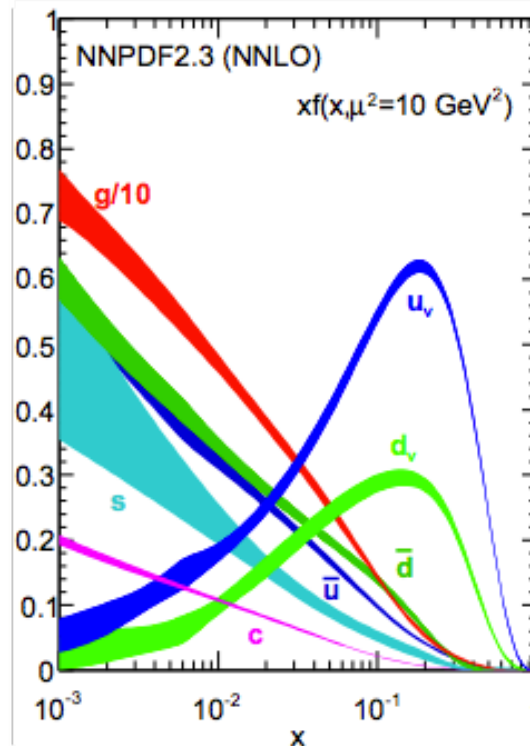


FIG. 27. "Soft-gluon" ( $\Lambda=200$  MeV) parton distributions of Duke and Owens (1984) at  $Q^2=5$  GeV<sup>2</sup>: valence quark distribution  $x[u_v(x)+d_v(x)]$  (dotted-dashed line),  $xG(x)$  (dashed line), and  $q_v(x)$  (dotted line).



PDG "Structure Functions"2013

- ◆ **< 2002:** sets without uncertainty
- ◆ **2003-2004:** first MRST, CTEQ, Alekhin sets with uncertainties
- ◆ **2004-now:** huge progress made in statistical and theoretical understand, new players



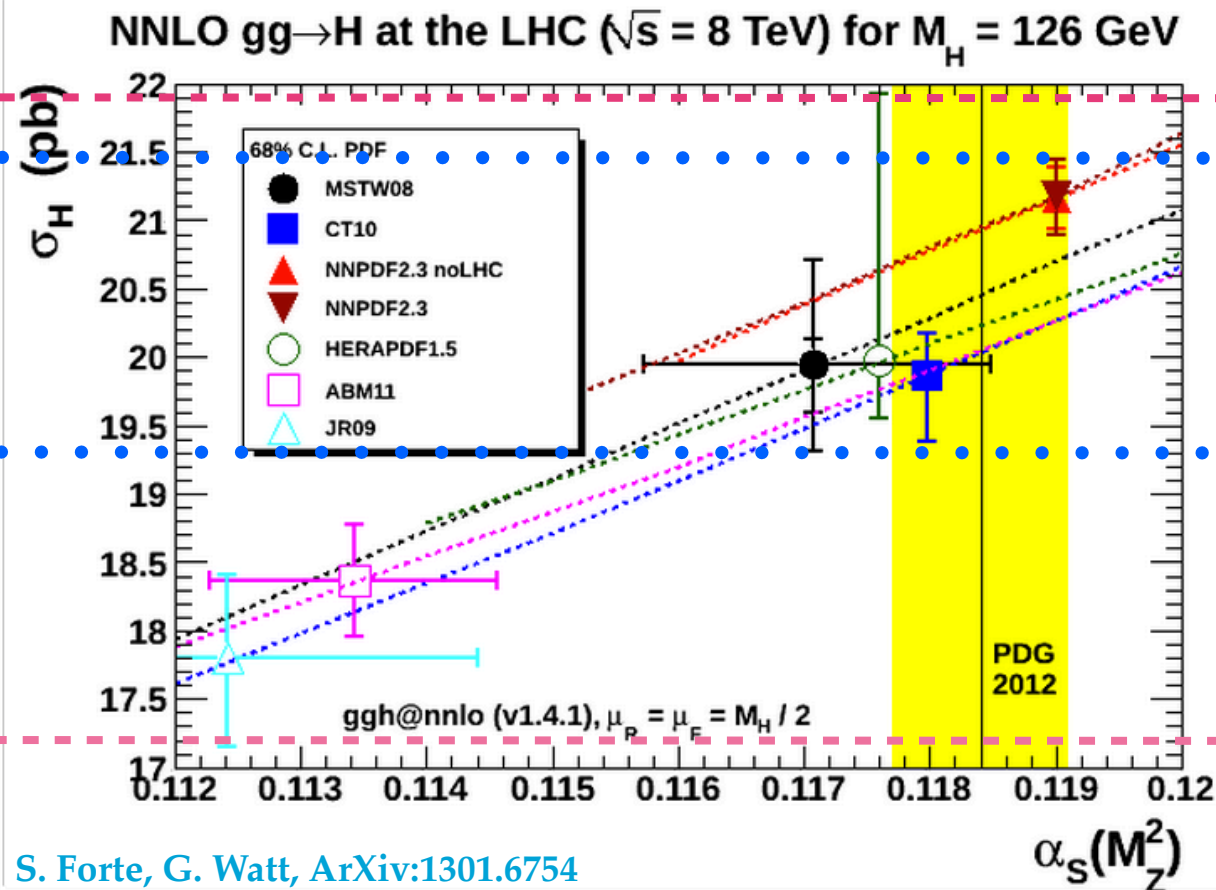
# Modern sets of PDFs

LHAPDF6.1.0 - <https://lhapdf.hepforge.org>

May 2014	CT10(w)	MSTW2008	NNPDF23	ABM12	HERAPDF15
Fixed Target DIS	✓	✓	✓	✓	✗
HERA	✓	✓	✓	✓	✓
Fixed Target DY	✓	✓	✓	✓	✗
Tevatron W,Z	✓	✓	✓	✗	✗
Tevatron jets	✓	✓	✓	✗	✗
LHC data	✗	✗	✓	✓	✗
Stat. treatment	Hessian $\Delta\chi^2=100$	Hessian $\Delta\chi^2$ dynamical	Monte Carlo	Hessian $\Delta\chi^2=1$	Hessian $\Delta\chi^2=100$
Parametrization	Pol. (26 pars)	Pol. (20 pars)	NN (259 pars)	Pol. (14 pars)	Pol. (14 pars)
HQ scheme	ACOT- $\chi$	TR'	FONLL	FFN	TR'
$\alpha_s$	Varied	Fitted+varied	Varied	Fitted	Varied



# Predictions for the LHC



S. Forte, G. Watt, ArXiv:1301.6754

◆ Gluon fusion initiated Higgs productions

◆ Wide spread of predictions limits accuracy in Higgs characterization

◆ Global sets quite close to each others and compatible to HERA analysis

◆ Larger discrepancies with ABM and JR

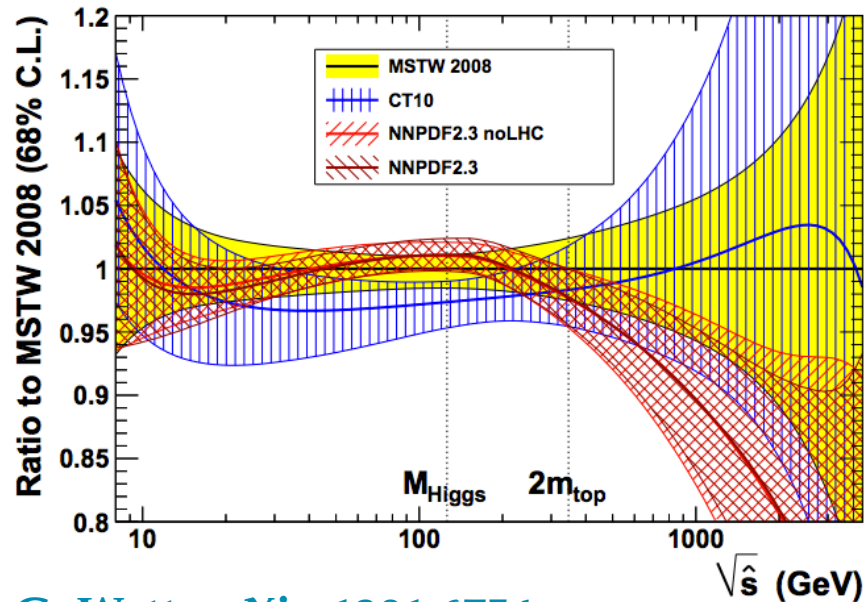
◆ Similar (worse) situation for  $t\bar{t}$  cross section predictions



# Parton Luminosities

Directly connected with gluon-gluon luminosity

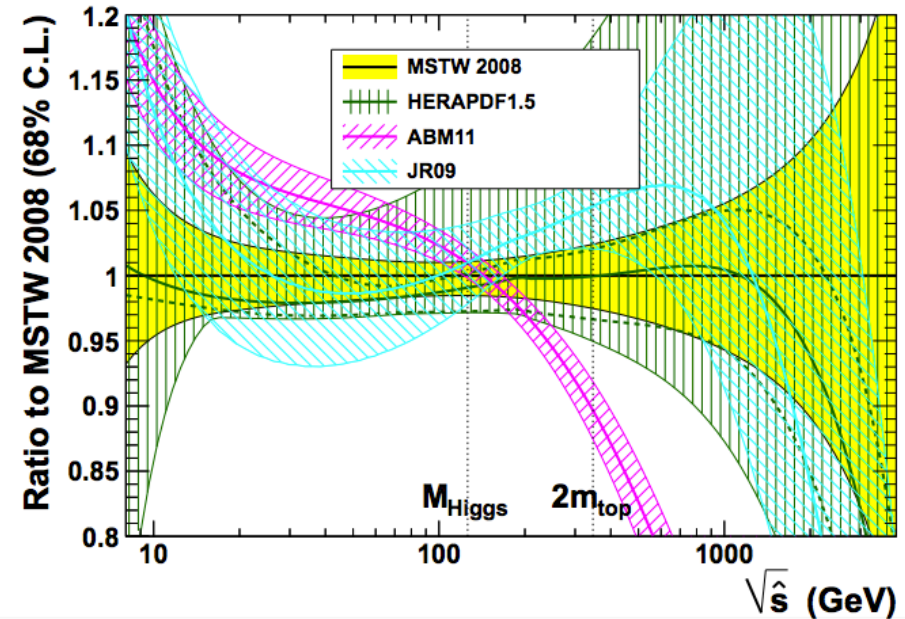
NNLO gg luminosity at LHC ( $\sqrt{s} = 8$  TeV)



G. Watt (November 2012)

G. Watt, arXiv:1301.6754

NNLO gg luminosity at LHC ( $\sqrt{s} = 8$  TeV)

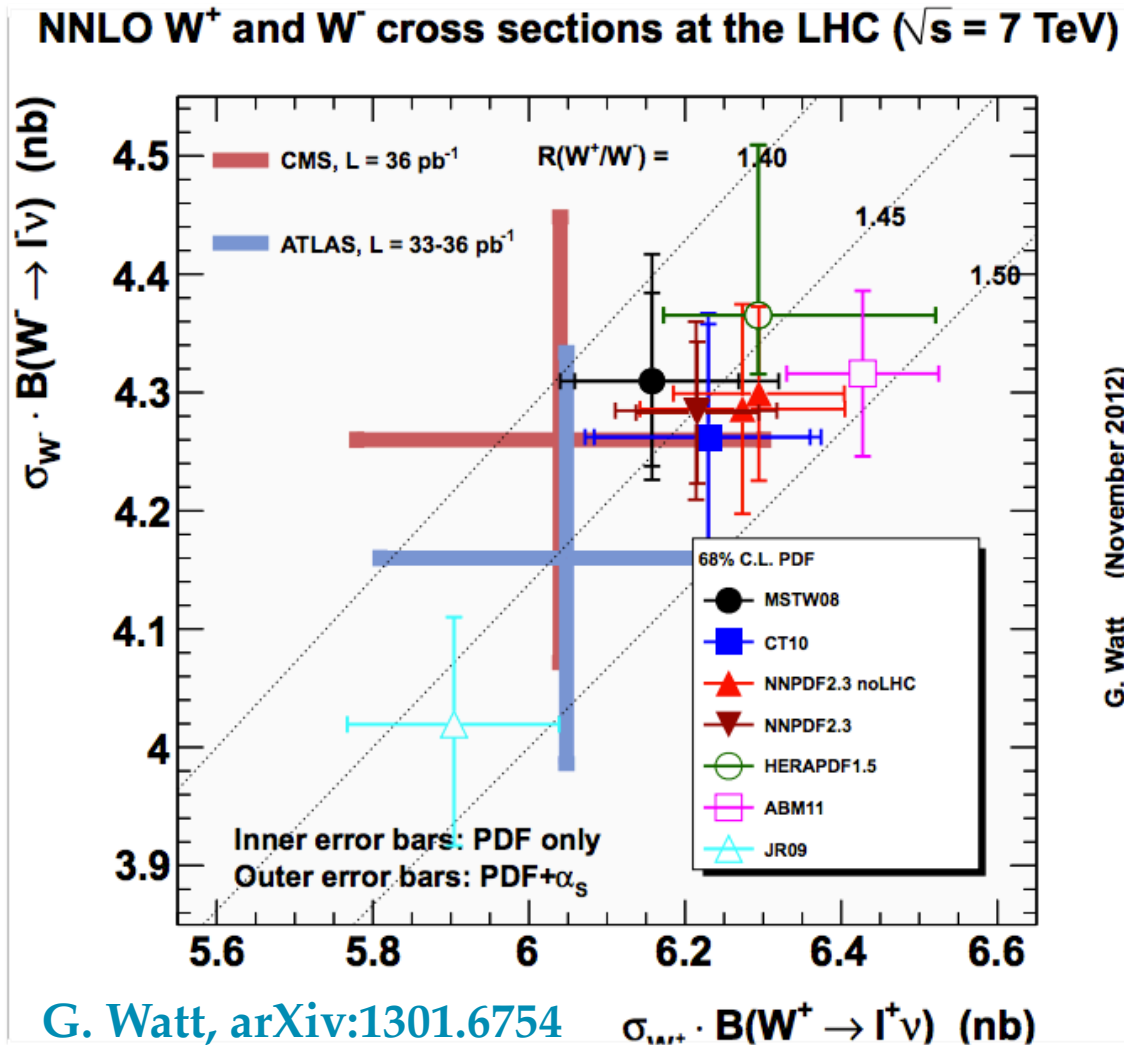


G. Watt (November 2012)

$$\Phi_{ij}(M_X^2) = \frac{1}{s} \int_{\tau}^1 \frac{dx}{x} f_i(x, M_X^2) f_j\left(\frac{\tau}{x}, M_X^2\right)$$



# Predictions for the LHC



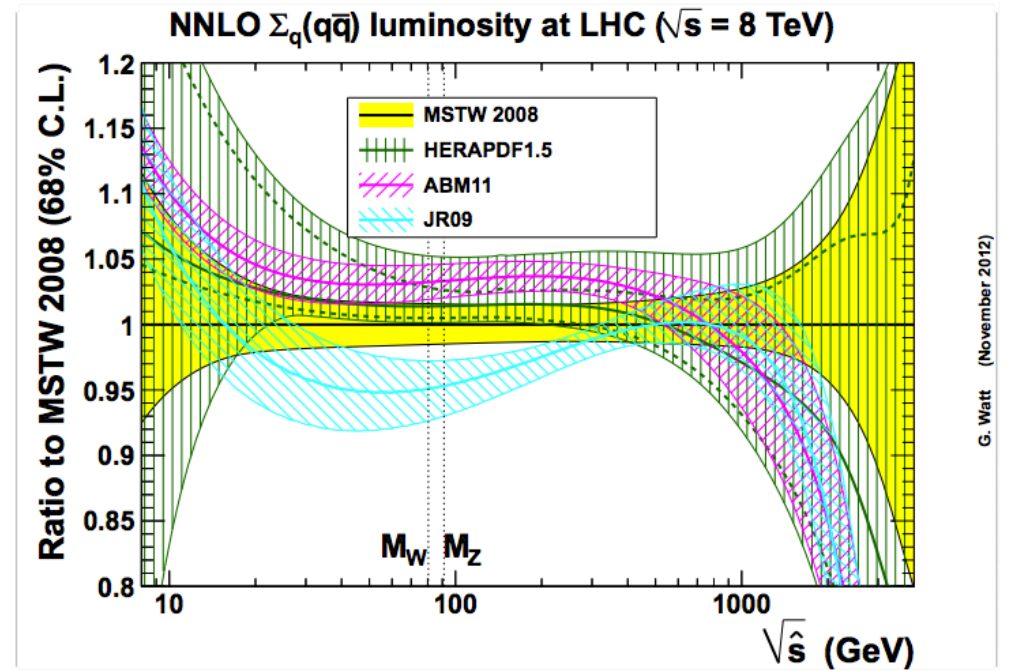
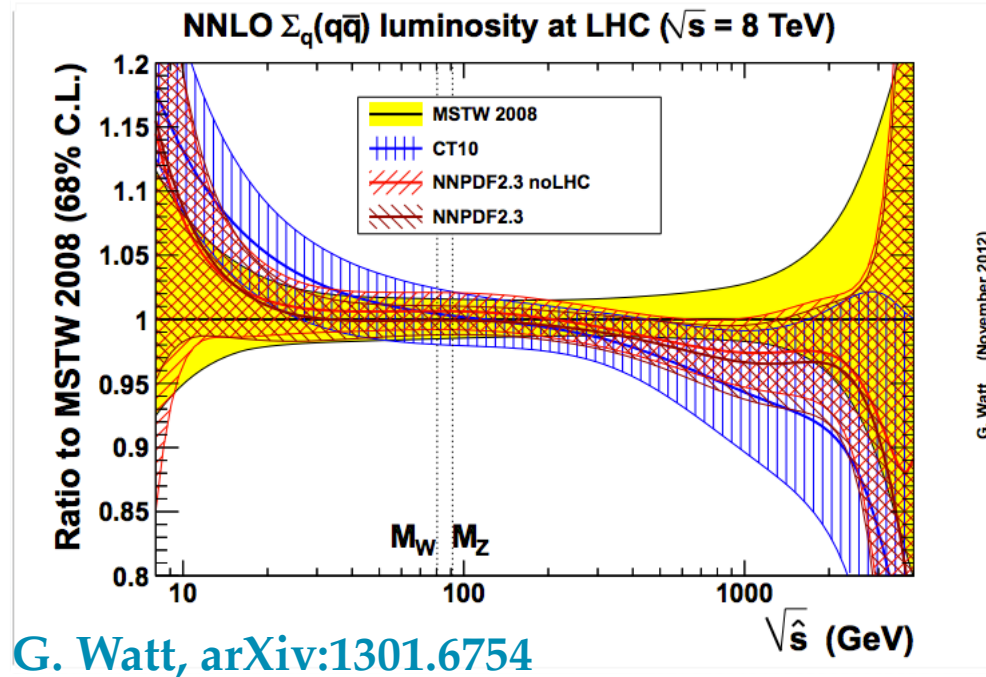
G. Watt (November 2012)

- ◆ For W and Z productions (quark dominated) situation is less dramatic
- ◆ Predictions mostly close to each others
- ◆ More significant discrepancies with ABM and JR
- ◆ Compatible with data, although data the more precise the more discriminating



# Parton Luminosities

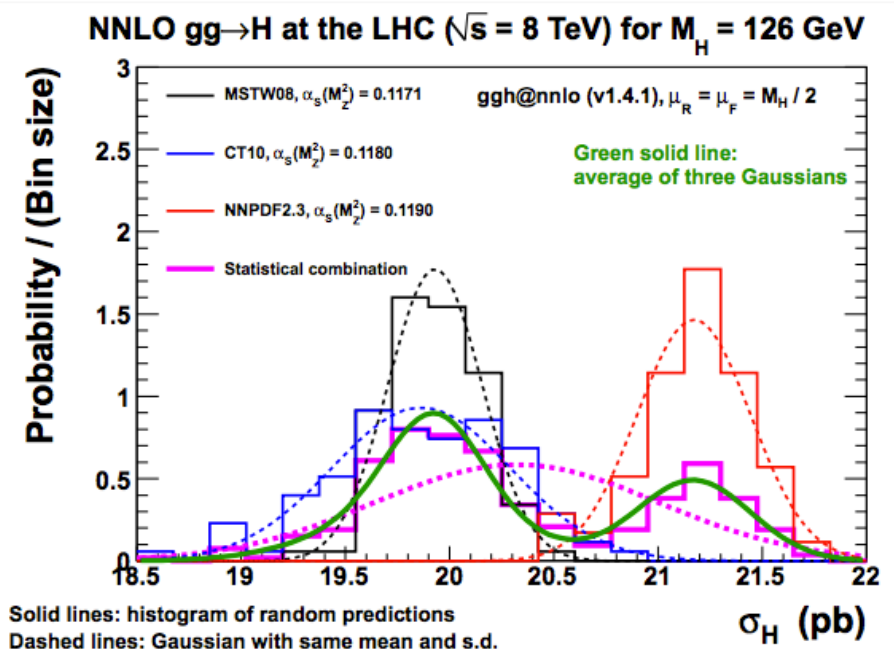
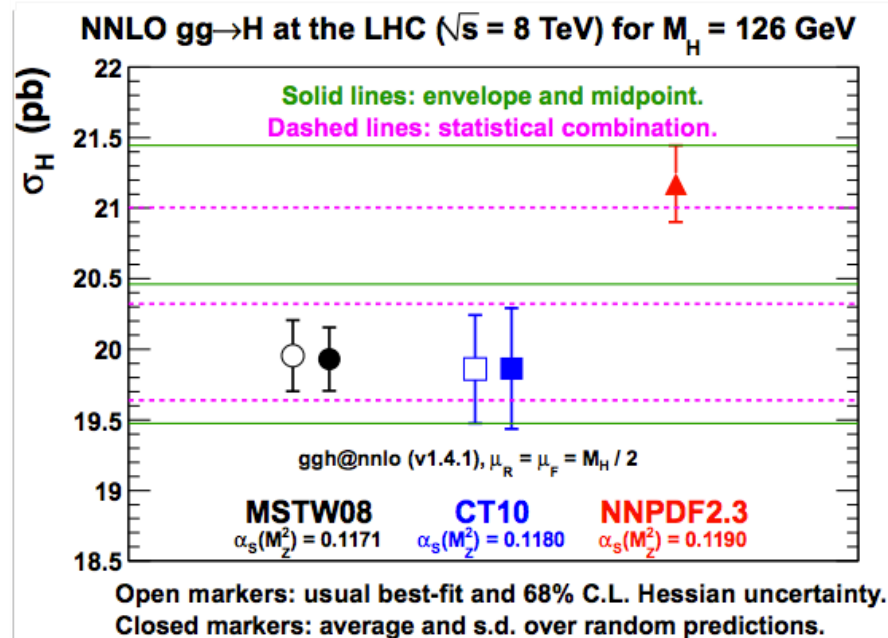
Directly connected with quark-quark luminosity



$$\Phi_{ij}(M_X^2) = \frac{1}{s} \int_{\tau}^1 \frac{dx}{x} f_i(x, M_X^2) f_j\left(\frac{\tau}{x}, M_X^2\right)$$



# How to combine them?



G. Watt, PDF4LHC 2013

- ➡ Envelopes [PDF4LHC prescription arXiv 1101.0538]
- ➡ Statistical combination from different PDF groups generating MC sets. [Forte, Watt, 2013] Smaller uncertainty than envelope: 4.8% vs 3.4% for  $gg \rightarrow H$
- ➡ Meta-PDFs: fit with input functional form the CT, MSTW and NNPDF shapes and combine in a unique consistent set [Gao, Nadolsky, 2014]
- ➡ Crucial to decide optimal value of  $\alpha_s$  and its uncertainty in combination



LHC data for PDFs



# LHC kinematics coverage

GLUON

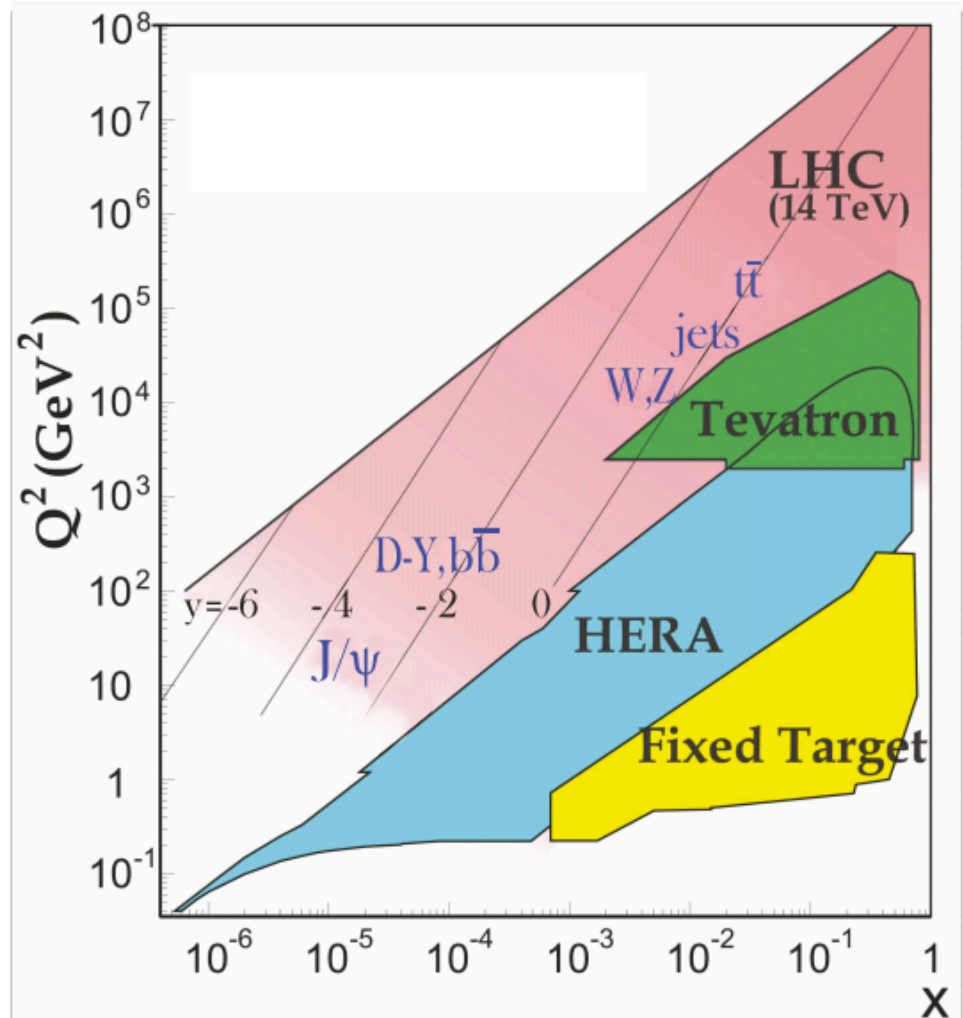
- Inclusive jets and dijets  
(medium/large  $x$ )
- Isolated photon and  $\gamma$ +jets  
(medium/large  $x$ )
- Top pair production (large  $x$ )
- High  $p_T$  Z(+jets) distribution  
(small/medium  $x$ )

QUARKS

- High  $p_T$  W(+jets) ratios  
(medium/large  $x$ )
- W and Z production  
(medium  $x$ )
- Low and high mass Drell-Yan  
(small and large  $x$ )
- Wc (strangeness at medium  $x$ )

PHOTON

- Low and high mass Drell-Yan
- WW production



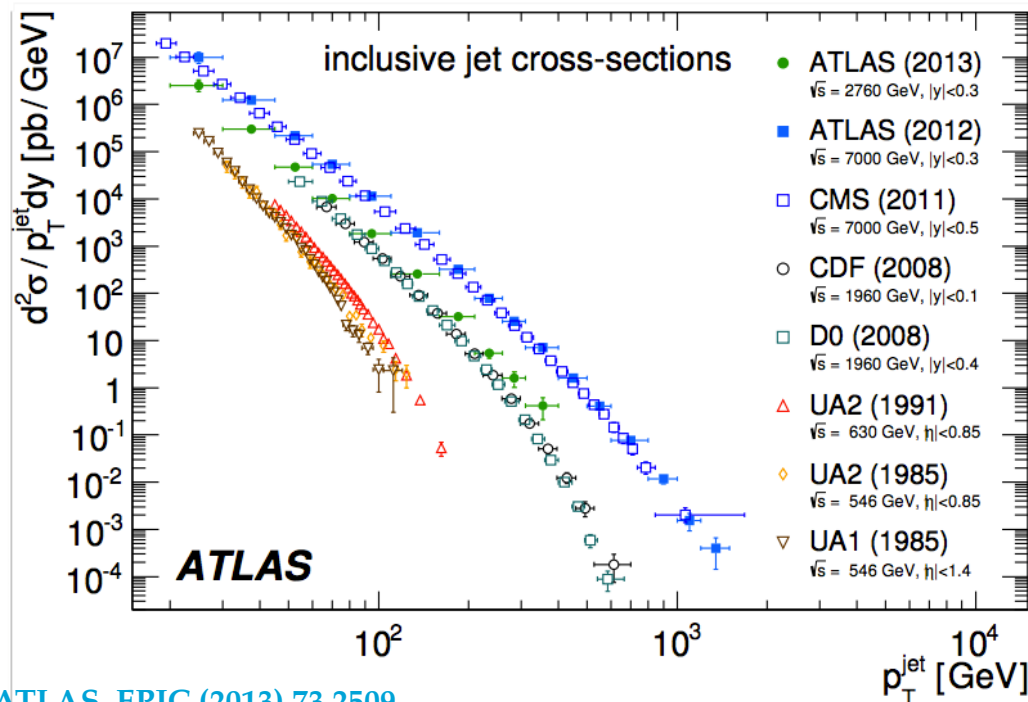


# Gluons

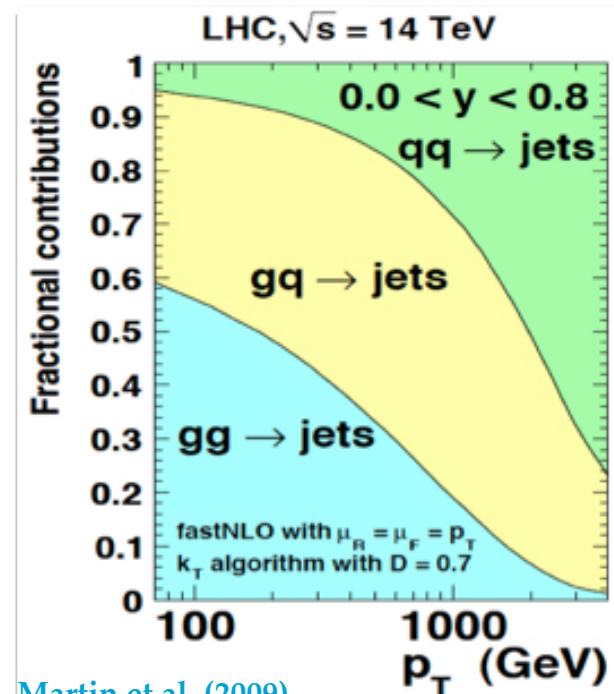
## Inclusive Jets: data

- Jets are traditional source of information on gluon and  $\alpha_s$
- Large- $x$  is the region where gluons and quarks are mostly unconstrained
- Wealth of precise experimental measurements
- Theoretical calculation: NLO and partially NNLO gg initiated contribution has been calculated

[Gehrmann et al]



ATLAS, EPJC (2013) 73 2509



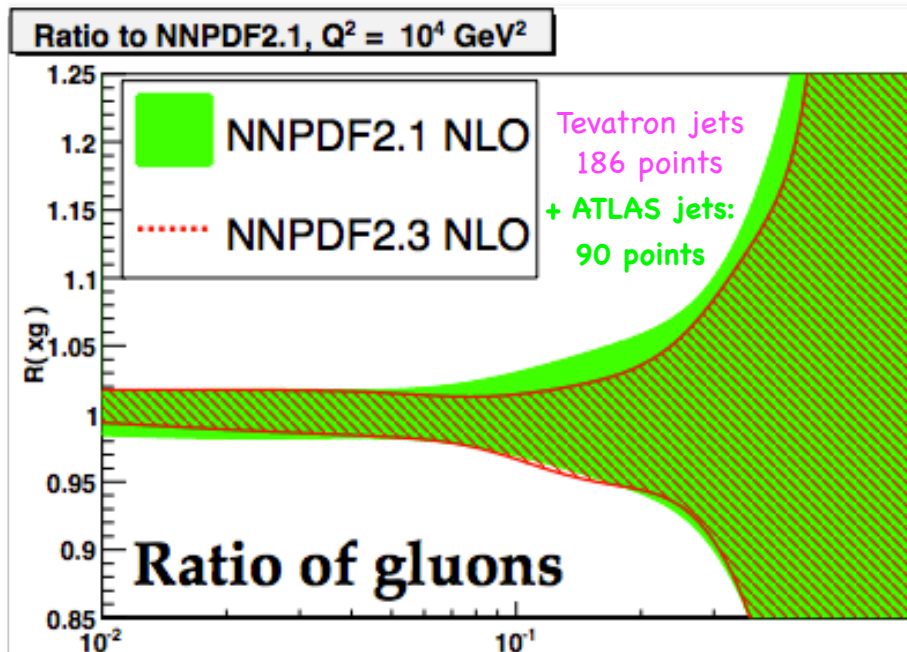
Martin et al, (2009)



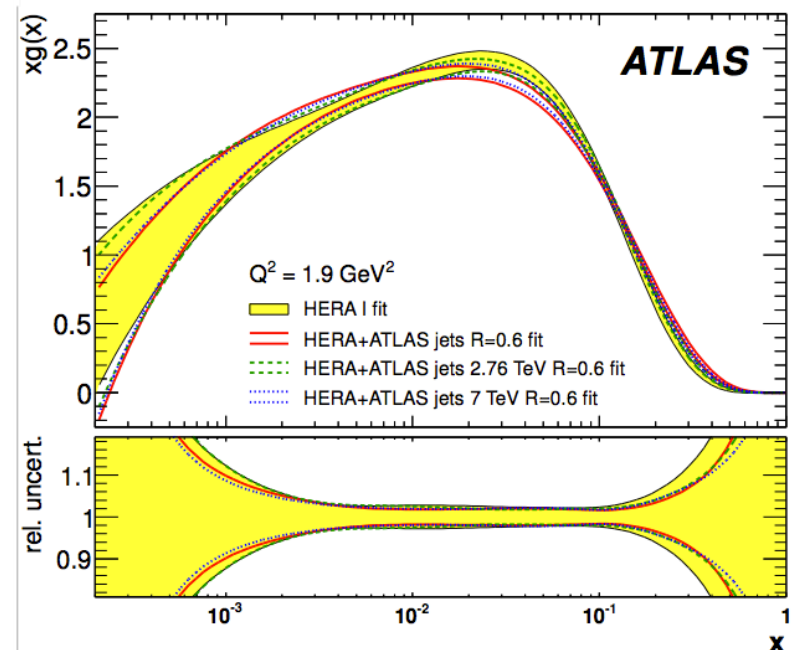
# Gluons

## Inclusive Jets: impact of data

- NNPDF2.3 analysis includes ATLAS 35 pb<sup>-1</sup> inclusive jet data
- Moderate but significant constraint and reduction in gluon uncertainty
- Many more data released: CMS full 7/8 GeV dataset, ATLAS 7/8 TeV and 2.76 TeV data
- Ratio of observable at different CoM energies strongly constraint due to correlations (ATLAS)
- CMS sizeable impact assessed by MSTW via reweighting



R. Ball et al, Nucl. Phys. B867 (2013) 244



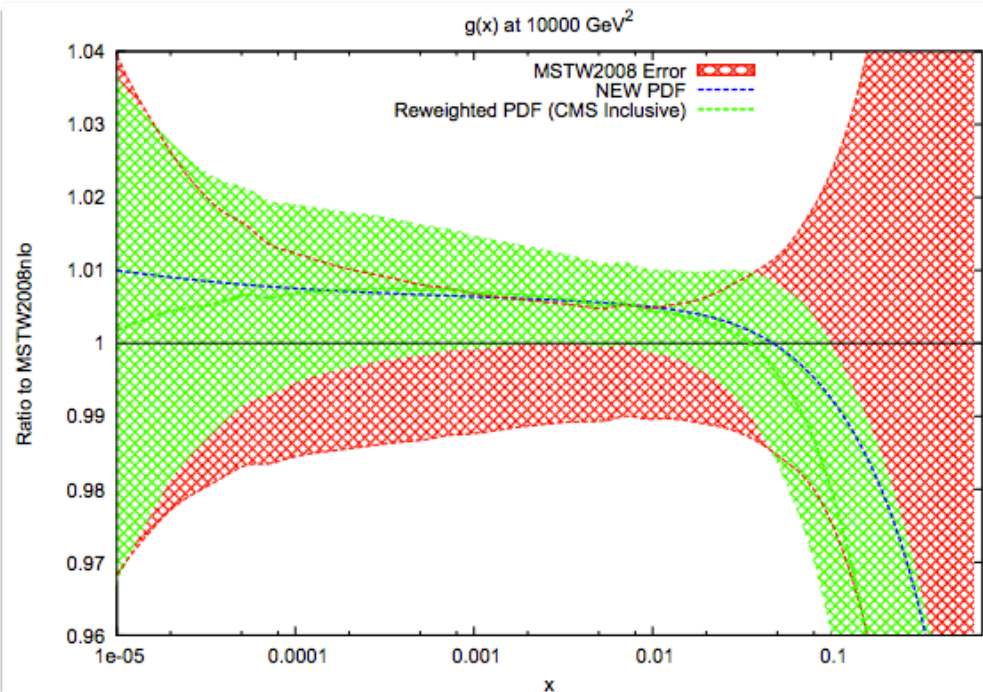
ATLAS, EPJC (2013) 73 2509



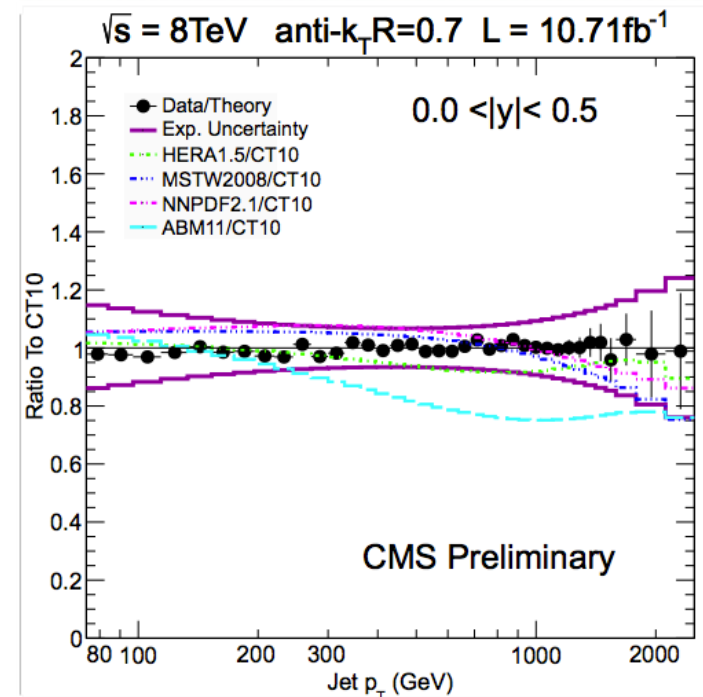
# Gluons

## Inclusive Jets: impact of data

- NNPDF2.3 analysis includes ATLAS 35 pb<sup>-1</sup> inclusive jet data
- Moderate but significant constraint and reduction in gluon uncertainty
- Many more data released: CMS full 7/8 GeV dataset, ATLAS 7/8 TeV and 2.76 TeV data
- Ratio of observable at different CoM energies strongly constraint due to correlations (ATLAS)
- CMS sizeable impact assessed by MSTW via reweighting [Ball et al (2012)]



R. Thorne, QCD@LHC 2013



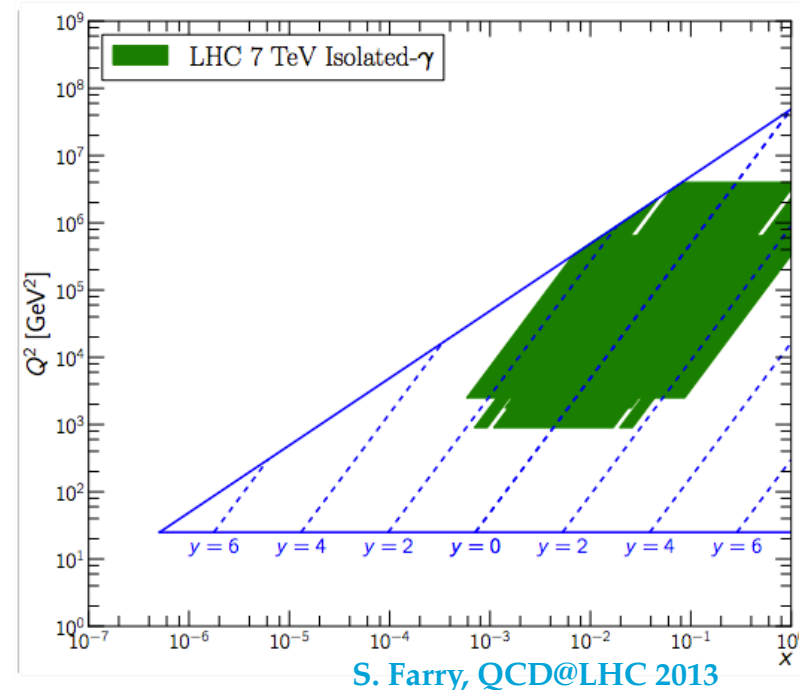
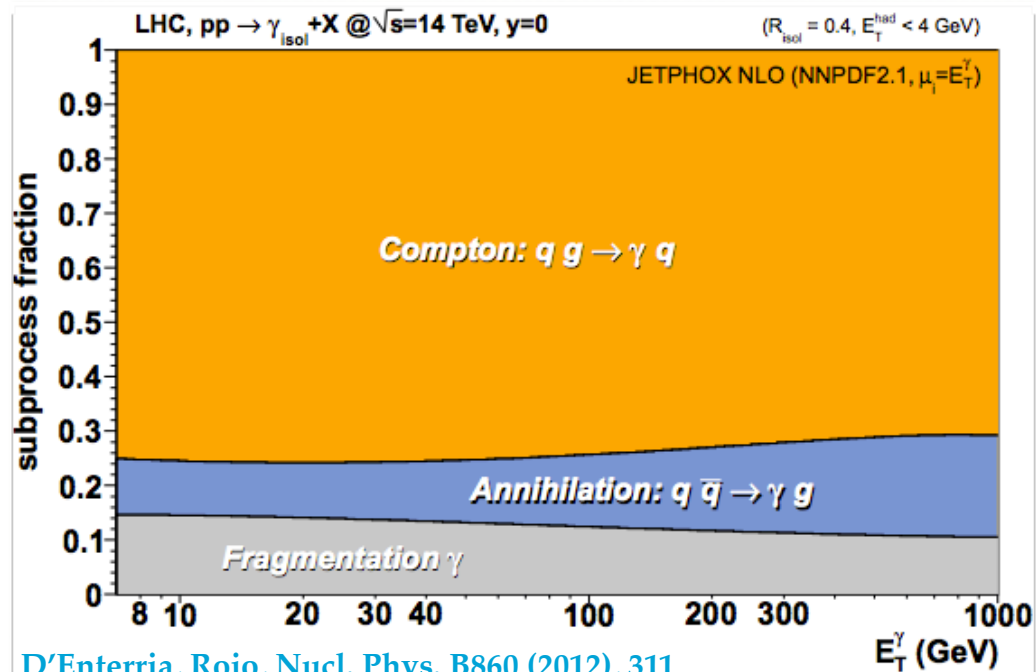
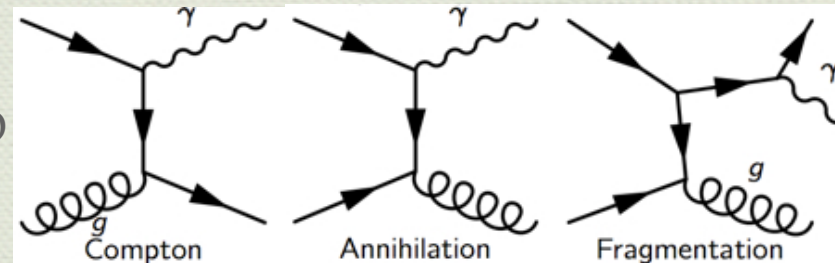
CMS-PAS-SMP-12-012



# Gluons

## Prompt photon production: data

- Prompt photon production directly sensitive to the gluon-quark luminosity via Compton scattering
- Isolated prompt photon data well described by NLO QCD theory
- ATLAS and CMS measurements at 7 TeV constrain medium-x region

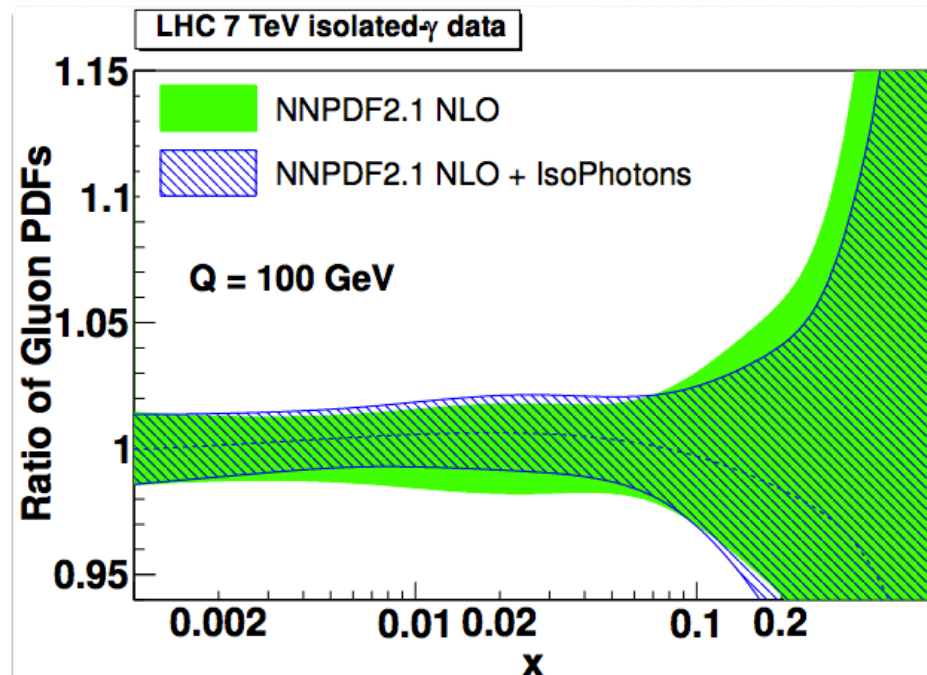
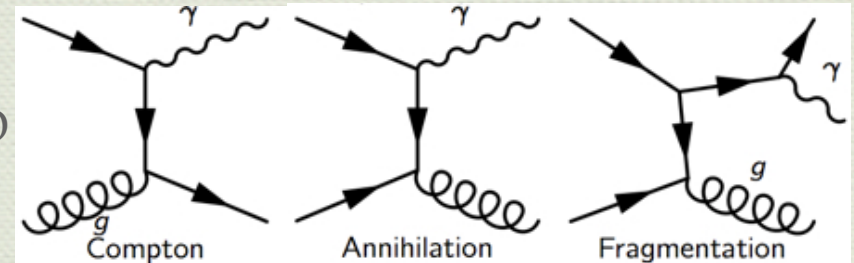




# Gluons

## Prompt photon production: impact of data

- Prompt photon production directly sensitive to the gluon-quark luminosity via Compton scattering
- Isolated prompt photon data well described by NLO QCD theory
- ATLAS and CMS measurements at 7 TeV constrain medium-x region



- Included ATLAS  $880 \text{ nb}^{-1}$ , and  $35 \text{ pb}^{-1}$ , CMS  $1.9^{-1}$  and  $36 \text{ pb}^{-1}$
- Moderate uncertainty reduction in the region which affects and reduce uncertainties for Higgs gluon fusion predictions by 20%
- Issue: there is not yet a public fast interface available for JETPHOX [P. Aurenche et al] in PDF fits but it is likely to be available shortly



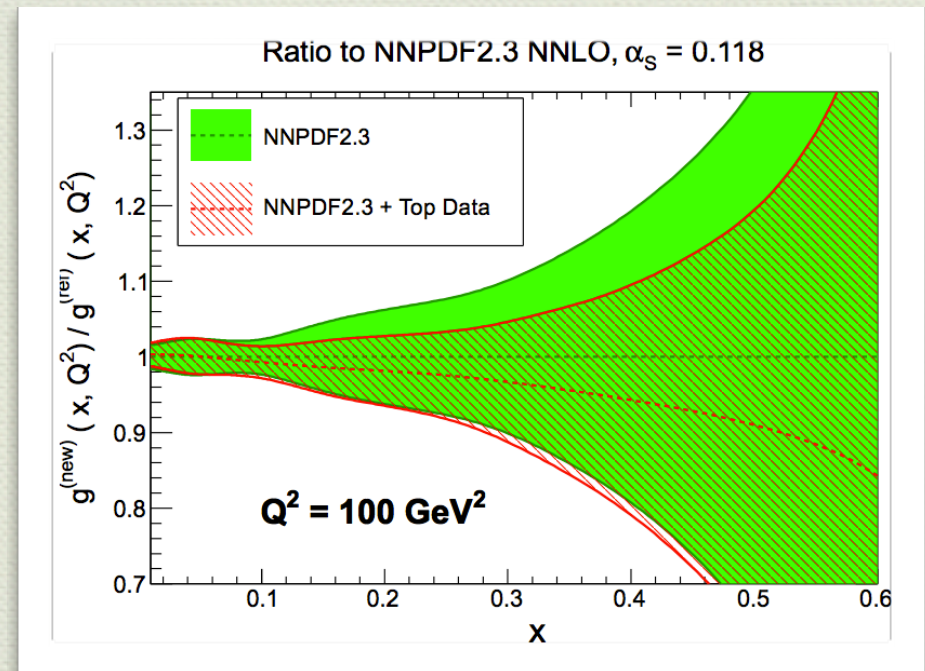
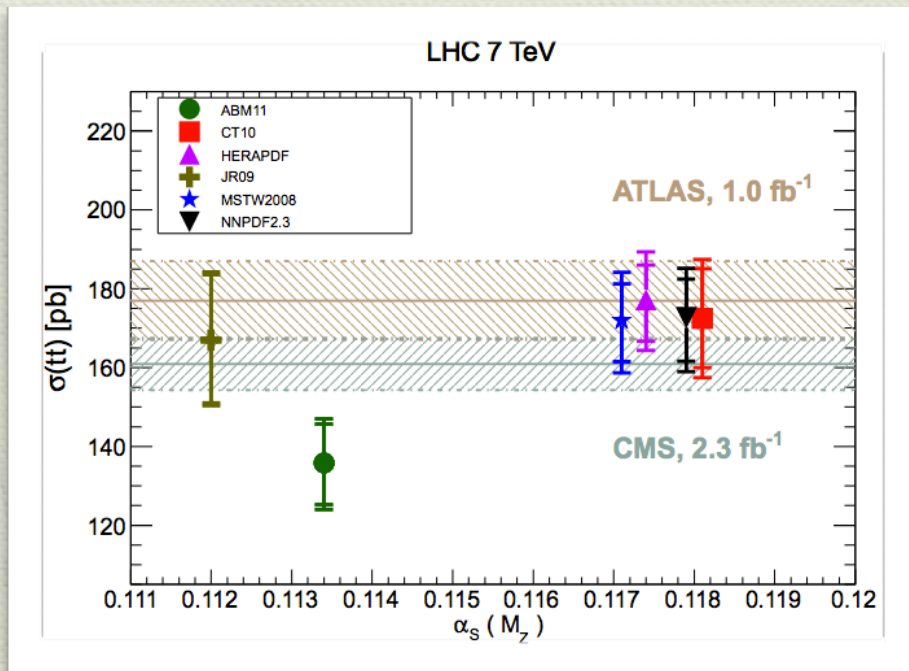
# Gluons

## Top pair production: data and impact

- At LHC, dominant channel is  $gg$  fusion
- Exp: precise measurements of total xsec by ATLAS and CMS + differential distributions
- Theory: full NNLO for total cross sections [Czakon et al] and NLO + NNLL code for differential distributions public soon [Guzzi et al]
- Significant constraints for gluon [Czakon et al, Beneke et al]

	TeVatron	LHC 7 TeV	LHC 8 TeV	LHC 14 TeV
$gg$	15.4%	84.8%	86.2%	90.2%
$qg + \bar{q}g$	-1.7%	-1.6%	-1.1%	0.5%
$qq$	86.3%	16.8%	14.9%	9.3%

Czakon et al, JHEP 1307 (2013) 167

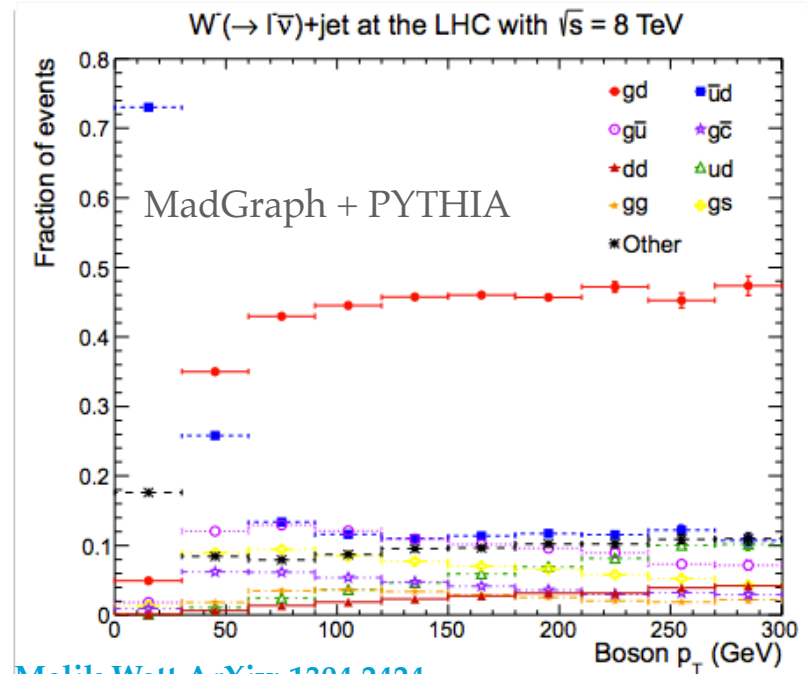
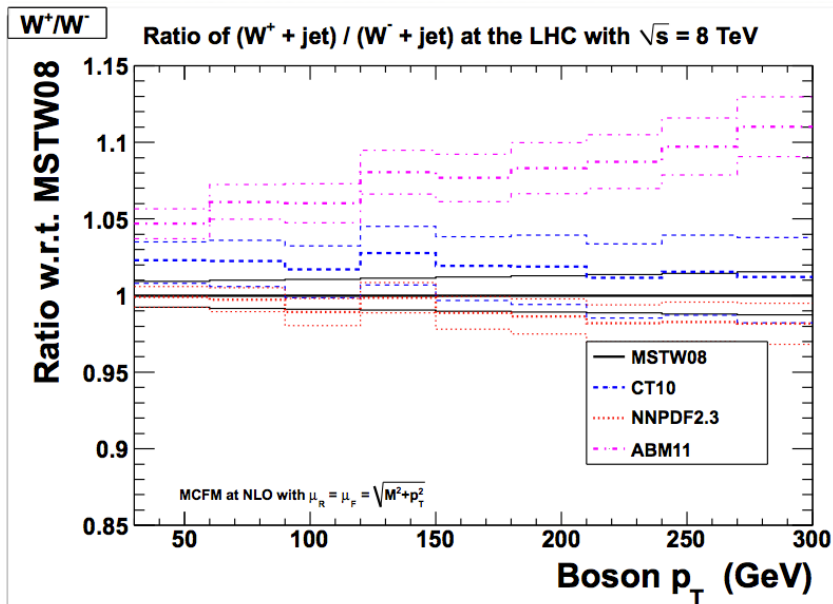




# Gluons

## High $p_T$ vector boson production

- In global fits, medium/large  $x$  gluon is mainly constrained by jet data.
- W/Z boson at large  $p_T$  (associated with jets) would provide a complementary constraint in  $x$  region which enters  $gg \rightarrow H$  production
- At large  $p_T$ , gluon up (for Z and  $W^+$ ) or gluon down (for  $W^-$ ) scattering dominate: can exploit these observables to constrain gluon and u/d ratio



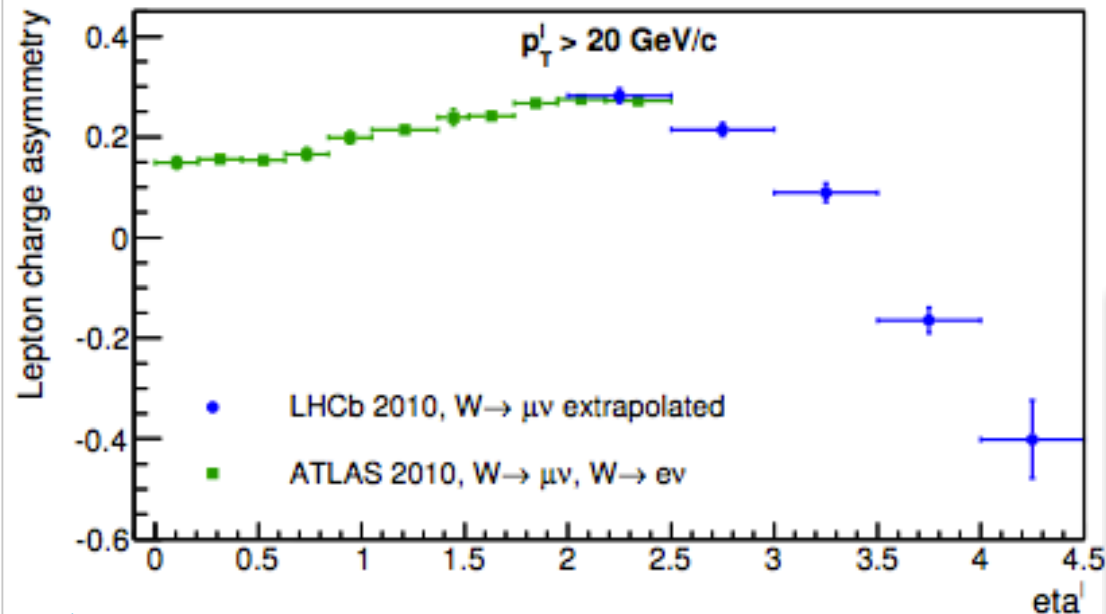
Malik,Watt ArXiv: 1304.2424

- $p_T$  spectra affected by possibly large theoretical uncertainties, soft resummation and EW corrections at small/large  $p_T$ .
- Need NNLO, hopefully not too far after calculation of  $H+j$  at NNLO [Boughezal et al]
- Exploit ratios to cancel theoretical uncertainties



# Quark flavor separation

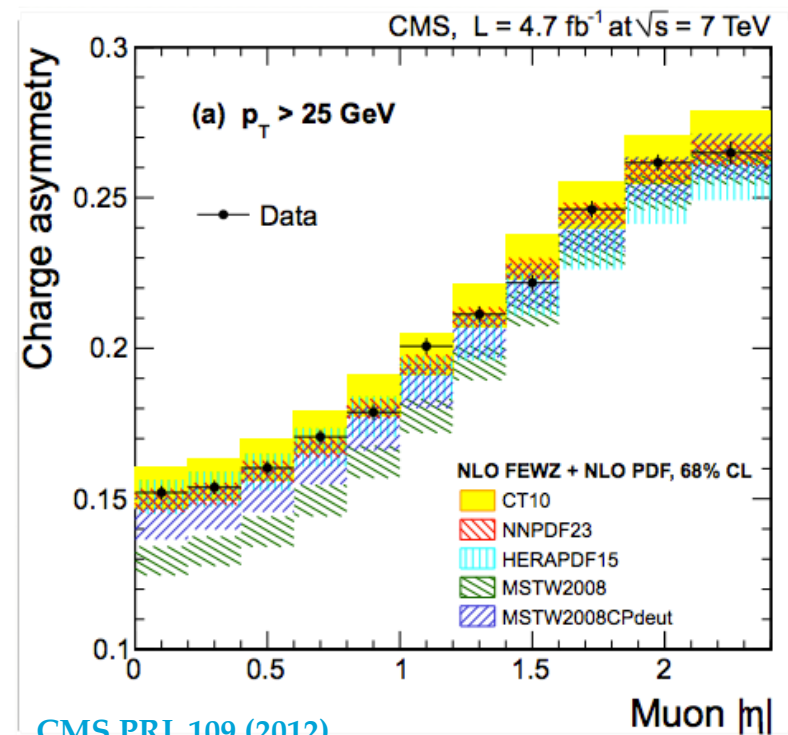
## A wealth of data from LHC



LHCb-CONF-2013-005

✓ W charge lepton asymmetry (ATLAS and CMS) Strong constraints on up and down valence quarks and sea asymmetry

✓ W/Z rapidity distribution, both central (CMS and ATLAS) and forward (LHCb) Constrain quark flavor separation in a wide  $x$  range

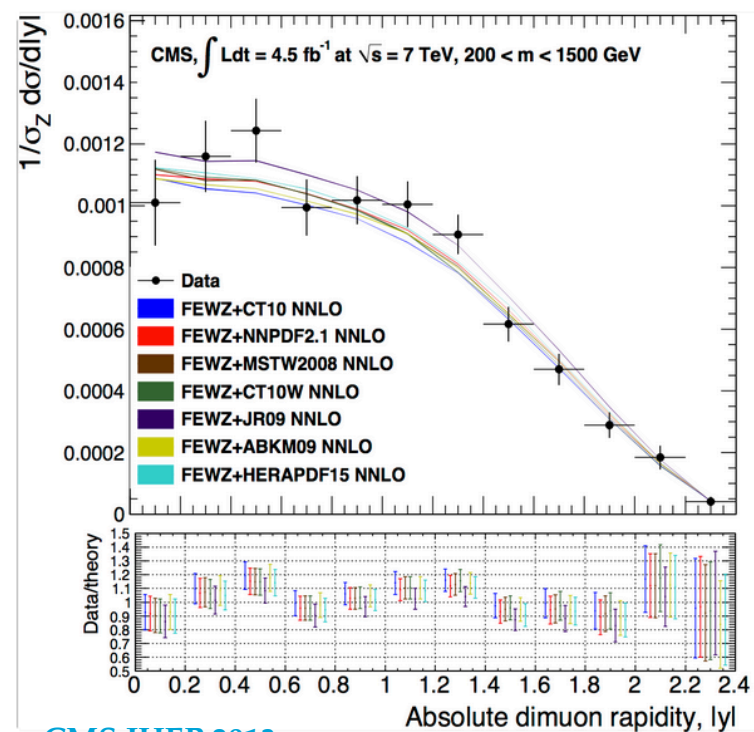


CMS PRL 109 (2012)

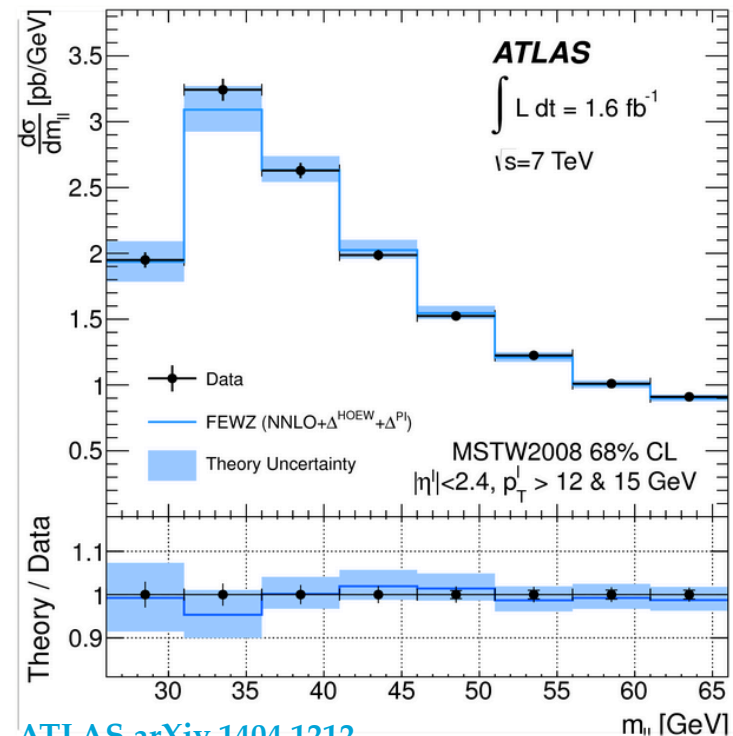


# Quark flavor separation

A wealth of data from LHC



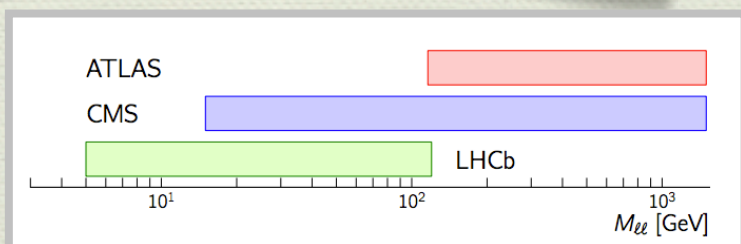
CMS JHEP 2013



ATLAS arXiv 1404.1212

✓ High and low mass Drell-Yan distributions provide valuable constrain to quarks and antiquarks in large and small  $x$  regions

$$x_{1,2}^0 = \frac{M}{\sqrt{s}} e^{\pm Y}$$





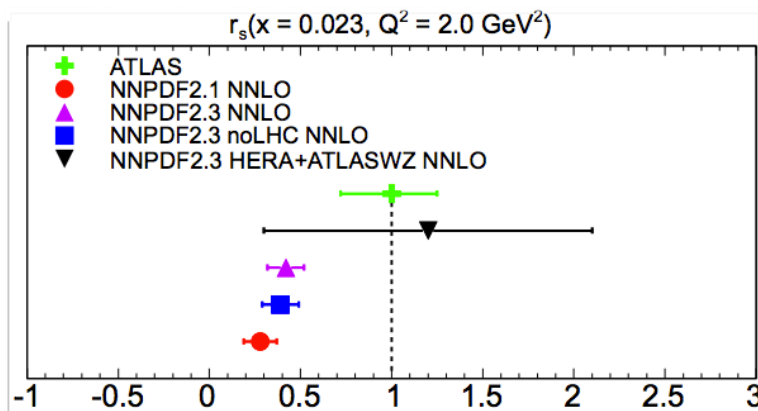
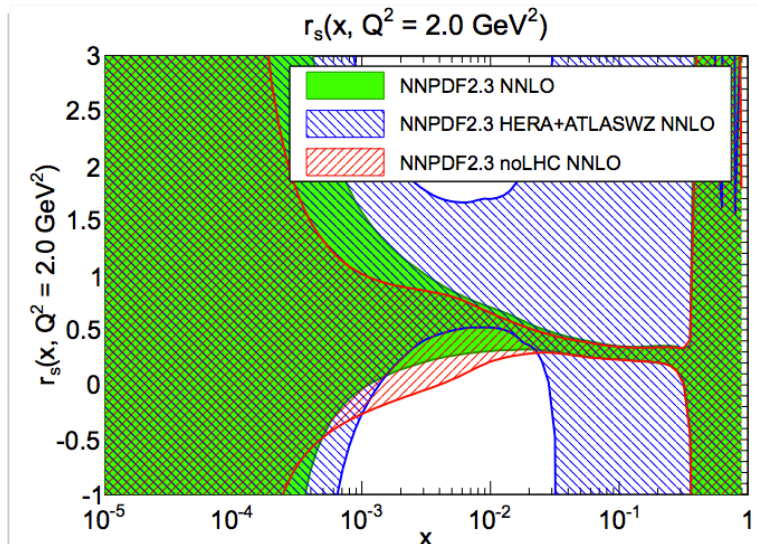
# Strangeness

## A “strange” story

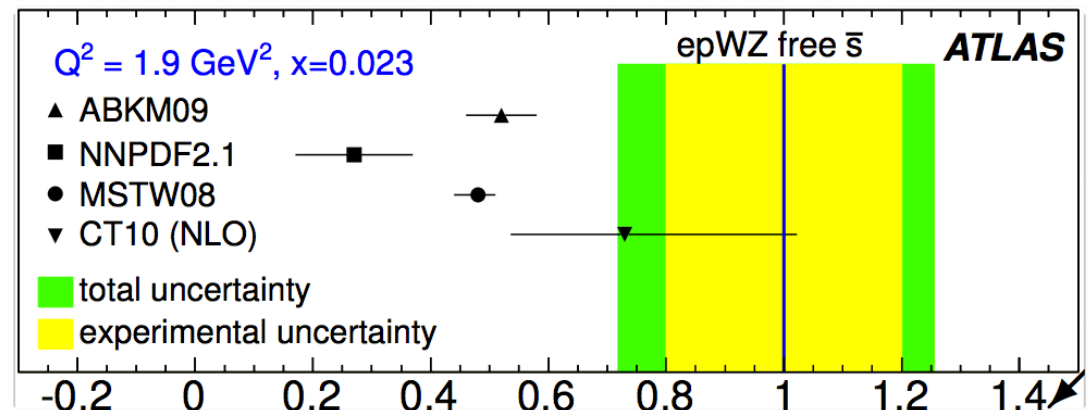
- In global analyses strangeness is mostly determined by DIS fixed target data (CHORUS, NuTeV) -> suppressed strange sea

$$r_s(x, Q^2) = \frac{s(x, Q^2) + \bar{s}(x, Q^2)}{2\bar{d}(x, Q^2)}$$

- ATLAS analysis, based on the HERAFITTER approach, points to a non-suppressed strangeness
- NNPDF2.3 analysis confirms the central value of the ATLAS analysis but finds larger uncertainties.



R. Ball et al, Nucl. Phys. B867 (2013) 244



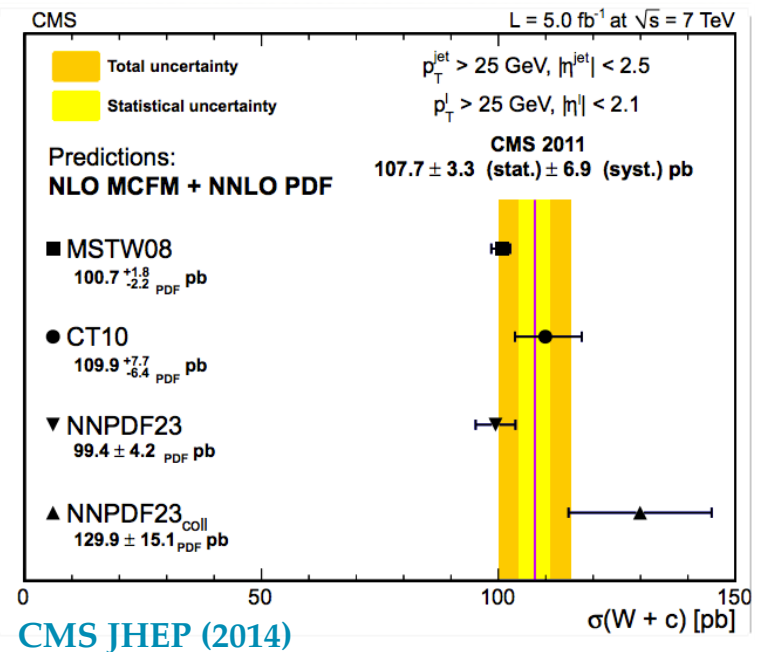
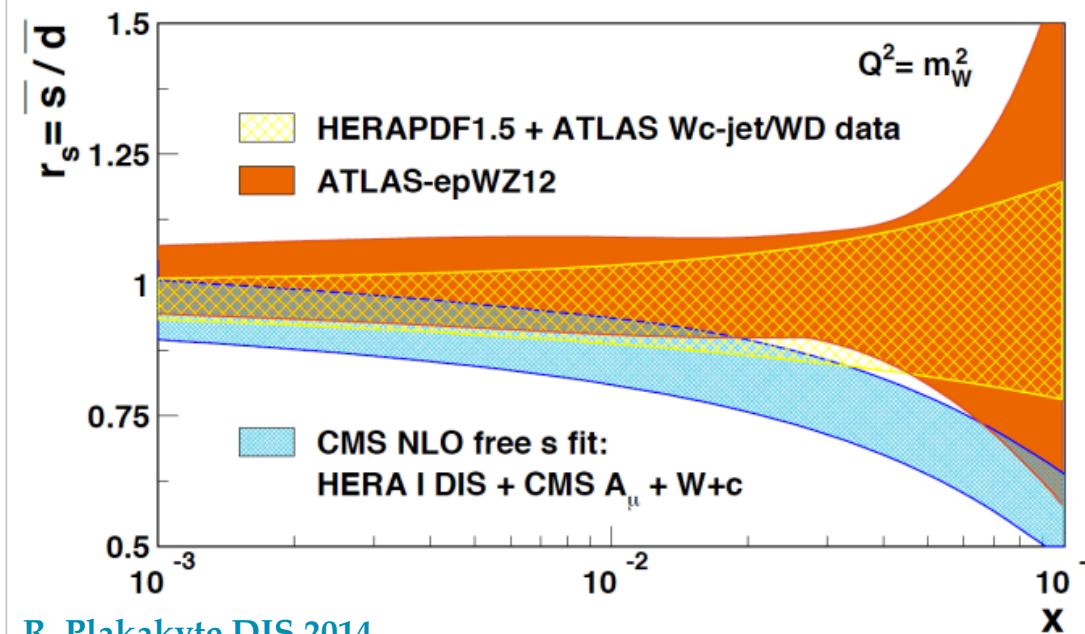
ATLAS, Phys. Rev. Lett. 109 (2012) 012001



# Strangeness

## A “strange” story

- W+charm data from ATLAS and CMS (both inclusive and distributions) provide a cleaner set of data to constrain strangeness from collider data
- ATLAS data consistent with large  $s$ , opposite to CMS data consistent with suppressed  $s$
- Recent from NOMAD: charm dimuon production in neutrino-iron scattering consistent with NuTeV
- Ultimate answer comes from inclusion of W+c data in PDF fits

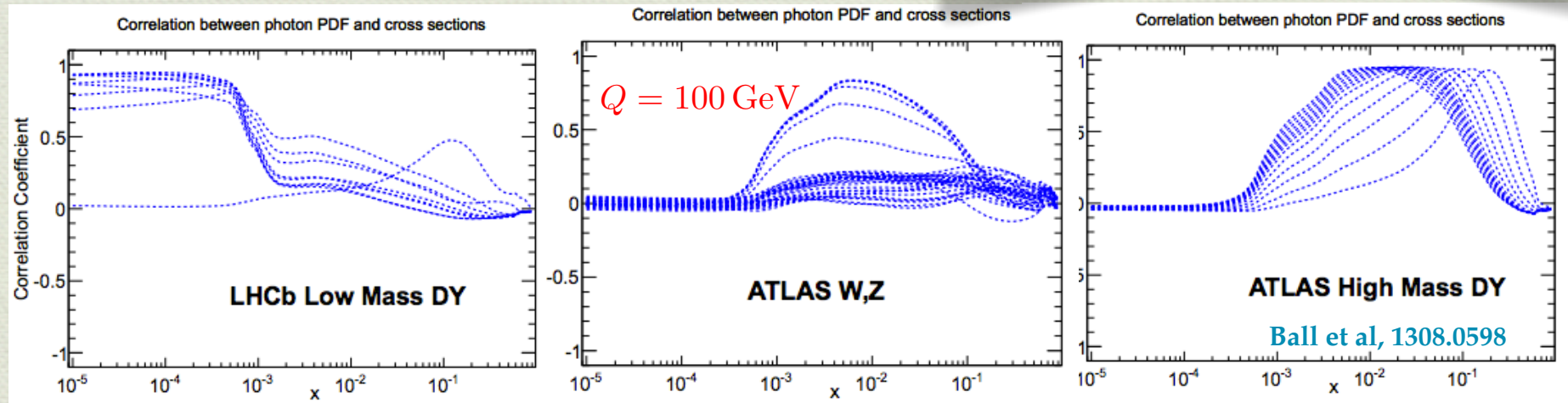
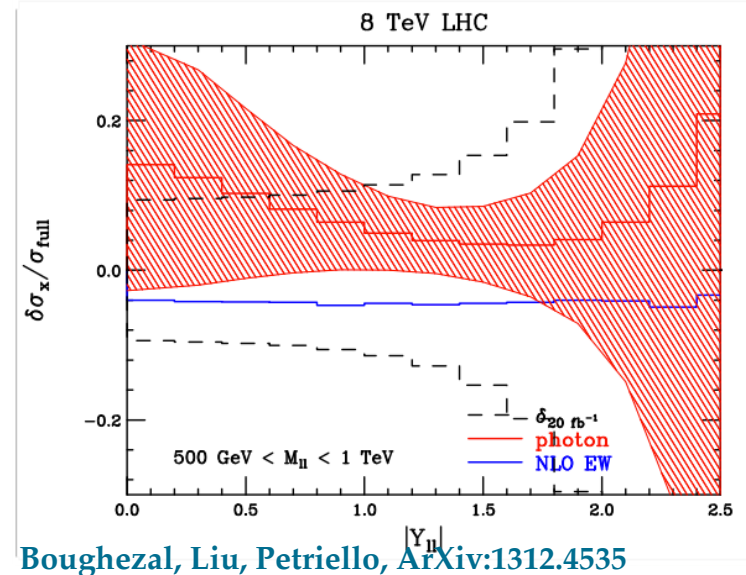




# Photon

## Electroweak corrections

- EW corrections become relevant at the current precision level
- Their inclusion requires PDF with QED effects
- NNPDF23QED is new PDF set with uncertainties which incorporates (N)NLO QCD + LO QED effects
- Photon PDF fitted from DIS and DY data (on-shell W,Z production and low/high mass DY)
- Photon PDF is poorly determined from DIS data. Need hadron collider processes where photon contributes at LO!

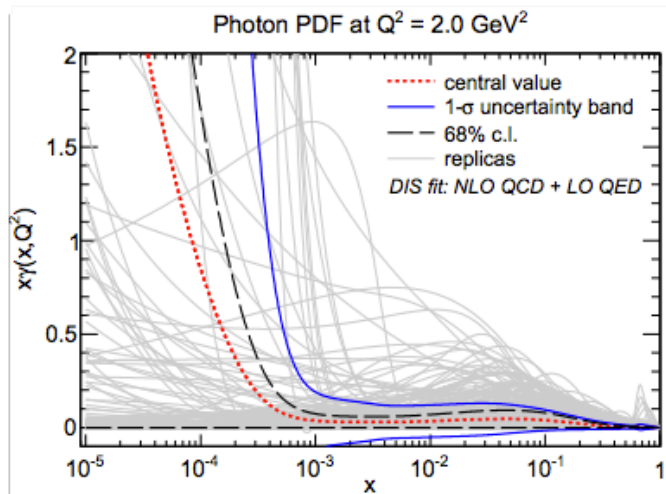




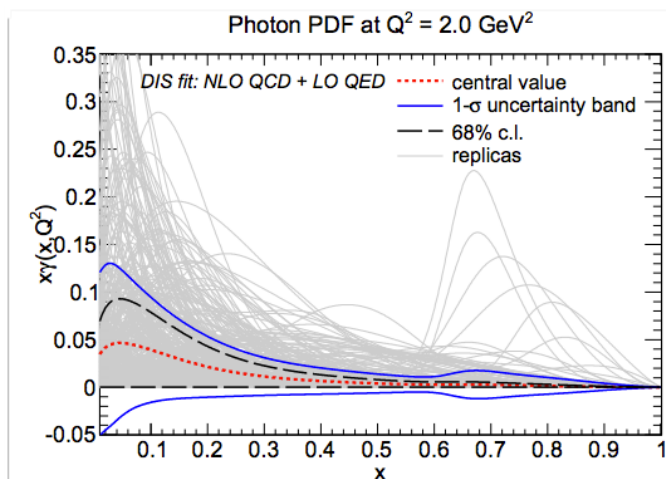
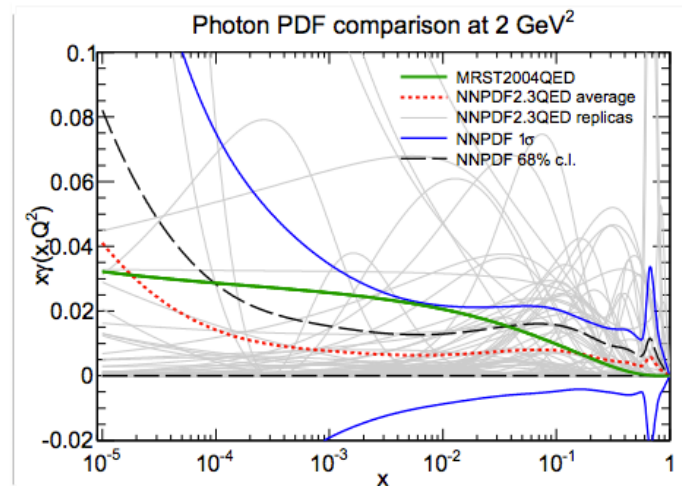
# Photon

## Constraints from LHC

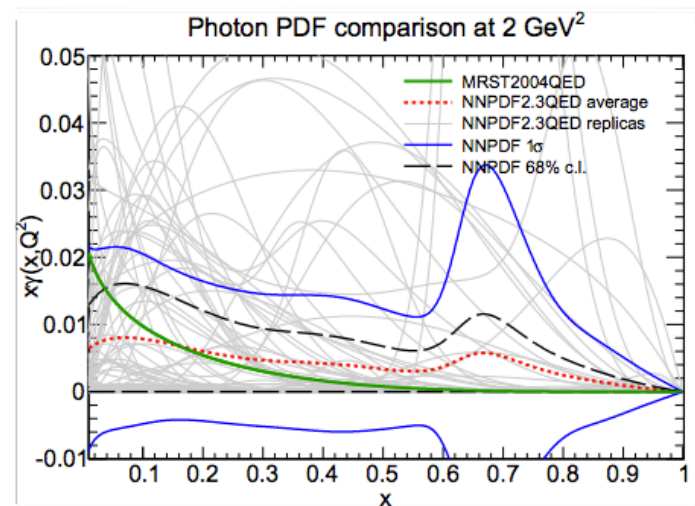
Ball et al, 1308.0598



small  $x$



large  $x$



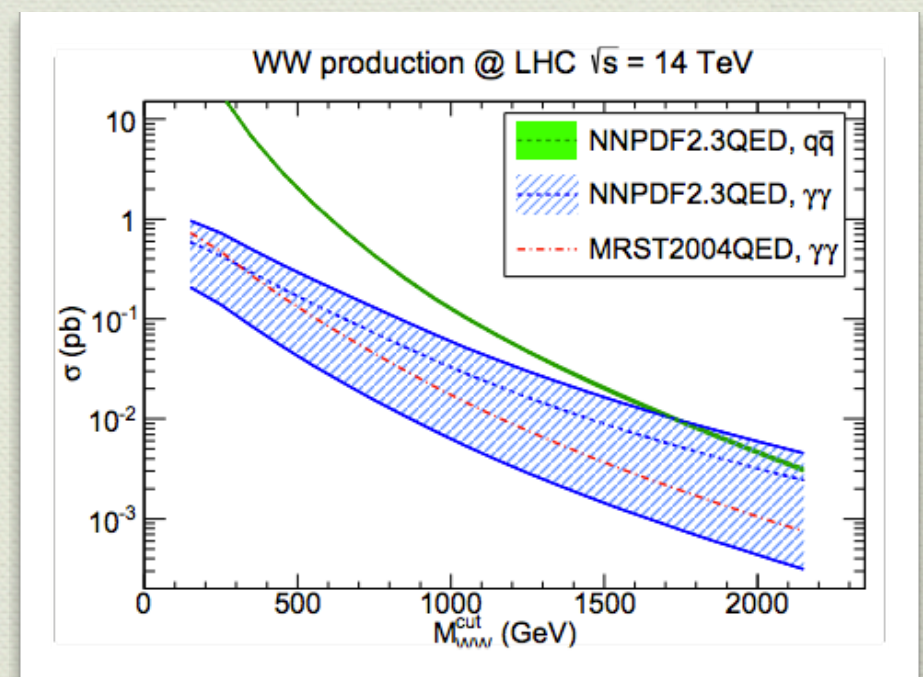
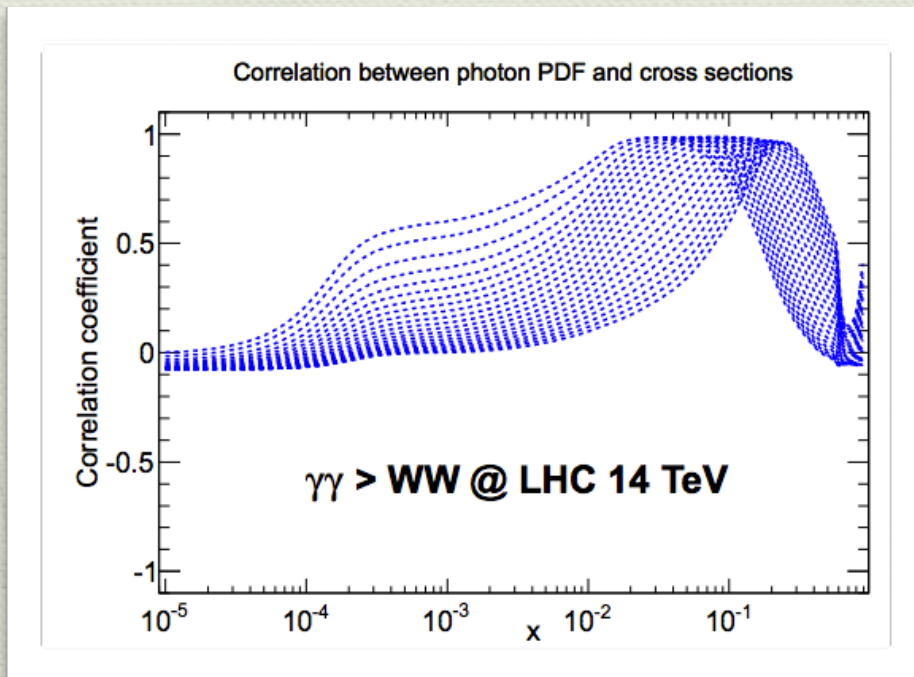
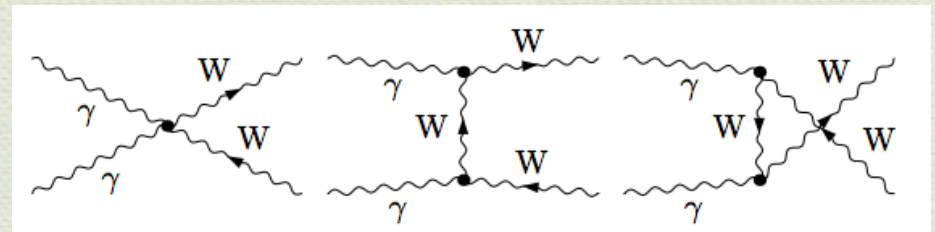


# Photon

## More constraints from LHC

Ball et al, 1308.0598

- WW production is phenomenologically relevant as a background for BSM searches
- At high  $M_{WW}$ , photon-induced contribution become relevant
- The large uncertainty at large  $M_{WW}$  comes from the large uncertainty of photon PDF for  $x > 0.1$
- New LHC data give unique opportunity of constraining the photon in that region





# Conclusions and outlook

- ◆ PDF uncertainties are often limiting factor in achieving precise predictions
- ◆ LHC data have huge potential in constraining PDFs
  - ✓ Inclusive jets and dijets both central and forward: large- $x$  quarks and gluons
  - ✓ Inclusive W and Z productions and asymmetries: quark-flavor separation, strangeness, photon
  - ✓ Isolated photon: medium- $x$  gluon
  - ✓ High- $p_T$  Z/W transverse momentum distribution
  - ✓ W+charm: direct handle on strangeness
  - ✓ W,Z + jets: gluon at medium- $x$  and u/d ratio
  - ✓ Off-resonance Drell-Yan at small and large mass: quarks & photon at small and large  $x$
  - ✓ WW production: photon and light quarks
  - ✓ Top quark inclusive and differential distribution: large- $x$  gluon
  - ✓ Ratios at different CME
  - ✓ Z+c: intrinsic charm PDF
  - ✓ Z+b: gluon and bottom PDF
  - ✓ Single top production: gluon and bottom PDFs
- ◆ Most collaborations working in inclusion of LHC data (NNPDF3.0)
- ◆ Towards collider only fits?
- ◆ Theoretical accuracy must catch up with experimental accuracy