Parton Distributions today: needs, achievements and challenges

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Foreword: parton distributions on the light cone

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$$f(x) \equiv f^{\uparrow}(x) + f^{\downarrow}(x) \qquad \Delta f(x) \equiv f^{\uparrow}(x) - f^{\downarrow}(x)$$

$$q(x) = \textcircled{g(x)} + \textcircled{g(x)} = \textcircled{g(x)} + \textcircled{g(x)} \qquad \Delta q(x) = \textcircled{g(x)} - \textcircled{g(x)} \rightarrow - (\textcircled{g(x)} \rightarrow - ())))))$$

2 Allow for a proper field-theoretic definition as matrix elements of bilocal operators



collinear transition of a massles proton hinto a massless parton iwith fractional momentum xlocal OPE \Longrightarrow lattice formulation

$$\begin{split} q(x) &= \frac{1}{4\pi} \int dy^{-} e^{-iy^{-}xP^{+}} \langle P | \bar{\psi}(0, y^{-}, \mathbf{0}_{\perp}) \gamma^{+} \psi(0) | P \rangle \\ \Delta q(x) &= \frac{1}{4\pi} \int dy^{-} e^{-iy^{-}xP^{+}} \langle P, S | \bar{\psi}(0, y^{-}, \mathbf{0}_{\perp}) \gamma^{+} \gamma^{5} \psi(0) | P, S \rangle \end{split}$$

with light-cone coordinates

 $y = (y^+, y^-, \mathbf{y}_\perp)$, $y^+ = (y^0 + y^z)/\sqrt{2}$, $y^- = (y^0 - y^z)/\sqrt{2}$, $\mathbf{y}_\perp = (v^x, v^y)$

Ill these definitions have ultraviolet divergences which must be renormalized

Theoretical framework



Perturbative expansion of coefficient functions

$$C_{Ii}(y, \alpha_s) = \sum_{k=0} a_s^k C_{Ii}^{(k)}(y), \qquad a_s = \alpha_s / (4\pi)$$

Perturbative (DGLAP) evolution of PDFs

$$\frac{\partial}{\partial \ln \mu^2} f_i(x,\mu^2) = \sum_{j}^{n_f} \int_x^1 \frac{dz}{z} P_{ji}\left(z,\alpha_s(\mu^2)\right) f_j\left(\frac{x}{z},\mu^2\right) \quad P_{ji}(z,\alpha_s) = \sum_{k=0} a_s^{k+1} P_{ji}^{(k)}(z)$$

Unpolarised PDFs: NNPDF3.1 [EPJ C77 (2017) 663]

- Higgs boson characterisation PDF uncertainty often dominant
- Determination of SM parameters PDF uncertainty largest theoretical uncertainty in M_W determination
- Searches for BSM the larger the mass of the final state, the larger the PDF uncertainty

	$rac{N_{ m dat}}{(m NNLO/NLO)}$	$_{\rm (NNLO)}^{\chi^2/N_{\rm dat}}$	$_{\rm (NLO)}^{\chi^2/N_{\rm dat}}$
FT DIS	1881/1881	1.15	1.20
HERA DIS	1211/1221	1.11	1.14
FT DY	189/189	1.25	0.96
Tevatron	150/156	1.08	1.06
ATLAS	360/358	1.09	1.37
CMS	409/397	1.06	1.20
LHCb	85/93	1.47	1.61
Total	4285/4295	1.148	1.168



 $\mathcal{O}(4000)$ data points after cuts $Q^2_{\rm cut}$ few ${\rm GeV}^2~W^2_{\rm cut}=3-12.5~{\rm GeV}^2$

Gluon and quark flavour separation



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The strange PDF: neutrino DIS vs collider data



In most PDF fits the strange PDF is suppressed w.r.t up and down sea quark PDFs effect mostly driven by neutrino dimuon data

A symmetric strange sea PDF is preferred by collider data in particular by ATLAS W, Z rapidity distributions (2011) [EPJC77 (2017) 367]

 $R_s(x,Q^2) = \frac{s(x,Q^2) + \bar{s}(x,Q^2)}{\bar{u}(x,Q^2) + \bar{d}(x,Q^2)} \left\{ \begin{array}{l} \sim 0.5 \text{ from neutrino and CMS } W + c \text{ data} \\ \sim 1.0 \text{ from ATLAS } W, Z \end{array} \right.$

The ATLAS data can be accommodated in the global fit increased strangeness, though not as much as in a collider-only fit; slight tension remains nuclear uncertainties in FT DIS? No [EPJC79(2019)282] massive CC coefficient functions at NNLO? Possibly [JHEP1802(2018)026] Suppressed strangeness confirmed by recent W + c CMS analysis [CMS PAS SMP-17-014]

Suppressed strangeness confirmed by recent W + c CWIS analysis (CMS PAS SMP-17-0.

The charm PDF: perturbative vs fitted [EPJ C76 (2016) 647]



Parametrise the $c^+(x,Q_0^2)$, quark and gluon PDFs on the same footing stabilise the dependence of LHC processes upon variations of m_c quantify the nonperturbative charm component in the proton (BHPS? sea-like?) take into account massive charm-initiated contribution to the DIS structure functions Fitted charm found to differ from perturbative charm at scales $Q \sim m_c$ in NNPDF3.1 preference for a BHPS-like shape shape driven by LHCb W, Z data + EMC data

At $Q=1.65~{\rm GeV}$ charm carry 0.26 ± 0.42 % of the proton momentum but it is affected by large uncertainties, especially if no EMC data are included

Standard candles and luminosities



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Theoretical uncertainties in PDF fits [arXiv:1801.04842]

Experimental uncertainties propagated to PDFs via minimisation of figure of merit

$$\chi^{2} = \sum_{i,j}^{N_{\text{dat}}} (D_{i} - T_{i}) (\text{cov}_{\text{exp}})_{ij}^{-1} (D_{j} - T_{j})$$

Assuming that theory uncertainties are (a) Gaussian and (b) independent from experimental uncertainties, modify this to account for (a wide range of) theory errors

$$\chi^{2} = \sum_{i,j}^{N_{\text{dat}}} (D_{i} - T_{i}) (\text{cov}_{\text{exp}} + \text{cov}_{\text{th}})_{ij}^{-1} (D_{j} - T_{j})$$

Problem reduced to estimate the th. cov. matrix, e.g. in terms of nuisance parameters

$$(\operatorname{cov}_{\operatorname{th}})_{ij} = \frac{1}{N} \sum_{k}^{N} \Delta_i^{(k)} \Delta_j^{(k)} \qquad \Delta_i \equiv T_i^{(k)} - T_i$$

Example 1: nuclear uncertainties in PDF fits [EPJ C79 (2019) 282]

Experimental correlation matrix



nuclear uncertainties determined by averaging over Monte Carlo replicas from three nuclear PDF sets: DSSZ12, nCTEQ15 and EPPS16



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Example 2: MHO uncertainties in PDF fits [arXiv:1906.10698]

 μ_F variations are correlated across all processes (PDF evolution) μ_R variations are correlated by process (hard cross section) vary scales in $\frac{1}{2} \leq \frac{\mu_F}{\mu_{F,0}}, \frac{\mu_R}{\mu_{R,0}} \leq 2$; consider 3-, 7- or 9-point variations average over flat distribution of points; consider different correlation treatments validate the NLO theory covariance matrix over the NLO-NNLO shift



Experimental + Theory Correlation Matrix (3 pt)

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Example 2: MHO uncertainties in PDF fits [arXiv:1906.10698]



PDF uncertainty increase encapsulates NLO-NNLO shift

Overall (rather small) increase in uncertainties

Increase in PDF uncertainties due to replica generation is counteracted by extra correlations in fitting minimisation

Tensions relieved: improvement in χ^2 exp only: $\chi^2/N_{\rm dat} = 1.139$ exp+th: $\chi^2/N_{\rm dat} = 1.110$

Data whose theoretical descrition is affected by large scale uncertainties are deweighted in favour of more perturbatively stable data

Polarised PDFs: NNPDFpol1.x [Nucl.Phys. B887 (2014) 276]



	FYDEDIMENT	N	$\chi^2/N_{\rm dat}$		
	EAFERIMENT	1'dat	1.0	1.1	1.2
	EMC	10	0.44	0.43	0.43
	SMC	24	0.93	0.90	0.92
	SMClowx	16	0.97	0.97	0.94
	E142	8	0.67	0.66	0.55
	E143	50	0.64	0.67	0.63
	E154	11	0.40	0.45	0.34
	E155	40	0.89	0.85	0.98
	COMPASS-D	15	0.65	0.70	0.57
	COMPASS-P	15	1.31	1.38	0.93
	HERMES97	8	0.34	0.34	0.23
	HERMES	56	0.79	0.82	0.69
new	COMPASS-P-15	51	0.98*	0.99*	0.65
new	COMPASS-D-17	15	1.32*	1.32*	0.80
new	JLAB-E93-009	148	1.26*	1.23*	0.94
new	JLAB-EG1-DVCS	18	0.45*	0.59*	0.29
new	JLAB-E06-014	2	2.81*	3.20*	1.33
	COMPASS (OC)	45	1.22*	1.22	1.22
	STAR (jets)	41	_	1.05	1.06
	PHENIX (jets)	6	—	0.24	0.24
	STAR- $A_L^{W^{\pm}}$ (2012)	24	_	1.05	1.05
	STAR- $A_{LL}^{W^{\pm}}$	12	_	0.95	0.94
new	STAR- $A_{L}^{W^{\pm}}$ (2013)	8	_	2.76*	1.34
new	STAR (dijets)	14	—	1.34*	1.00
	TOTAL		0.77	1.05	1.01

* data set not included in the corresponding fit

Total up and down polarisations [JPCS 678 (2016) 012030]



- Improved accuracy at small x: new COMPASS data (+ improved unpolarized F_L and F₂ from NNPDF3.1)
- Improved accuracy at large x: new JLAB data (also note that the positivity bound is slightly different)
- A lower cut on W^2 will allow for exploiting the full potential of JLAB data (if we replace $W^2 \ge 6.25 \text{ GeV}^2$ with $W^2 \ge 4.00 \text{ GeV}^2$ the χ^2 deteriorates significantly) (need to include and fit dynamic higher twists, in progress)

Gluon polarisation



High-p_T di-jets [PRD 95 (2017) 071103] confirm a positive gluon polarization in the proton



Sea guark polarisation $\Delta_s = \Delta \bar{u} - \Delta d_{\text{[arXiv:1702.05077]}}$



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 $\rightarrow +0.07 \pm 0.01$

х

SU(3) breaking and strangeness



All PDF determinations based only on DIS data (+ SU(3)) find a negative Δs^+ PDF determinations based on DIS+SIDS data (+SU(3)) find a negative or a positive Δs^+ depending on the K FF set [PRD 91 (2015) 054017]

Tension between DIS and SIDIS data can be ficticious

SU(3) may be broken [PRD 58 (1998) 094028, Ann.Rev.Nucl.Part.Sci.53 (2003) 39], but how much? \rightarrow in NNPDFpol, the nominal uncertainty on a_8 in inflated by 30% of its value to allow for a SU(3) symmetry violation ($a_8 = 0.585 \pm 0.025 \rightarrow a_8 = 0.585 \pm 0.176$) \rightarrow but e.g. lattice finds a larger SU(3) symmetry violation [PRL 108 (2012) 222001]

Opportunities at an EIC

one could study kaon multiplicities in SIDIS \longrightarrow further constraint on kaon FFs one could study CC charm production $W^+s \to c$ in DIS \longrightarrow direct handle on s, \bar{s}

Global fits: SIDIS and Fragmentation Functions

	DHESS	JAM	NNFF
SIA	Ø	Ø	Ø
SIDIS	\checkmark	\checkmark	\boxtimes
PP	К	\boxtimes	🗹 (h [±])
statistical treatment	Iterative Hessian 68% - 90%	Monte Carlo	Monte Carlo
parametrisation	standard	standard	neural network
pert. order	(N)NLO	NLO	up to NNLO
HF scheme	ZM(GM)-VFN	ZM-VFN	ZM-VFN

 $\begin{array}{lll} \mbox{DEHSS} & \pi^{\pm} \ \mbox{[PRD 91 (2015) 014035]} \ K^{\pm} \ \mbox{[PRD 95 (2017) 094019]} & \begin{tabular}{ll} 0 \\ 1.4 \\ \mbox{JAM} & \pi^{\pm}, \ K^{\pm} \ \mbox{[PRD 94 (2016) 114004]} & \end{tabular} \\ \mbox{NNFF} & \pi^{\pm}, \ K^{\pm}, \ p/\bar{p} \ \mbox{[EPJ C77 (2017) 516]} & \end{tabular} \end{array}$

Focus on new data: BELLE and BABAR SIA cross sections COMPASS SIDIS multiplicities Overall fair agreement among the three sets (except flavour separation for K^{\pm}) NNFF uncertainties usually larger (especially for the gluon) Note various shapes for the π^{\pm} gluon



Global fits: SIDIS and Fragmentation Functions

	DHESS	JAM	NNFF
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SIDIS	\checkmark	\checkmark	\boxtimes
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Simultaneous fits of (pol.) PDFs and FFs [PRL 119 (2017) 132001]





 $= 0.36 \pm 0.09 \qquad \Delta u - \Delta d = 0.05 \pm 0.08$

Comparing lattice QCD and global fit PDF moments



Which precision shall we require to lattice QCD?

Generate lattice QCD pseudodata assuming NNPDFpol1.1 central values for

 $g_A\equiv\langle 1\rangle_{\Delta u^+-\Delta d^+}\text{, }\langle 1\rangle_{\Delta u^+}\text{, }\langle 1\rangle_{\Delta d^+}\text{, }\langle 1\rangle_{\Delta s^+}\text{, }\langle x\rangle_{\Delta u^--\Delta d^-}$

scenario	g_A	$\left<1\right>_{\Delta u}+$	$\left<1\right>_{\Delta d}+$	$\left<1\right>_{\Delta s}+$	$\left\langle x\right\rangle _{\Delta u^{-}-\Delta d^{-}}$
A B C	5% 3% 1%	5% 3% 1%	10% 5% 2%	100% 50% 20%	70% 30% 15%
current	3%	3%	5%	70%	65%

Assume percentage uncertainties according to three scenarios

Reweight NNPDFpol1.1 with lattice pseudodata and look at the impact



Simultaneous fits of (unp.) PDFs and FFs [arXiv:1905.03788] Multi-step procedure

- sampling the posterior distributions from flat priors for fixed-target DIS data (BCDMS, SLAC, NMC)
- update these posteriors with collider DIS data (HERA I-II)
- update the resulting posteriors with DY data (E866)
- sampling the posterior distributions from flat priors for SIA data (DESY, SLAC, CERN, KEK)

• update the FF/PDF posteriors with SIDIS data (COMPASS)

Process	$N_{\rm dat}$	$\chi^2/N_{\rm dat}$
DIS	2680	1.28
SIDIS	992	1.25
DY	250	1.67
SIA	444	1.27
Total	4366	1.30



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Simultaneous fits of (unp.) PDFs and FFs [PRD 96 (2017) 094020]

IDEA: iterative reweighting of PDFs and fit of FFs with kaon SIDIS data ($N_{\rm dat} = 906$) HERMES [PRD 87 (2013) 074029] COMPASS [PLB 767 (2017) 133]





PDFs today: need, achievements, challenges

Improvements in the NNPDF fit methodology [arXiv:1907.05075]

Current NNPDF methodology is no longer state-of-the-art Gradient-based optimisation of large NNs Quality industry backed libraries available

New NNPDF methodology: gradient descent techniques Implemented with Keras + TensorFlow Performance increased by a factor ~20 Allows to remove a lot of legacy code

Central values and fit quality remarkably stable

PDF uncertainties somewhat affected comparable in the data region significantly reduced outside

Fewer replicas for equal accuracy

Completely new classes of studies open up



Summary

Interimpact of the data

Extended experimental input, with a full control of experimental uncertainties

Unpolarised PDFs the gluon PDF at small and large xthe strange-antistrange asymmetry fitting charm (photon PDF, resummation,...)

- 2 The (limits of the) methodology
 - methodology must adapt accordingly
 - statistical analysis tools necessary to cope with data accuracy
 - PDF uncertainties are faithful, but not optimised
- The theory frontier
 - theory must adapt accordingly
 - with the reduction of data uncertainties, theoretical uncertainties become relevant
 - a complete characterisation of theoretical uncertainties in PDF fits

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the gluon PDF at small xthe individual guark-antiguark PDFs the strange PDF

Polarised PDFs

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Thank you

the gluon PDF at small x the individual quark-antiquark PDFs the strange PDF

Polarised PDFs