Helicity PDFs: status and prospects

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Foreword: parton distributions on the light cone

1 The momentum densities of partons with spin (^{\uparrow}) or (^{\downarrow}) *w.r.t.* the nucleon

$$\Delta f(x) \equiv f^{\uparrow}(x) - f^{\downarrow}(x) , \qquad \qquad f = u, \bar{u}, d, \bar{d}, s, \bar{s}, g$$

Allow for a proper field-theoretic definition as matrix elements of bilocal operators parton



$$\begin{split} y &= (y^+, y^-, \mathbf{y}_\perp) \,, \qquad y^+ = (y^0 + y^z)/\sqrt{2} \,, \qquad y^- = (y^0 - y^z)/\sqrt{2} \,, \qquad \mathbf{y}_\perp = (v^x, v^y) \\ G^{\alpha}_{\mu\nu} &= \partial_\mu A^a_\nu - \partial_\nu A^a_\mu + f^{abc} A^b_\mu A^c_\nu \end{split}$$

All these definitions have ultraviolet divergences which must be renormalized

Experimental probes

Process	Reaction	Subprocess	PDFs probed	x	$Q^2/p_T^2/M^2 \; [{\rm GeV^2}]$
	$\ell^{\pm}\{p,d,n\} \to \ell^{\pm}X$	$\gamma^* q \to q$	$\begin{array}{c} \Delta q + \Delta \bar{q} \\ \Delta g \end{array}$	$0.003 \lesssim x \lesssim 0.8$	$1 \lesssim Q^2 \lesssim 70$
N N N N N N N N N N N N N N N N N N N	$\ell^{\pm}\{p,d\} \to \ell^{\pm}hX$ $\ell^{\pm}\{p,d\} \to \ell^{\pm}DX$	$\gamma^* q \to q$ $\gamma^* g \to c\bar{c}$	$\begin{array}{c} \Delta u \ \Delta \bar{u} \\ \Delta d \ \Delta \bar{d} \\ \Delta g \\ \Delta g \\ \Delta g \end{array}$	$0.005 \lesssim x \lesssim 0.5$ $0.06 \lesssim x \lesssim 0.2$	$\begin{split} &1 \lesssim Q^2 \lesssim 60 \\ &\sim 10 \end{split}$
N2 N1	$\overrightarrow{p} \overrightarrow{p} \to jet(s)X$ $\overrightarrow{p} p \to W^{\pm}X$ $\overrightarrow{p} \overrightarrow{p} \to \pi X$	$\begin{array}{c} gg \rightarrow qg \\ qg \rightarrow qg \\ u_L \bar{d}_R \rightarrow W^+ \\ d_L \bar{u}_R \rightarrow W^- \\ gg \rightarrow qg \\ qg \rightarrow qg \end{array}$	Δg $\Delta u \ \Delta ar u$ $\Delta d \ \Delta ar d$ Δg	$0.05 \lesssim x \lesssim 0.2$ $0.05 \lesssim x \lesssim 0.4$ $0.05 \lesssim x \lesssim 0.4$	$\begin{aligned} 30 &\lesssim p_T^2 \lesssim 800 \\ &\sim M_W^2 \\ 1 &\lesssim p_T^2 \lesssim 200 \end{aligned}$
DIS :	$g_{1} = \frac{\sum_{q}^{n_{f}} e_{q}^{2}}{2n_{f}} \left(C_{\rm NS} \otimes \Delta q_{\rm NS} + C_{\rm S} \otimes \Delta \Sigma + 2n_{f}C_{g} \otimes \Delta g \right)$				
SIDIS :	$g_1^h = \sum_{q,\bar{q}} e_q^2 \left[\Delta q \otimes C_{qq}^{1,h} \otimes D_q^h + \Delta q \otimes C_{gq}^{1,h} \otimes D_g^h + \Delta g \otimes C_{qg}^{1,h} \otimes D_q^h \right]$				
pp:	$\Delta \sigma = \sigma^{(+)+} - \sigma^{(+)-} = \sum_{a,b,(c)} \Delta f_a \otimes (\Delta) f_b(\otimes D_c^h) \otimes \Delta \hat{\sigma}_{ab}^{(c)}$				

 $C{\rm s:}$ NNLO for DIS [NPB 889(2014) 351; arXiv:1908.03779]; NLO for SIDIS and pp $P{\rm s:}$ NNLO [NP B889(2014) 351]

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Helicity PDFs: status and prospects

Recent determinations of polarised PDFs

	DSSV	NNPDF	JAM
DIS	\square	\square	\square
SIDIS	\checkmark	\boxtimes	\checkmark
pp	\checkmark (jets, π^0)	\swarrow (jets, W^{\pm})	\boxtimes
statistical treatment	Lagr. mult. $\Delta\chi^2/\chi^2=2\%$ Monte Carlo	Monte Carlo	Monte Carlo
parametrization	polynomial (23 pars)	neural network (259 pars)	polynomial (10 pars)
features	global fit	minimally biased fit	large-x effects
latest updates	DSSV08 PRD 80 (2009) 034030 DSSV14 PRL 113 (2014) 012001	NNPDFpol1.0 NPB 874 (2013) 36 NNPDFpol1.1 NPB 887 (2014) 276	JAM15 PRD 93 (2016) 074005 JAM17 PRL 119 (2017) 132001

+ simultaneous determination of PDF uncertainties (data, theory, methodology) A matematically ill-posed problem: determine a set of functions from a finite set of data

$$E[\mathcal{O}] = \int \mathcal{D}\Delta f \mathcal{P}(\Delta f | data) \mathcal{O}(\Delta f) \qquad V[\mathcal{O}] = \int \mathcal{D}\Delta f \mathcal{P}(\Delta f | data) [\mathcal{O}(\Delta f) - E[\mathcal{O}]]^2$$

 $\begin{array}{l} \text{Monte Carlo (JAM, NNPDF, DSSV)} \\ \mathcal{P}(\Delta f | data) \longrightarrow \{\Delta f_k\} \\ E[\mathcal{O}] \approx \frac{1}{N} \sum_k \mathcal{O}(\Delta f_k) \\ V[\mathcal{O}] \approx \frac{1}{N} \sum_k [\mathcal{O}(\Delta f_k) - E[\mathcal{O}]]^2 \end{array}$

Maximum likelihood (DSSV, LSS, BB)

$$\mathcal{P}(\Delta f | data) \longrightarrow \Delta f_0$$
$$E[\mathcal{O}] \approx \mathcal{O}(\Delta f_0)$$

 $V[\mathcal{O}] \approx \mathsf{Hessian}, \Delta \chi^2 \mathsf{envelope}, \dots$

Polarised PDFs: NNPDFpol1.x [Nucl.Phys. B887 (2014) 276]



	EXPERIMENT	Ndat	x	$\chi^2/N_{\rm dat}$		
		dat	1.0	1.1	1.2	
	EMC	10	0.44	0.43	0.43	
	SMC	24	0.93	0.90	0.92	
	SMClowx	16	0.97	0.97	0.94	
	E142	8	0.67	0.66	0.55	
	E143	50	0.64	0.67	0.63	
	E154	11	0.40	0.45	0.34	
	E155	40	0.89	0.85	0.98	
	COMPASS-D	15	0.65	0.70	0.57	
	COMPASS-P	15	1.31	1.38	0.93	
	HERMES97	8	0.34	0.34	0.23	
	HERMES	56	0.79	0.82	0.69	
new	COMPASS-P-15	51	0.98*	0.99*	0.65	
new	COMPASS-D-17	15	1.32*	1.32*	0.80	
new	JLAB-E93-009	148	1.26*	1.23*	0.94	
new	JLAB-EG1-DVCS	18	0.45*	0.59*	0.29	
new	JLAB-E06-014	2	2.81*	3.20*	1.33	
	COMPASS (OC)	45	1.22*	1.22	1.22	
	STAR (jets)	41	_	1.05	1.06	
	PHENIX (jets)	6	—	0.24	0.24	
	STAR- $A_L^{W^{\pm}}$ (2012)	24	_	1.05	1.05	
	STAR- $A_{LL_1}^{W^{\pm}}$	12	—	0.95	0.94	
new	STAR- $A_{I}^{W^{\pm}}$ (2013)	8	_	2.76*	1.34	
new	STAR (dijets)	14	—	1.34*	1.00	
	TOTAL		0.77	1.05	1.01	

* data set not included in the corresponding fit

Gluon polarisation



High-p_T di-jets [PRD 95 (2017) 071103] confirm a positive gluon polarization in the proton



Gluon polarisation



New Monte Carlo version of the DSSV analysis [arXiv:1902.10548]

Effect of STAR high- p_T dijets at $\sqrt{s} = 200$ GeV similar to that observed in NNPDF

Uncertainty almost unaffected

Slight distortion of the central value, consistent with a positive polarisation, towards smaller values of x

Gluon polarisation



Small-x behaviour can be modified by small-x evolution [JHEP1601 (2016) 072, JHEP1710 (2017) 198, ...]

Gluon polarisation and charm



Heavy flavour contribution to g_1 , specifically from charm irrelevant ($\ll 1\%$) so far in fixed-target DIS, relevant at an EIC depending on Δg small Δg (DSSV07) $\Rightarrow g_1^c$ negligible; $A_1^c \sim \mathcal{O}(10^{-5})$ too small to be measured large Δg (GRSV) $\Rightarrow g_1^c \sim 10 - 15\%$ of g_1 at $x = 10^{-3}$, $Q^2 \simeq 10$ GeV²; $A_1^c \sim \mathcal{O}(10^{-3})$ charm not massless at the EIC kinematics: relevant NLO corrections are needed

Total up and down polarisations [JPCS 678 (2016) 012030]



- Improved accuracy at small x: new COMPASS data (+ improved unpolarized F_L and F₂ from NNPDF3.1)
- Improved accuracy at large x: new JLAB data (also note that the positivity bound is slightly different)
- A lower cut on W^2 will allow for exploiting the full potential of JLAB data (if we replace $W^2 \ge 6.25 \text{ GeV}^2$ with $W^2 \ge 4.00 \text{ GeV}^2$ the χ^2 deteriorates significantly) (need to include and fit dynamic higher twists, in progress)

Total up and down at large x [PLB 742 (2015) 117]

Playground for models



Model	$\Delta d^+/d^+$	Model	$\Delta d^+/d^+$		
$\begin{array}{l} {\rm SU(6)}\\ {\rm RCQM}\\ {\rm QHD} \ (\sigma_{1/2})\\ {\rm QHD} \ (\psi_{\rho}) \end{array}$	$-1/3 \\ -1/3 \\ 1 \\ -1/3$	NJL DSE (<i>realistic</i>) DSE (<i>contact</i>) pQCD	$-0.25 \\ -0.26 \\ -0.33 \\ 1$		
NNPDFpol1.1 ($x = 0.9$) -0.74 ± 3.57 NNPDFpol1.2 ($x = 0.9$) -0.23 ± 1.06					

Beyond leading-twist factorisation

Fit of higher twist terms (up to $\tau = 4$) in JAM15 [PRD 93 (2016) 074005]



 $g_1^{\tau=3} \propto D$ and $g_1^{\tau=4} = H/Q^2$

nonzero twist-3 quark distributions twist-4 quark distributions compatible with zero

Small-x asymptotics of the quark helicity



[JHEP 1601 (2016) 072]

Small-x evolution equations for g_1 based on the dipole model resum powers of $\alpha_s \ln^2(1/x)$ become closed for N_C , n_f large a solution for the flavor-singlet is

$$g_1 \sim \Delta \Sigma \sim \left(rac{1}{x}
ight)^{lpha_h}, \quad \alpha_h \sim 2.31 \sqrt{rac{lpha_s N_C}{2\pi}}$$

Potential solid amount of spin at small x attach $\Delta \hat{\Sigma}(x,Q^2) = N x^{-\alpha_h}$ at x_0 to DSSV detailed phenomenology needed Should be tested at an EIC



arXiv:1611.07980

FIT	1:	$\Delta T_3 = 1.2701$	1 ± 0.0025				
		$\Delta T_8 = 0.585$	± 0.176				
FIT	2:	$\Delta U^{+}_{} = +1.0$	98 ± 0.220				
		$\Delta D^{+} = -0.4$	17 ± 0.084				
		$\Delta S^+ = -0.00$	05 ± 0.001				
FII	3.	$\Delta U^+ = +1.1$	32 ± 0.226				
	$\Delta D^+ = -0.368 \pm 0.074$						
_	4	$\Delta S^{+} = 0$					
_		FIT1	FIT2	FIT3			
x	2 dat	0.74	0.76	0.79			
	uau						

Sea guark polarisation $\Delta_s = \Delta \bar{u} - \Delta d_{\text{[arXiv:1702.05077]}}$



See also M. Zurek's talk

 $\rightarrow +0.07 \pm 0.01$

х

Sea quark polarisation $\Delta_s = \Delta \bar{u} - \Delta d$

Deep insight:

More data available: PHENIX W run 11-13 at 510 GeV [PRD 93 (2016) 051103] a high-energy polarised Electron-Ion Collider [PRD 88 (2013) 114025] accurate determination of $\Delta \bar{u}$ and Δd through CC DIS and SIDIS





SU(3) breaking and strangeness



All PDF determinations based only on DIS data (+ SU(3)) find a negative Δs^+ PDF determinations based on DIS+SIDIS data (+SU(3)) find a negative or a positive Δs^+ depending on the K FF set [PRD 91 (2015) 054017]

Tension between DIS and SIDIS data can be ficticious

SU(3) may be broken [PRD 58 (1998) 094028, Ann.Rev.Nucl.Part.Sci. 53 (2003) 39], but how much? \rightarrow in NNPDFpol, the nominal uncertainty on a_8 in inflated by 30% of its value to allow for a SU(3) symmetry violation ($a_8 = 0.585 \pm 0.025 \rightarrow a_8 = 0.585 \pm 0.176$) \rightarrow but e.g. lattice finds a larger SU(3) symmetry violation [PRL 108 (2012) 222001]

Opportunities at an EIC

one could study kaon multiplicities in SIDIS \longrightarrow further constraint on kaon FFs one could study CC charm production $W^+s \rightarrow c$ in DIS \longrightarrow direct handle on s, \bar{s} (handle on $s-\bar{s}$ asymmetry also from three-loop evolution [PRD 99 (2019) 054001])

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SIDIS and Fragmentation Functions [See A. Vossen's talk]

	DHESS	JAM	NNFF
SIA	SIA 🔽		Ø
SIDIS	SIDIS 🗹		\boxtimes
PP	PP 🗹		🗹 (h [±])
statistical treatment	tistical Iterative Hessian atment 68% - 90%		Monte Carlo
parametrisation	standard	standard	neural network
pert. order	(N)NLO	NLO	up to NNLO
HF scheme	ZM(GM)-VFN	ZM-VFN	ZM-VFN

Focus on new data: BELLE and BABAR SIA cross sections COMPASS SIDIS multiplicities Overall fair agreement among the three sets (except flavour separation for K^{\pm}) NNFF uncertainties usually larger (especially for the gluon) Note various shapes for the π^{\pm} gluon



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Fragmentation Functions at a future EIC [PRD 99 (2019) 094004]

Assess the quantitative impact of simulated π^{\pm} and K^{\pm} DIS data at an EIC Consider one kinematic scenario for the EIC (\sqrt{s} =140 GeV)

Appreciate the significant impact on all FFs



Comparing lattice QCD and global fit PDF moments



Which precision shall we require to lattice QCD?

Generate lattice QCD pseudodata assuming NNPDFpol1.1 central values for

 $g_A\equiv\langle 1\rangle_{\Delta u^+-\Delta d^+}\text{, }\langle 1\rangle_{\Delta u^+}\text{, }\langle 1\rangle_{\Delta d^+}\text{, }\langle 1\rangle_{\Delta s^+}\text{, }\langle x\rangle_{\Delta u^--\Delta d^-}$

scenario	g_A	$\left<1\right>_{\Delta u}+$	$\left<1\right>_{\Delta d}+$	$\left<1\right>_{\Delta s}+$	$\left\langle x\right\rangle _{\Delta u^{-}-\Delta d^{-}}$
A B C	5% 3% 1%	5% 3% 1%	10% 5% 2%	100% 50% 20%	70% 30% 15%
current	3%	3%	5%	70%	65%

Assume percentage uncertainties according to three scenarios

Reweight NNPDFpol1.1 with lattice pseudodata and look at the impact



Simultaneous fits of (pol.) PDFs and FFs [PRL 119 (2017) 132001]





Improvements in the NNPDF fit methodology [arXiv:1907.05075]

Current NNPDF methodology is no longer state-of-the-art Gradient-based optimisation of large NNs Quality industry backed libraries available

New NNPDF methodology: gradient descent techniques Implemened with Keras + TensorFlow Performance increased by a factor ~20 Allows to remove a lot of legacy code

Central values and fit quality remarkably stable

PDF uncertainties somewhat affected comparable in the data region significantly reduced outside

Fewer replicas for equal accuracy



Summary

After three decades of experimental and theoretical activity, we cannot really say we know $\Delta\Sigma$ and Δg Main culprit: small-x behavior of polarized PDFs

Spin experiments continue to produce high impact results (RHIC, JLAB, COMPASS) first evidence of gluon polarization and light sea symmetry in the proton

Theory efforts and global QCD analyses try to keep up

Only an EIC would be able to push forward our knowledge of the nucleon spin content

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[Spin] is a mysterious beast, and yet its practical effect prevails the whole of science. The existence of spin, and statistics associated with it, is the most subtle and ingenious design of Nature - without it the whole Universe would collapse.

S-I. Tomonaga, The story of spin 2nd ed., University of Chicago Press (1998) [from the preface]

Thank you