



INTRINSIC CHARM IN THE PROTON

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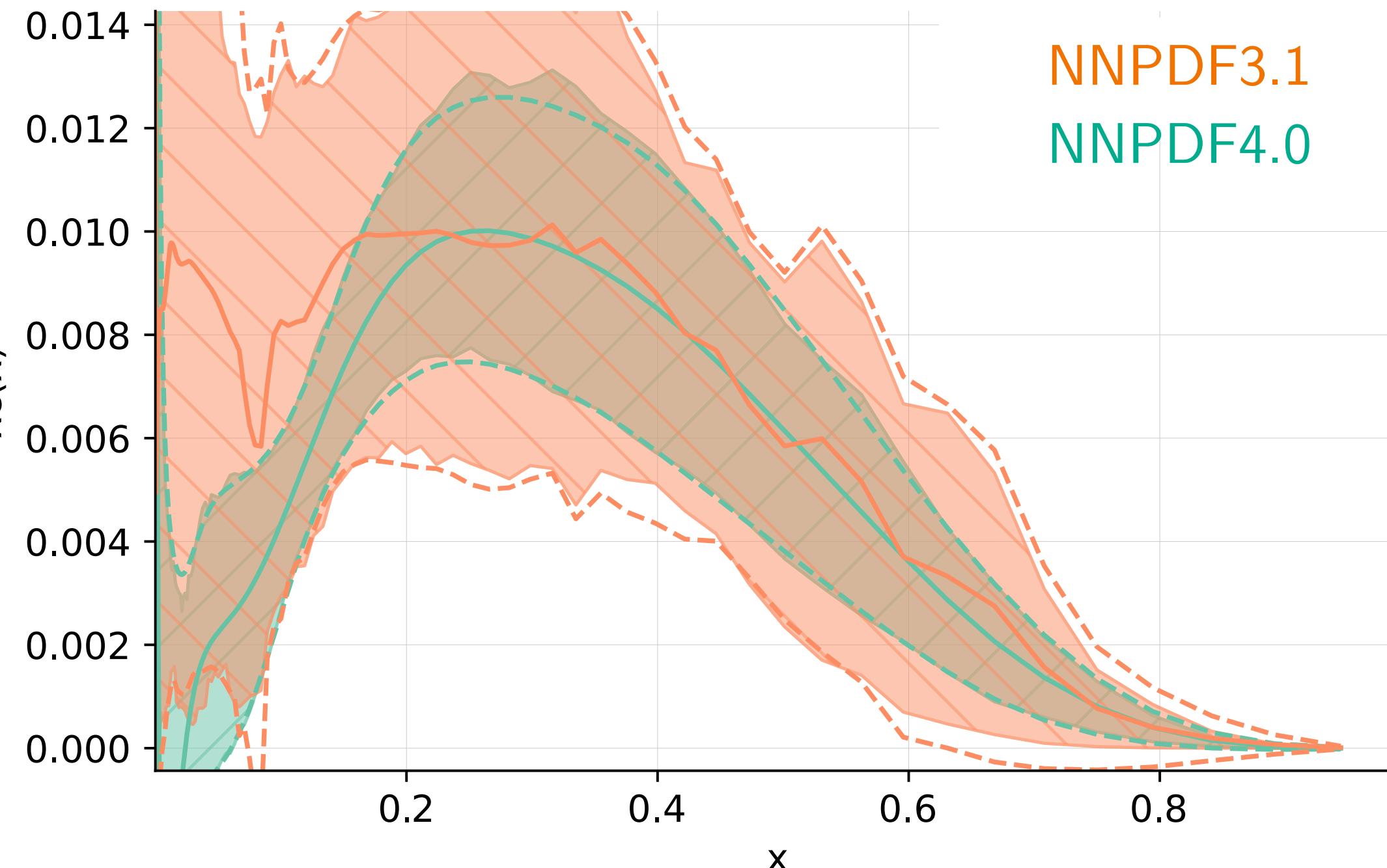
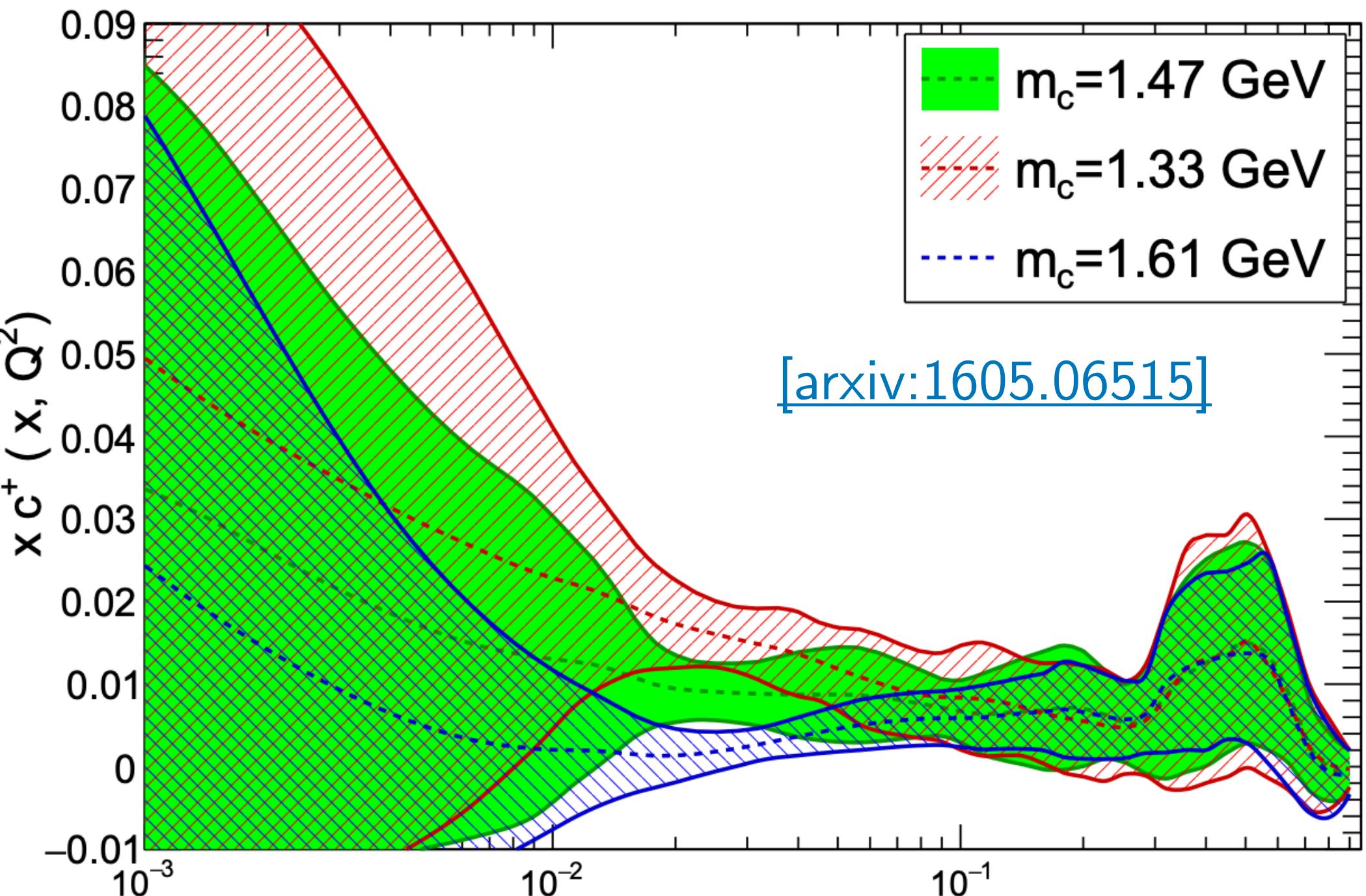


Introduction & Motivation

Do heavy quarks contribute to the proton PDFs at low scales?

- Will focus on the **charm PDF**, as the *natural candidate* to answer this question
- Will present results based on a work:
NNPDF collaboration, "Charm in the proton"
[Ball, Candido, Cruz-Martinez, Forte, Giani, Hekhorn, Kudashkin, Magni, Rojo] (*in preparation*)
- Results are based on the NNPDF4.0 [\[arxiv:2109.02653\]](#): great progress in the charm determination in the last years: both in the fitting framework and in number of included datapoints.

NNPDF3 NLO Fitted Charm, $Q=1.65 \text{ GeV}$

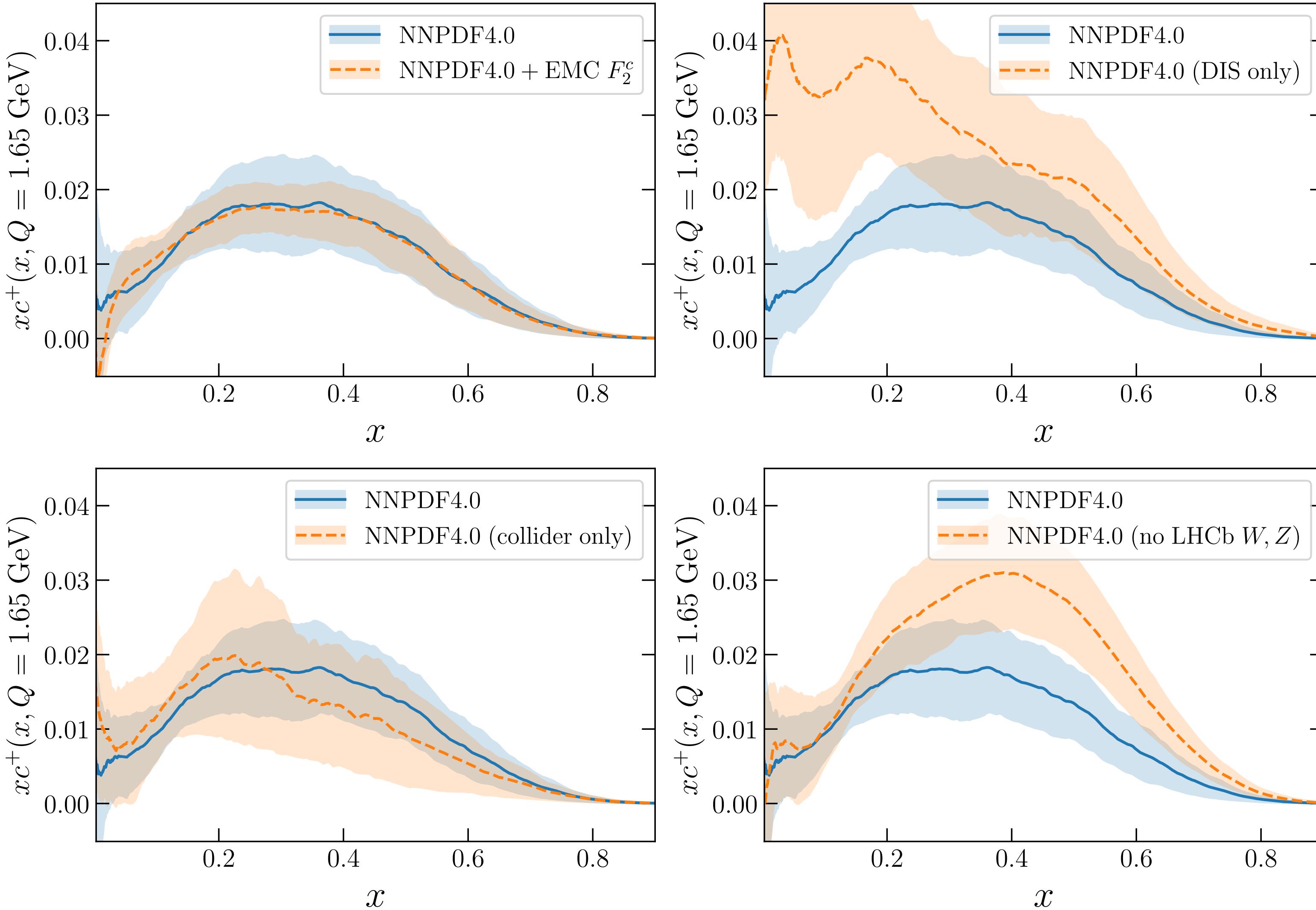


The charm PDF

NNPDF4.0 baseline

- The charm PDF is parametrised as an independent combination at scale $Q_0 = 1.65 \text{ GeV}$, and $n_f = 4$ (4FNS)
- c^+ at the fitting scale exhibits a non vanishing peak in the *high-x* region and vanishes at *low-x*
- $\bar{c} = c$
- Constrains are coming mainly from collider data
- NNPDF4.0 is consistent with EMC data.

$$xc^+(x, Q_0, \Theta) = \left(x^{\alpha_\Sigma} (1-x)^{\beta_\Sigma} NN_\Sigma(x, \Theta) - x^{\alpha_{T_{15}}} (1-x)^{\beta_{T_{15}}} NN_{T_{15}}(x, \Theta) \right) / 4$$



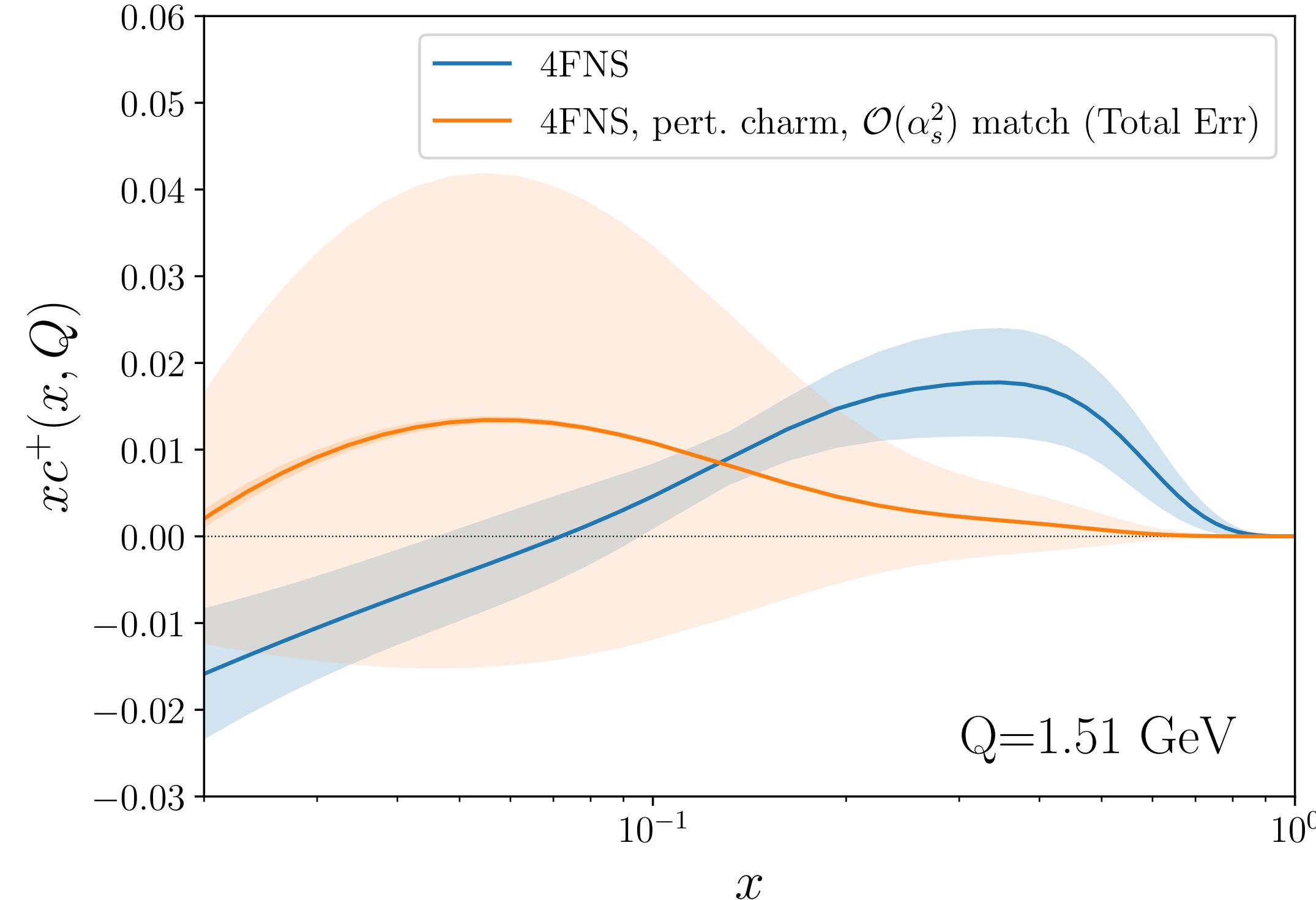
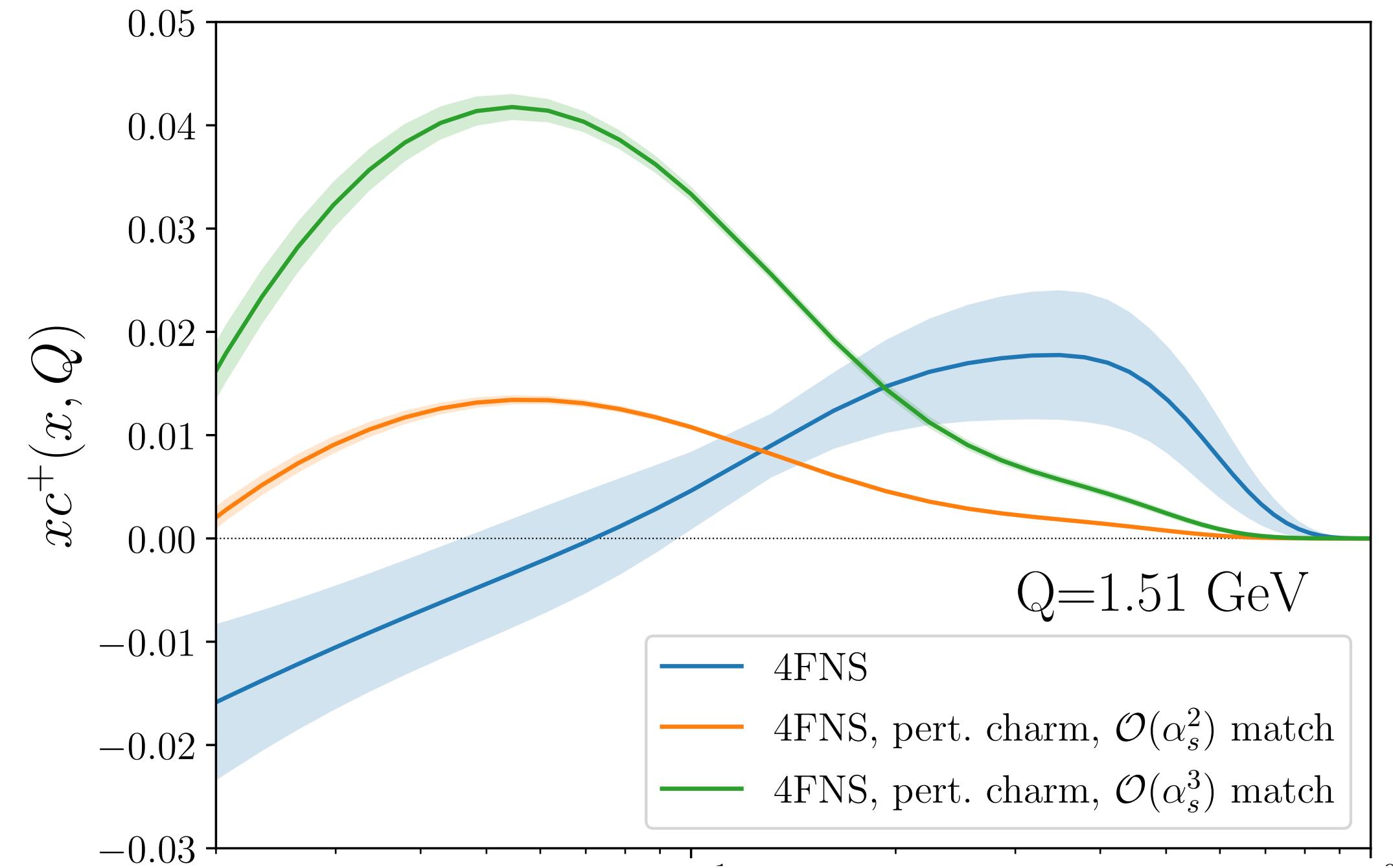
Why do we need fitted charm?

The fully perturbative scenario

- **Perturbative charm** functional form is fully determined by the DGLAP evolution and the initial boundary conditions.
- In this case PDF uncertainties are clearly not the dominant source of uncertainties. Needs to estimate MHOU and mass dependence.

However...

- $\chi^2_{\text{fitted ch.}} = 1.17 \rightarrow \chi^2_{\text{pert ch.}} = 1.19$ mainly due to a worsening of the LHC W, Z and top pair data sets
- Fully perturbative charm is not compatible with the fitted one.



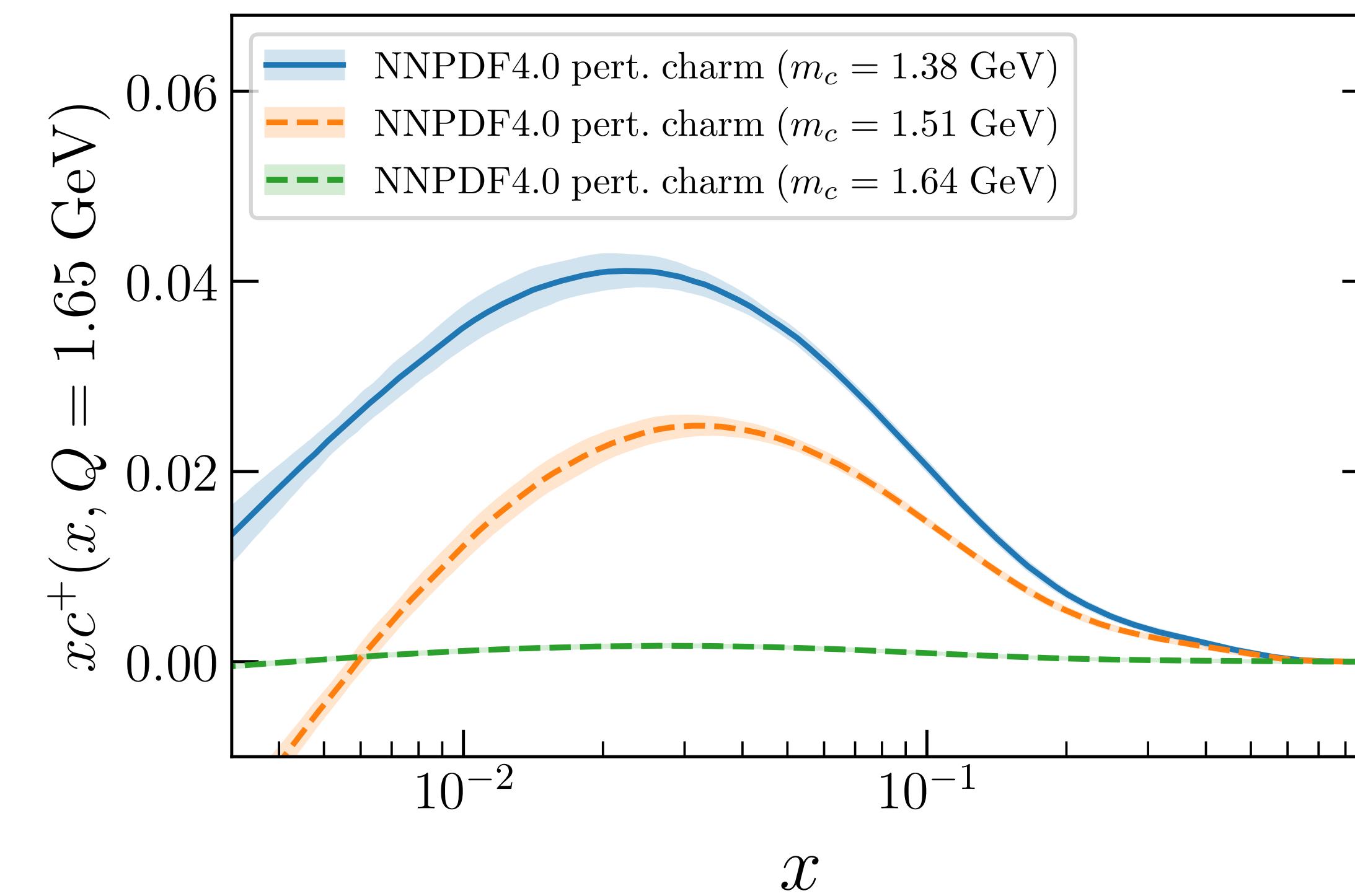
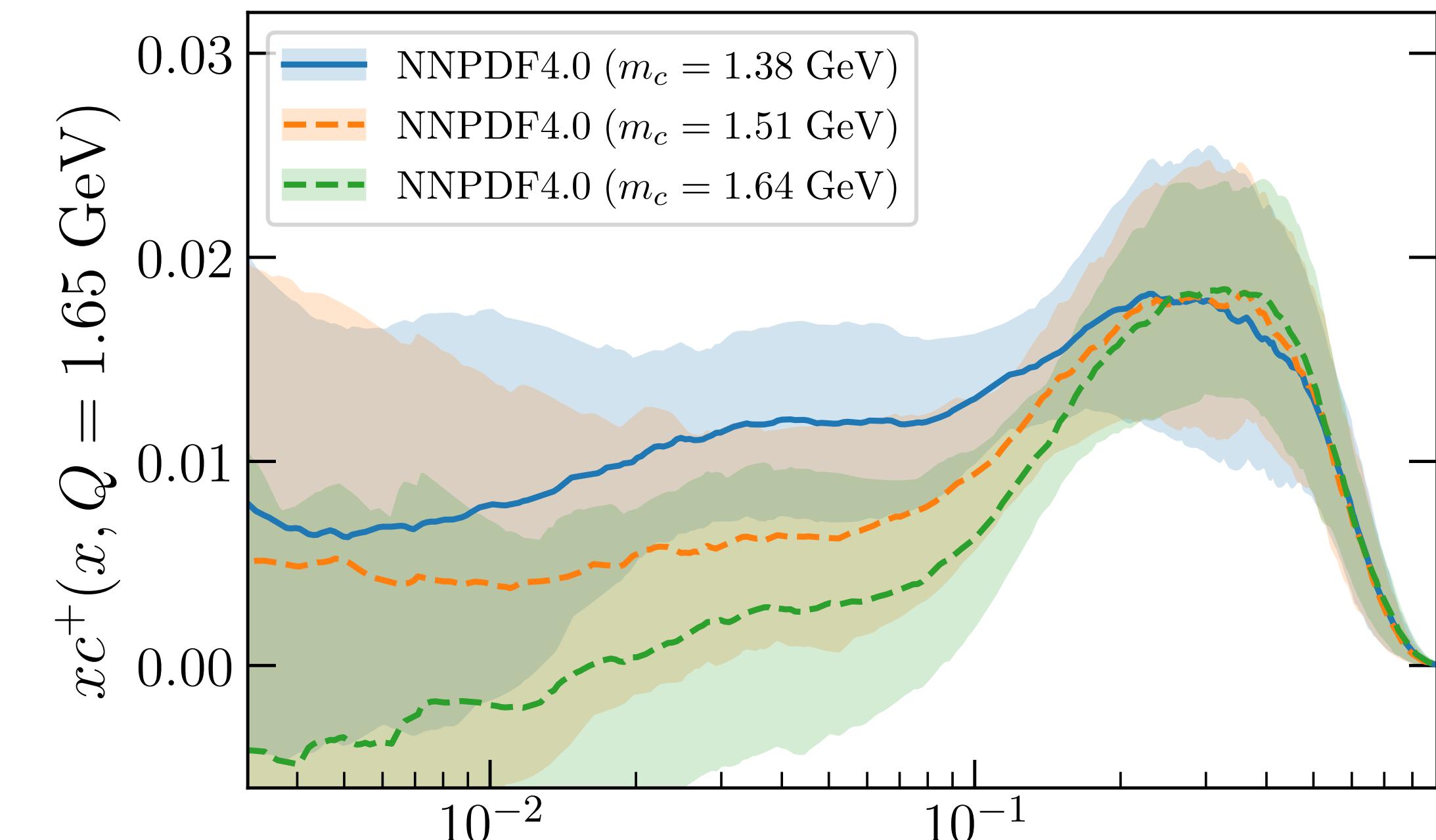
Why do we need fitted charm?

Mass dependence

- NNPDF4.0 fit is carried out using heavy quark *pole masses*
- Charm mass is varied in the range:

$$m_c = 1.51 \pm 0.13 \text{ GeV}$$

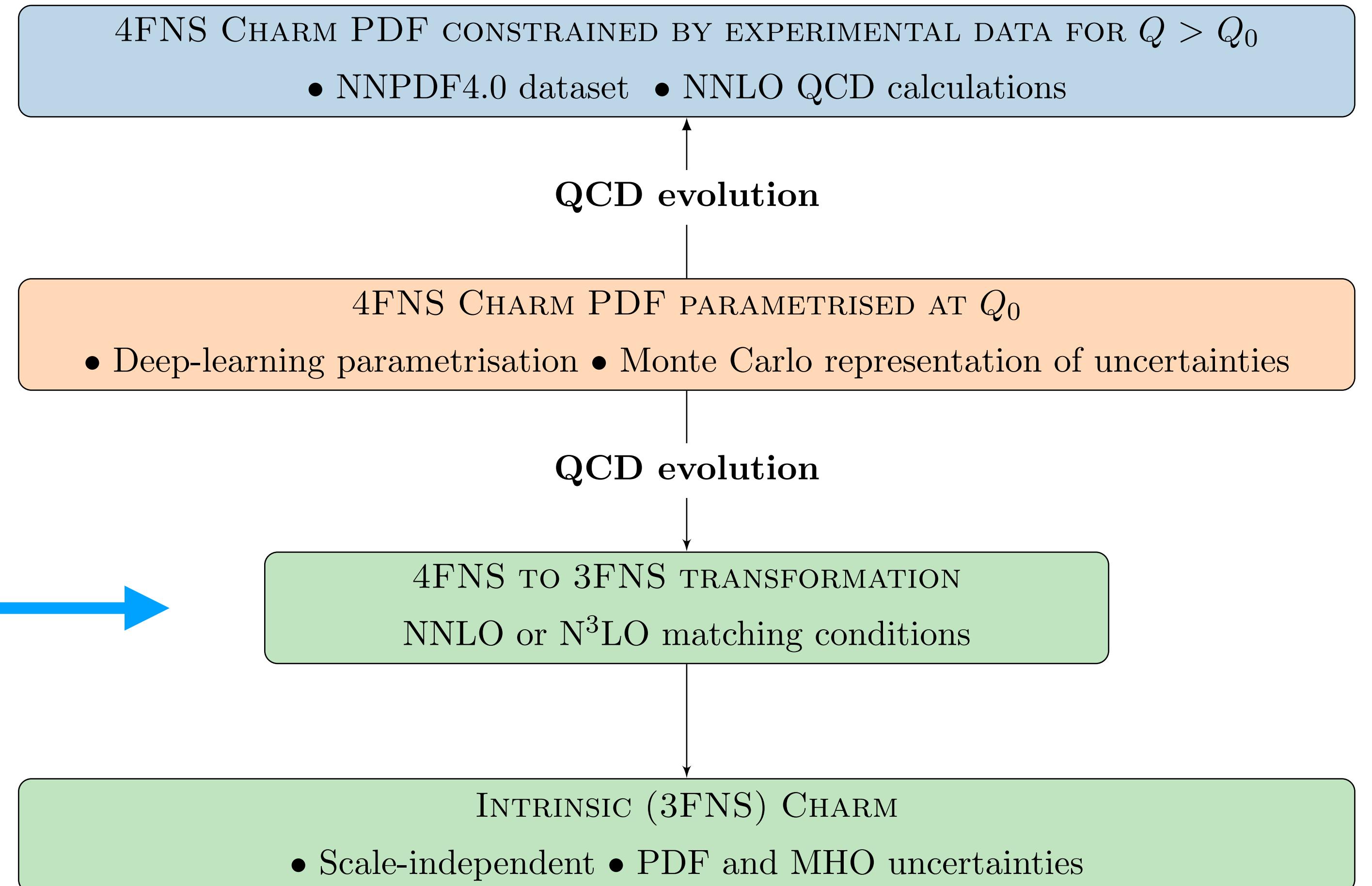
- The fitted charm is much more stable upon mass variation especially in the *high-x* region compared to the perturbative one.



The Intrinsic charm scenario

From 4FNS to 3FNS

- Below the charm mass scale the perturbative charm is vanishing by definition
- Fitted charm in *4FNS* contains both the intrinsic and the perturbative components.
- Need to determine the *3FNS* charm PDF



A brief digression on DGLAP

DGLAP evolution with EKO

$$\frac{d}{d\alpha_s} \tilde{\mathbf{f}}(\mu_F^2) = - \frac{\gamma(a_s)}{\beta(a_s)} \cdot \tilde{\mathbf{f}}(a_s)$$



[\[arxiv:2202.02338\]](https://arxiv.org/abs/2202.02338)

- The formal solution of DGLAP can be written as in Mellin-space:

$$\tilde{\mathbf{f}}(a_s) = \tilde{\mathbf{E}}(a_s \leftarrow a_s^0) \cdot \tilde{\mathbf{f}}(a_s^0)$$

- In x-space:

$$\mathbf{f}(x_k, a_s) = \mathbf{E}_{k,j}(a_s \leftarrow a_s^0) \mathbf{f}(x_j, a_s^0)$$

$$\tilde{\mathbf{E}}(a_s \leftarrow a_s^0) = \mathcal{P} \exp \left[- \int_{a_s^0}^{a_s} \frac{\gamma(a'_s)}{\beta(a'_s)} da'_s \right]$$

LHA Benchmark comparison

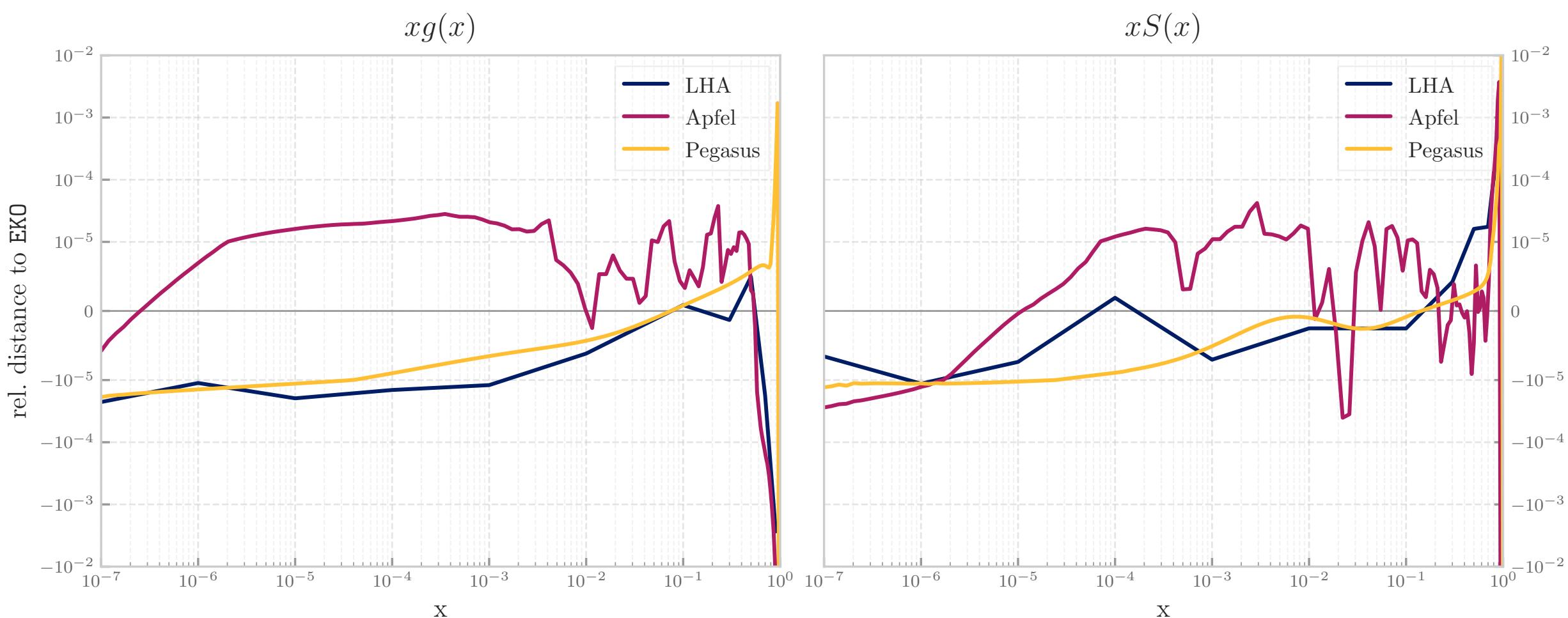
- Evolution is performed in **Intrinsic** Evolution basis:

$$\text{span}\{g, \Sigma, V, V_3, T_3, V_8, T_8, c^+, c^-, b^+, b^-, t^+, t^-\}$$

- Solution is available at: LO, NLO, NNLO

- EKO implements various solution methods:

Exact, Truncated, Expanded
documentation



From 4FNS to 3FNS

The matching conditions

At the heavy quark mass threshold the number of active flavour changes:

$$\tilde{\mathbf{f}}^{(n_f+1)}(Q_1^2) = \tilde{\mathbf{E}}^{(n_f+1)}(Q_1^2 \leftarrow \mu_h^2) \mathbf{R}^{(n_f)} \tilde{\mathbf{A}}^{(n_f)}(\mu_h^2) \tilde{\mathbf{E}}^{(n_f)}(\mu_h^2 \leftarrow Q_0^2) \tilde{\mathbf{f}}^{(n_f)}(Q_0^2)$$

Rotation from *intrinsic*^(nf) basis to *intrinsic*^(nf+1)

The Operator Matrix Elements:

- In FFNS there are no difference between forward and backward evolution (just swap the integration bounds)

- The OME depends on $\alpha_s^{n_f+1}(\mu_h^2)$ and on $\log(\mu_h^2/m_h^2)$

- OME are available up to N³LO (*NLO for heavy quark entries*)

$$\mathbf{A}^{(n_f)}(\mu_h^2) = \mathbf{I} + a_s^{(n_f+1)}(\mu_h^2) \mathbf{A}^{(n_f),(1)} + a_s^{(n_f+1),2}(\mu_h^2) \mathbf{A}^{(n_f),(2)} + a_s^{(n_f+1),3}(\mu_h^2) \mathbf{A}^{(n_f),(3)} + \mathcal{O}(\alpha_s^4)$$

$$\begin{pmatrix} \tilde{V}_{(n_f)} \\ \tilde{h}^- \end{pmatrix}^{n_f+1}(\mu_h^2) = \tilde{\mathbf{A}}_{NS,h^-}^{(n_f)}(\mu_h^2) \begin{pmatrix} \tilde{V}_{(n_f)} \\ \tilde{h}^- \end{pmatrix}^{n_f}(\mu_h^2)$$

$$\begin{pmatrix} \tilde{g} \\ \tilde{\Sigma}_{(n_f)} \\ \tilde{h}^+ \end{pmatrix}^{n_f+1}(\mu_h^2) = \tilde{\mathbf{A}}_{S,h^+}^{(n_f)}(\mu_h^2) \begin{pmatrix} \tilde{g} \\ \tilde{\Sigma}_{(n_f)} \\ \tilde{h}^+ \end{pmatrix}^{n_f}(\mu_h^2)$$

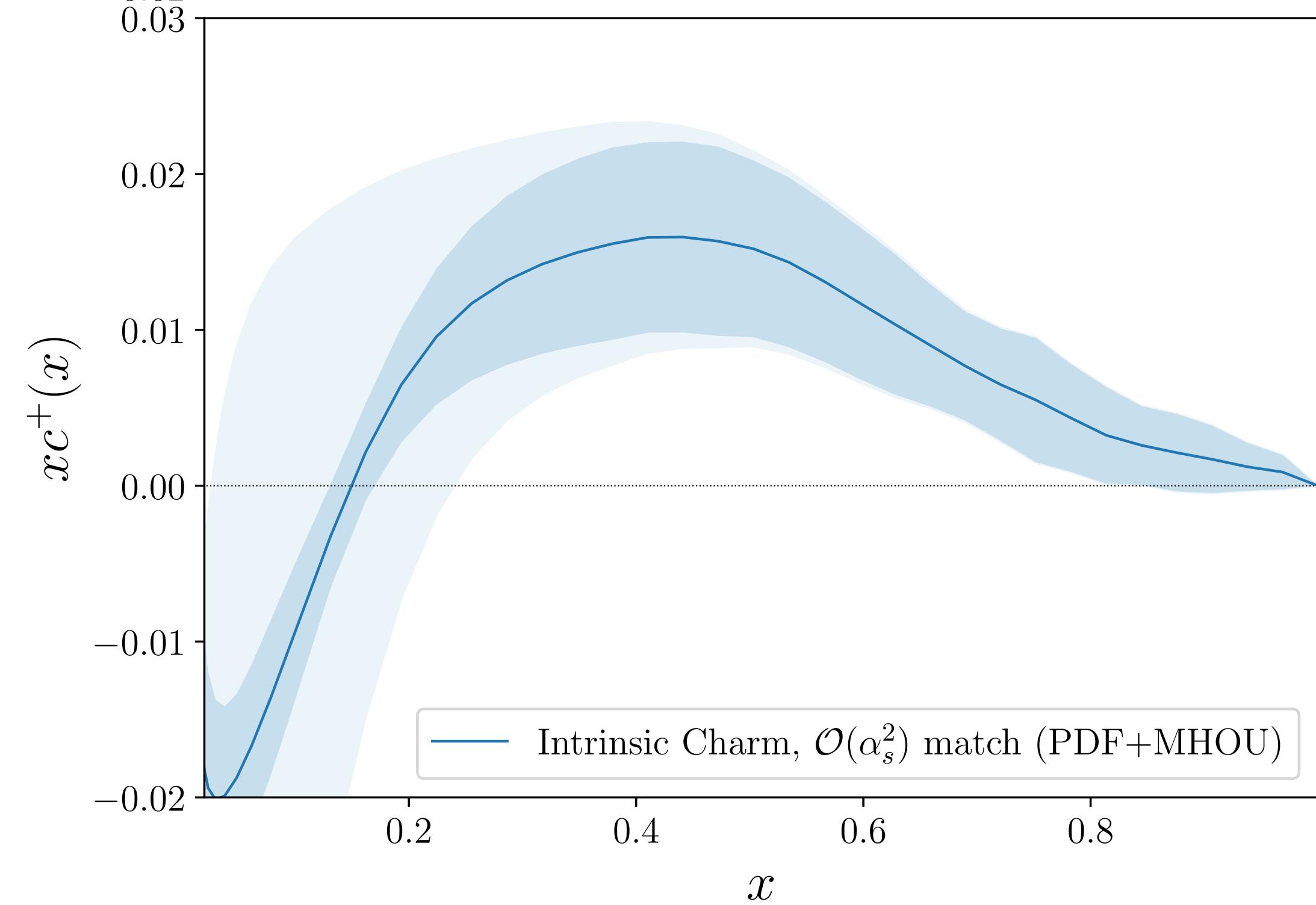
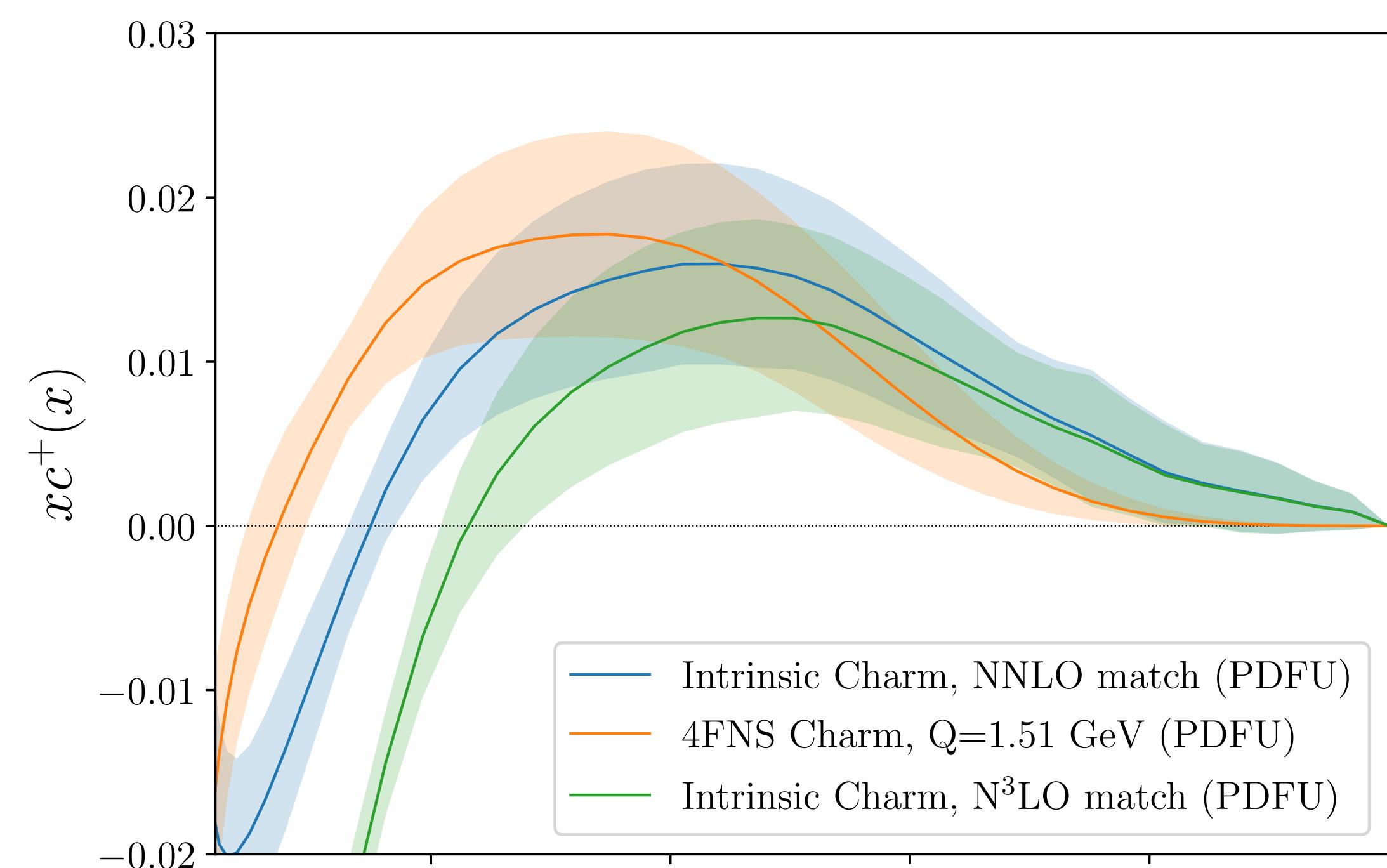
[[Eur.Phys.J.C 1 \(1998\) 301-320](#),
[Phys.Lett.B 754 \(2016\) 49-58](#),
[Nucl.Phys.B 820 \(2009\) 417-482 et al.](#)]

Intrinsic charm

- Starting from the fitting scale we evolve the NNPDF4.0 baseline to $Q = m_c$.
- When passing the heavy quark threshold we need to apply the basis rotation and then invert the OMEs $\tilde{A}_{i,j}$.
- The remaining part of the charm pdf is the intrinsic component, which is scale independent

In 3FNS:

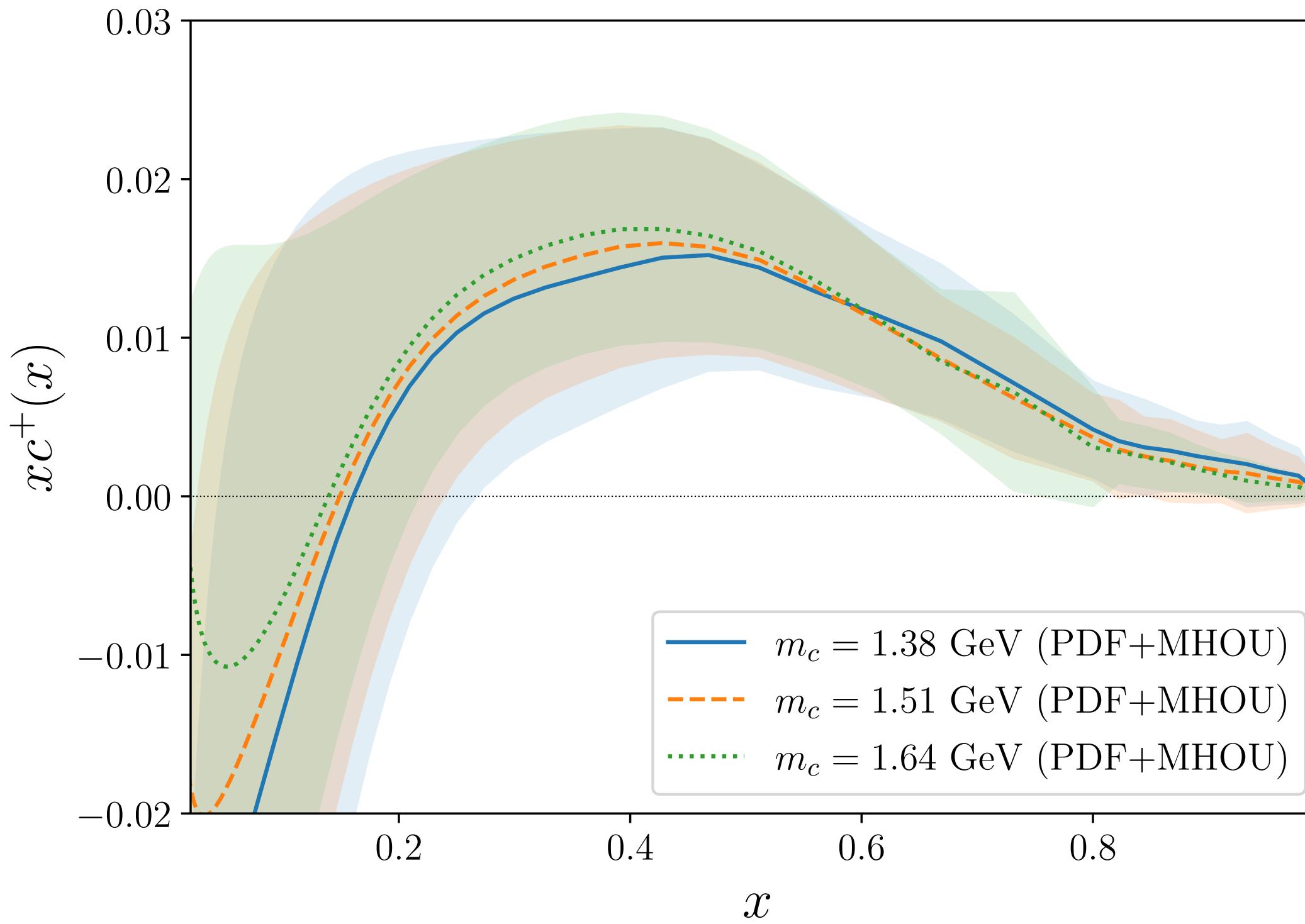
- The *valence-like* peak is still present.
- For $x \leq 0.2$ the perturbative uncertainties are quite large
- The carried momentum fraction is within 1%



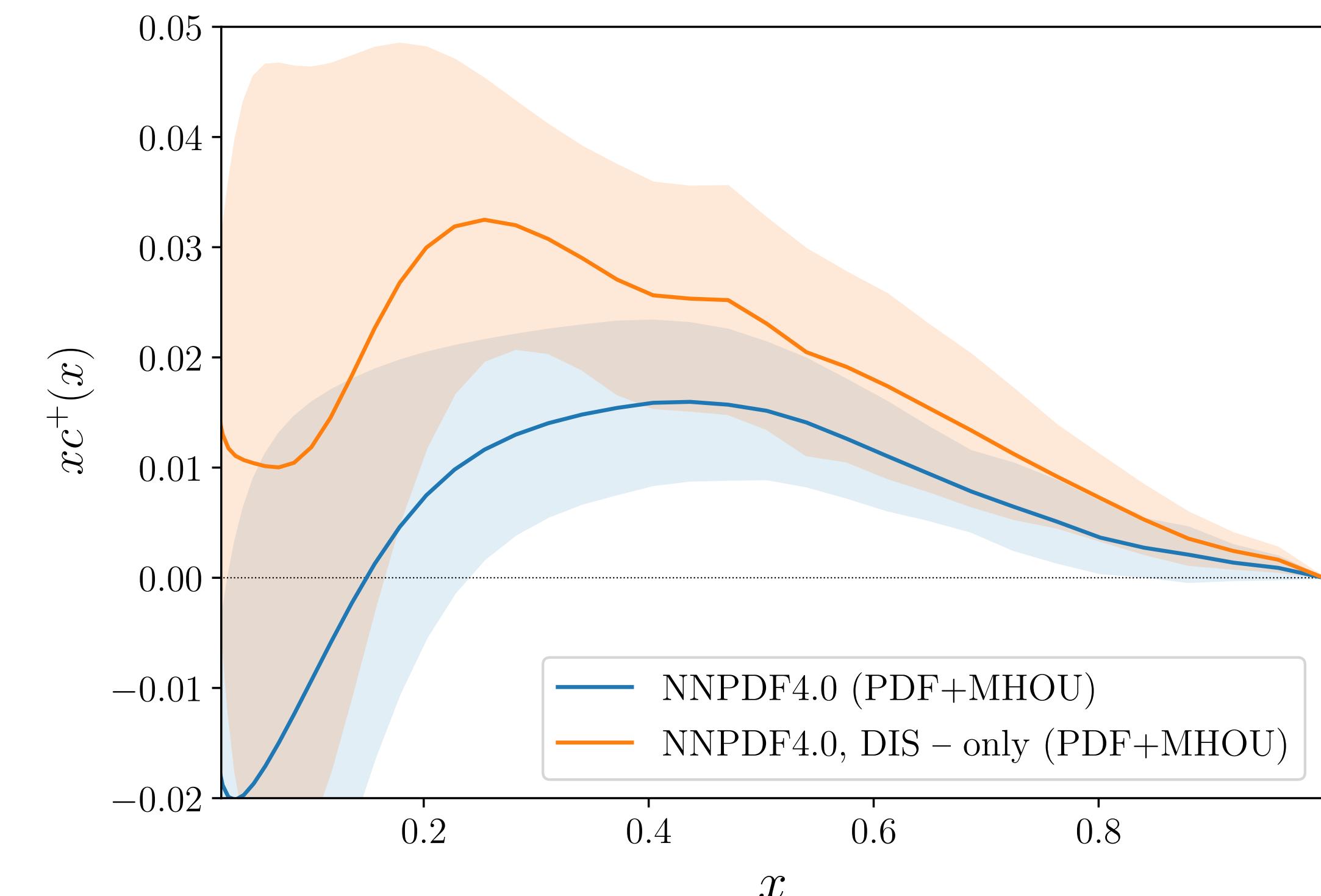
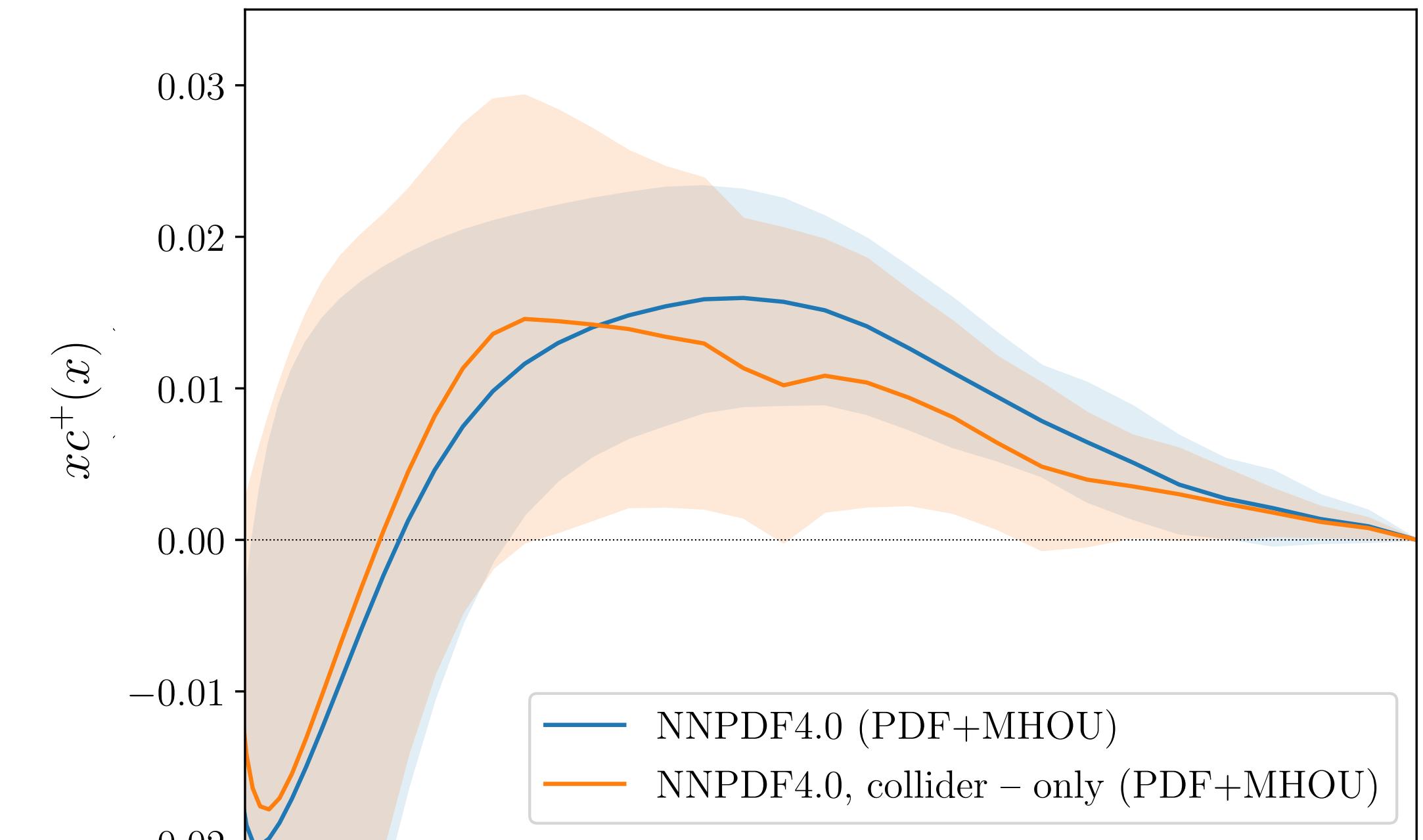
Intrinsic charm stability and accuracy

Mass dependence and dataset variation

- Intrinsic charm is stable upon mass variation
- Scale independency
- Always vanishing for $x \leq 0.2$
- MHOU coming from NNLO-N³LO matching



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The Intrinsic charm

Comparison with Models

- **BHPS model:** [\[Phy. Letter B \(1980\) 451-455\]](#)

$$p \rightarrow uud c \bar{c}$$

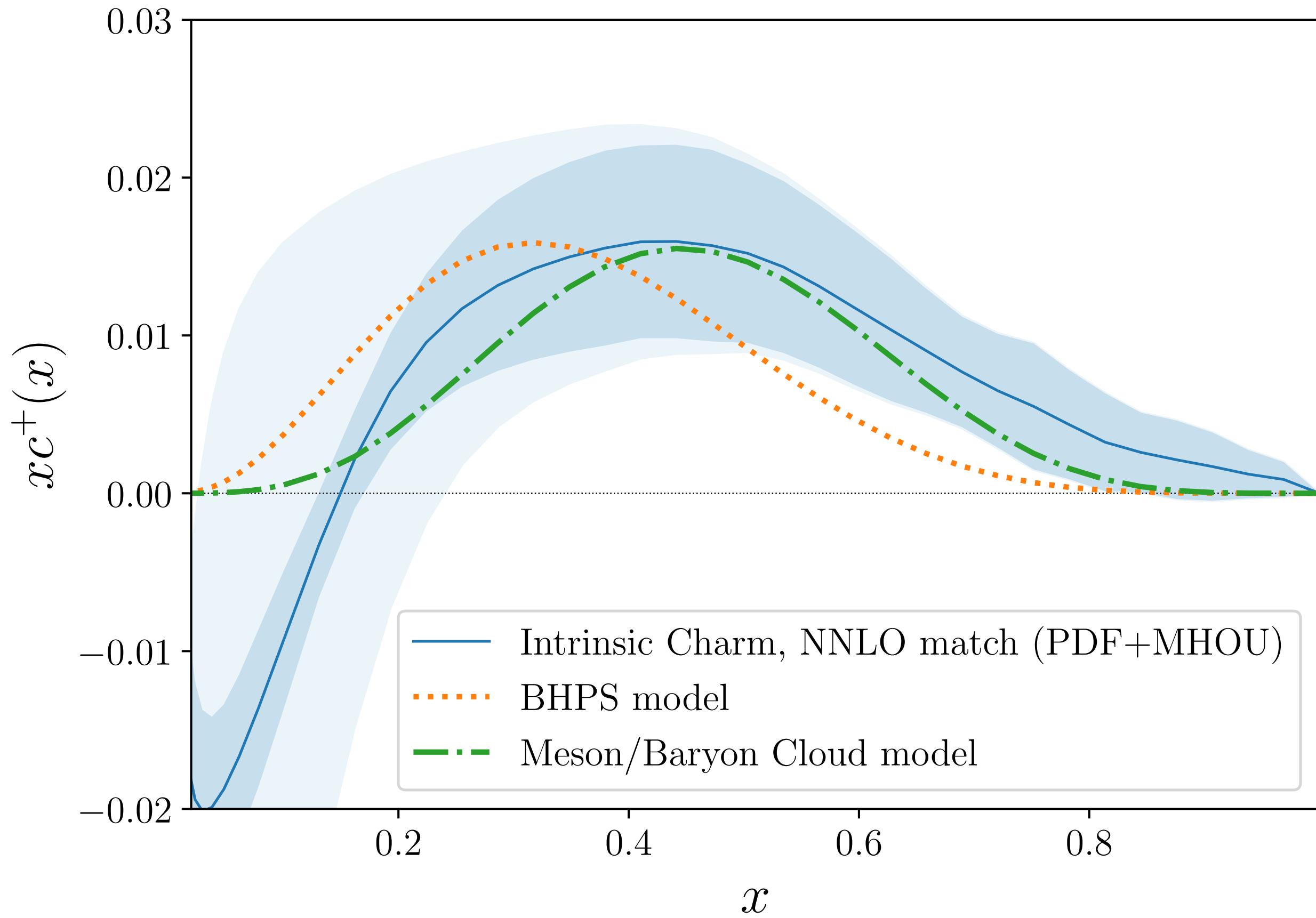
$$x c^+ = \frac{1}{2} N x^3 \left[\frac{1}{3} (1-x)(1+10x+x^2) + 2x(1+x^2)\ln(x) \right]$$

- **Meson Baryon model:** [\[arxiv:1311.1578\]](#)

$$p \rightarrow \Lambda_c^+ + \bar{D}_0$$

$$x c^+ = \frac{N}{B(\alpha+2, \beta+1)} x^{(1+\alpha)} (1-x)^\beta$$

- $\bar{c} = c$ by assumption in BHPS, not true in M/B models.
- Work in the limit $m_c \gg m_p$

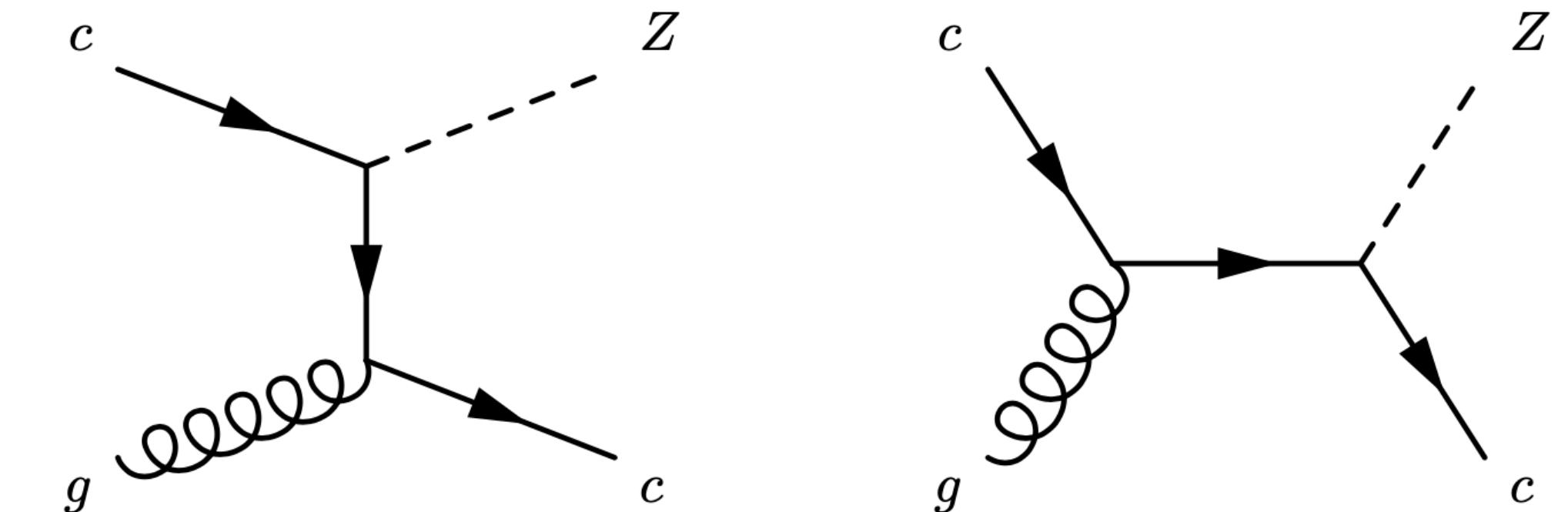
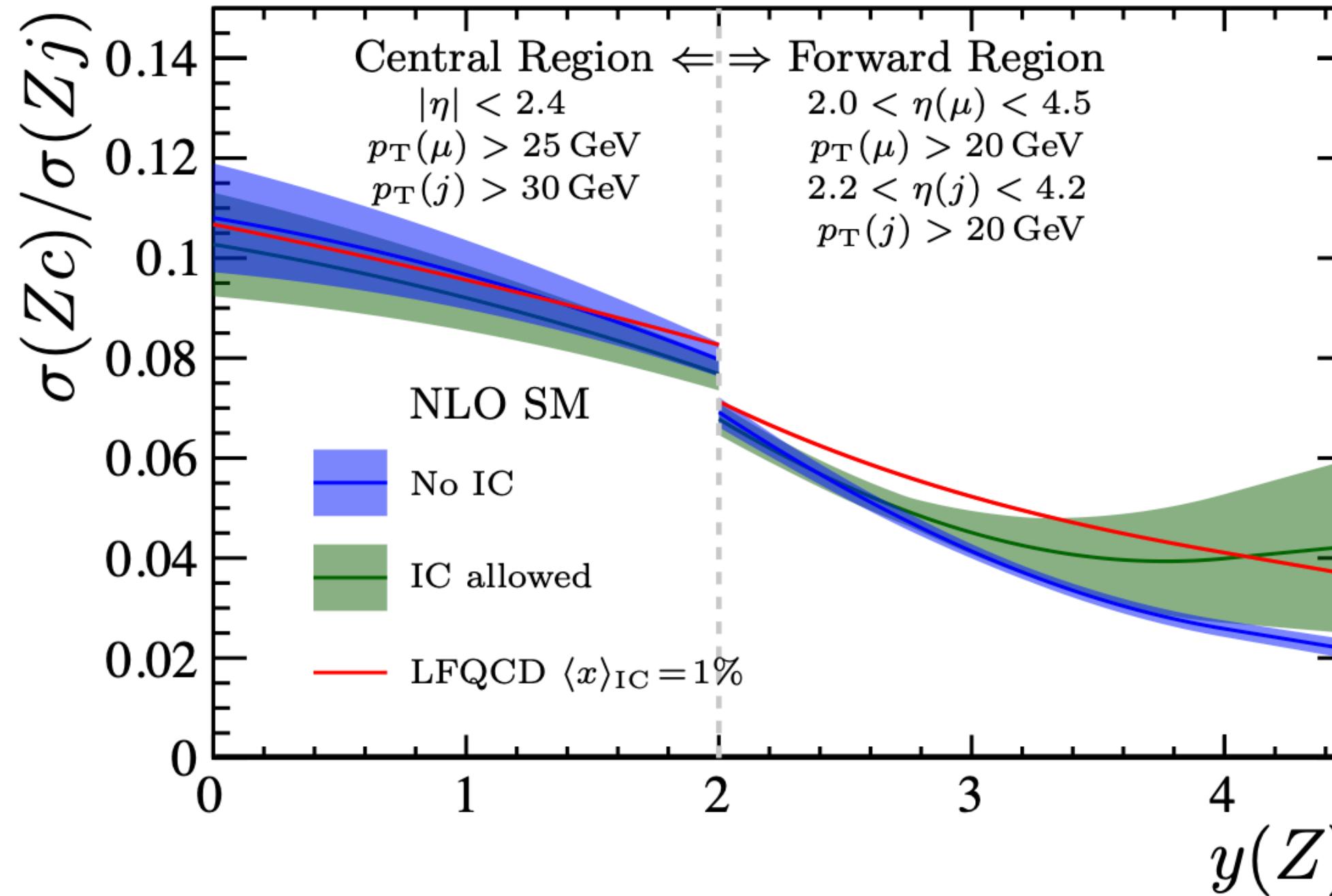


Impact on LHC observables

Z+charm production @ LHCb

We validate our observation of Intrinsic charm evaluating the prediction for:

$Z + c$ production at LHCb [\[arxiv:2109.08084\]](https://arxiv.org/abs/2109.08084)



$$R_j^c(y_Z) = \frac{\sigma_{Zc}}{\sigma_{Zj}}$$

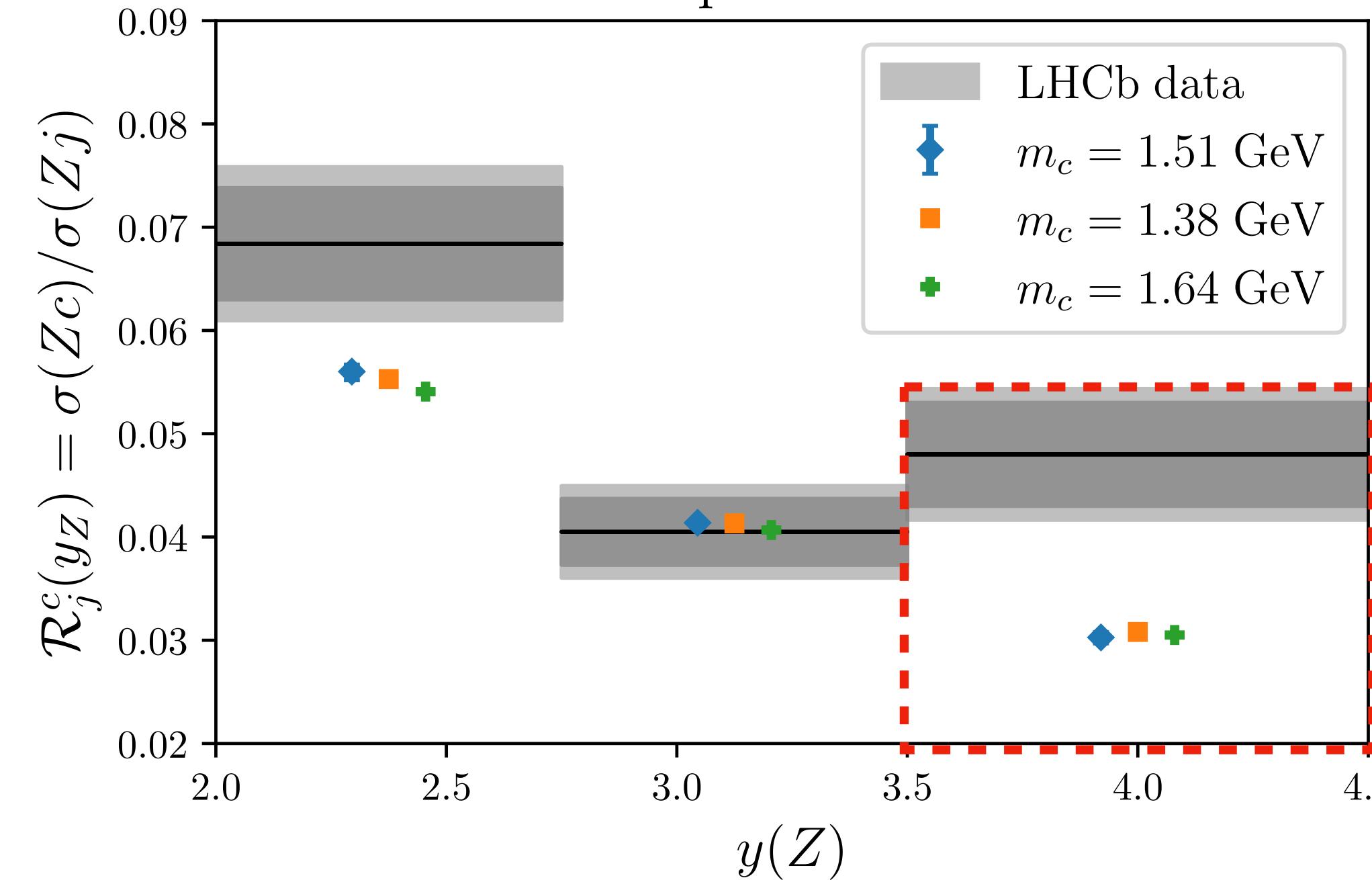
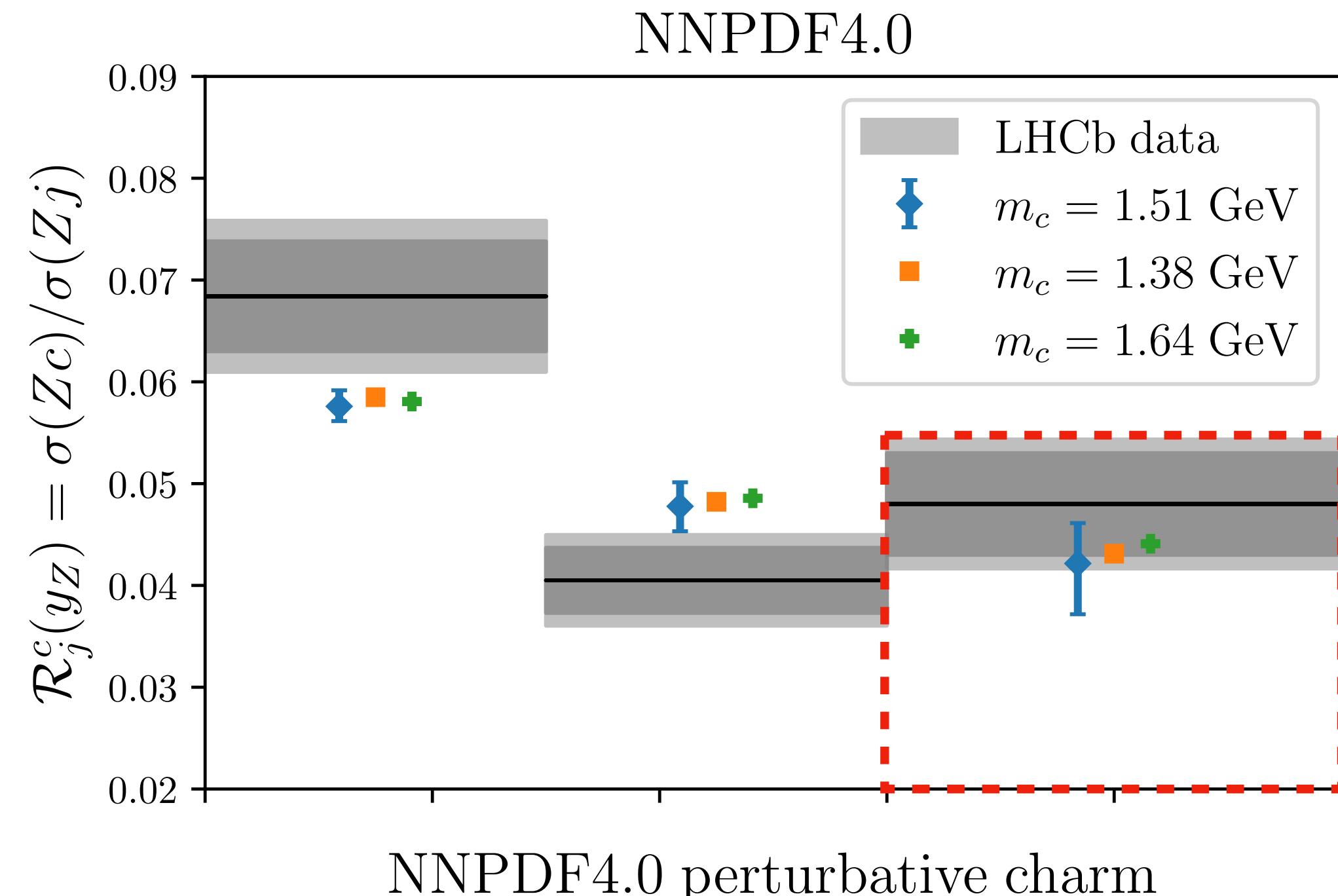
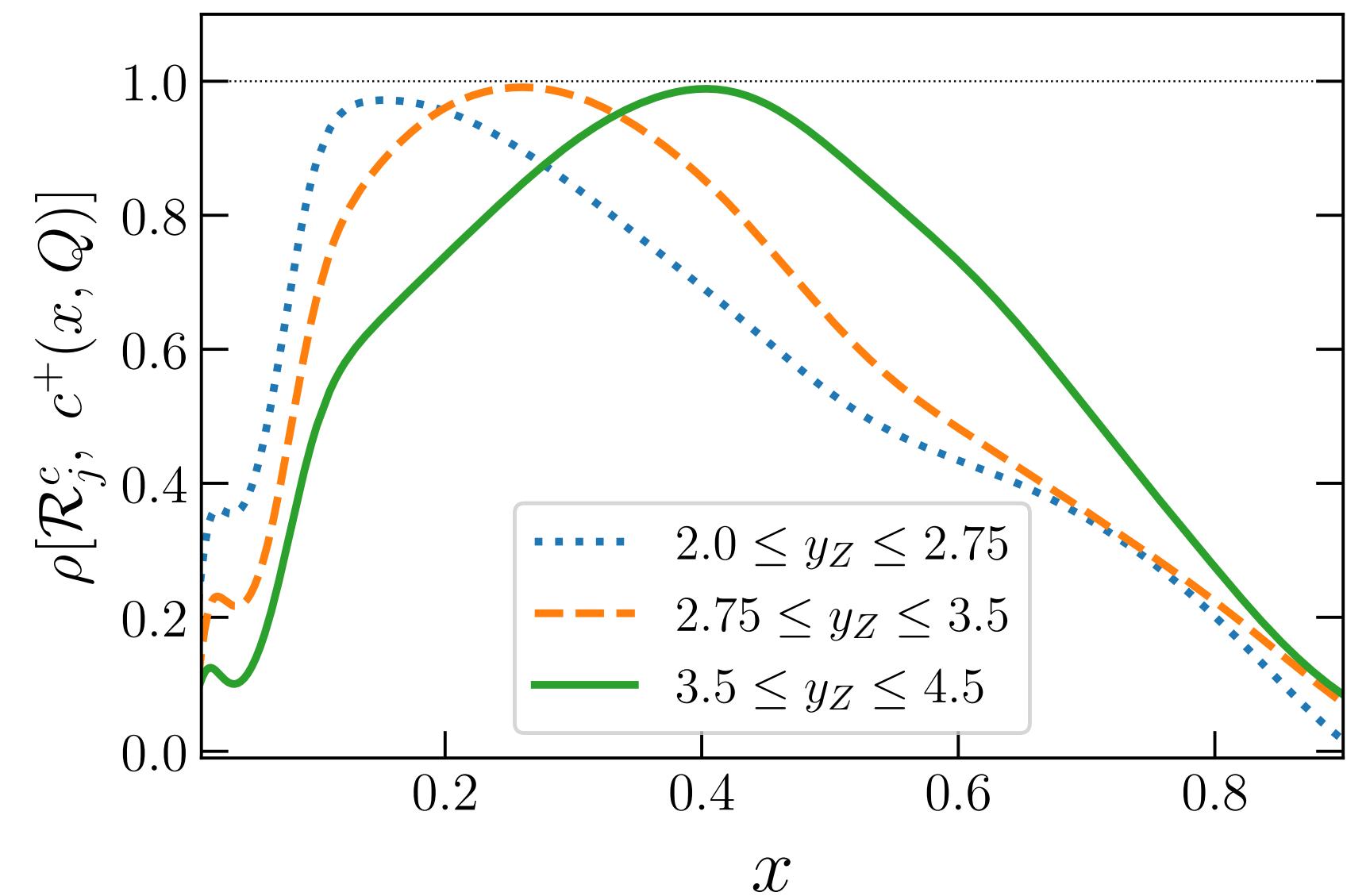
$y(Z)$	$\mathcal{R}_j^c (\%)$
2.00–2.75	$6.84 \pm 0.54 \pm 0.51$
2.75–3.50	$4.05 \pm 0.32 \pm 0.31$
3.50–4.50	$4.80 \pm 0.50 \pm 0.39$
2.00–4.50	$4.98 \pm 0.25 \pm 0.35$
	Stat Syst

Impact on LHC observables

Z+charm production @ LHCb

Compare data to *Powheg* @ NLO+PS [[arxiv: 1009.5594](#)]

- Better agreement is found with the NNPDF4.0 baseline especially in the **forward region**
- Predictions are also stable upon charm mass variation
- NNLO corrections not taken into account yet
- High ***correlation*** with the charm PDF and LHCb observable:



The Intrinsic charm

Our current best estimation

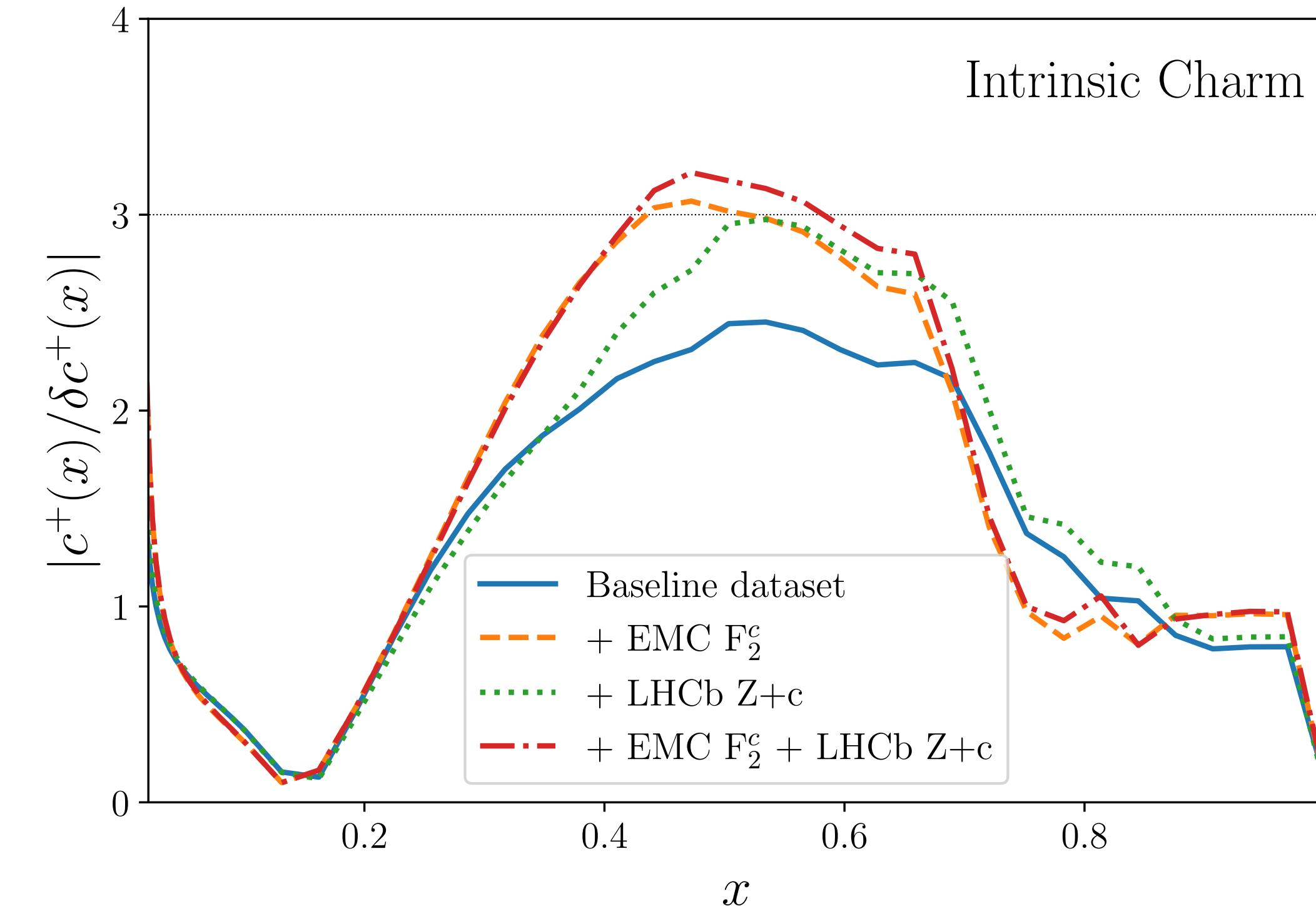
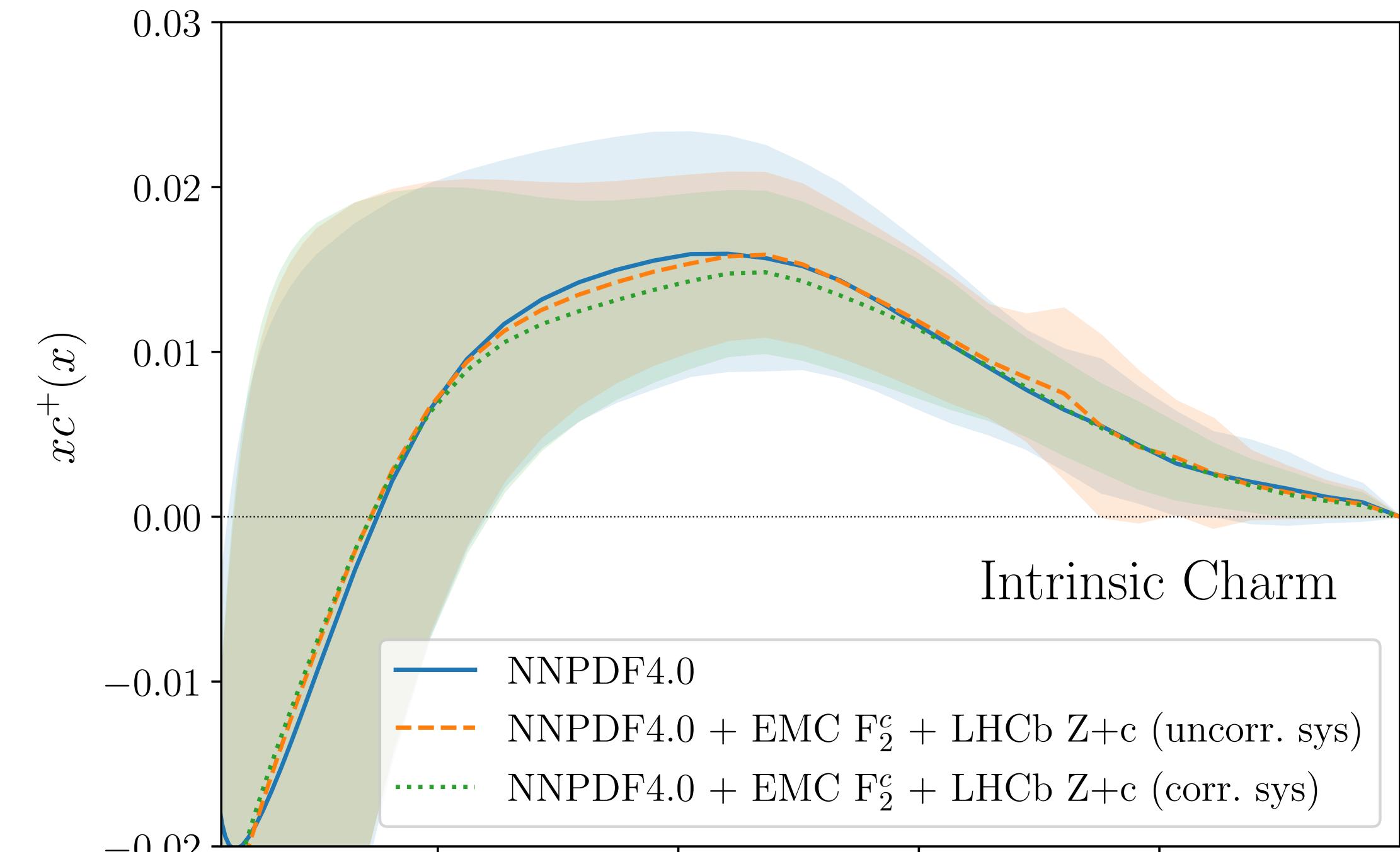
To achieve the best sensitivity on the intrinsic charm, we add the LHCb results to the NNPDF4.0 baseline.

We compute:

- **local significance:**

- **momentum fraction:** $[c] = \int_0^1 xc^+(x, Q^2)dx$

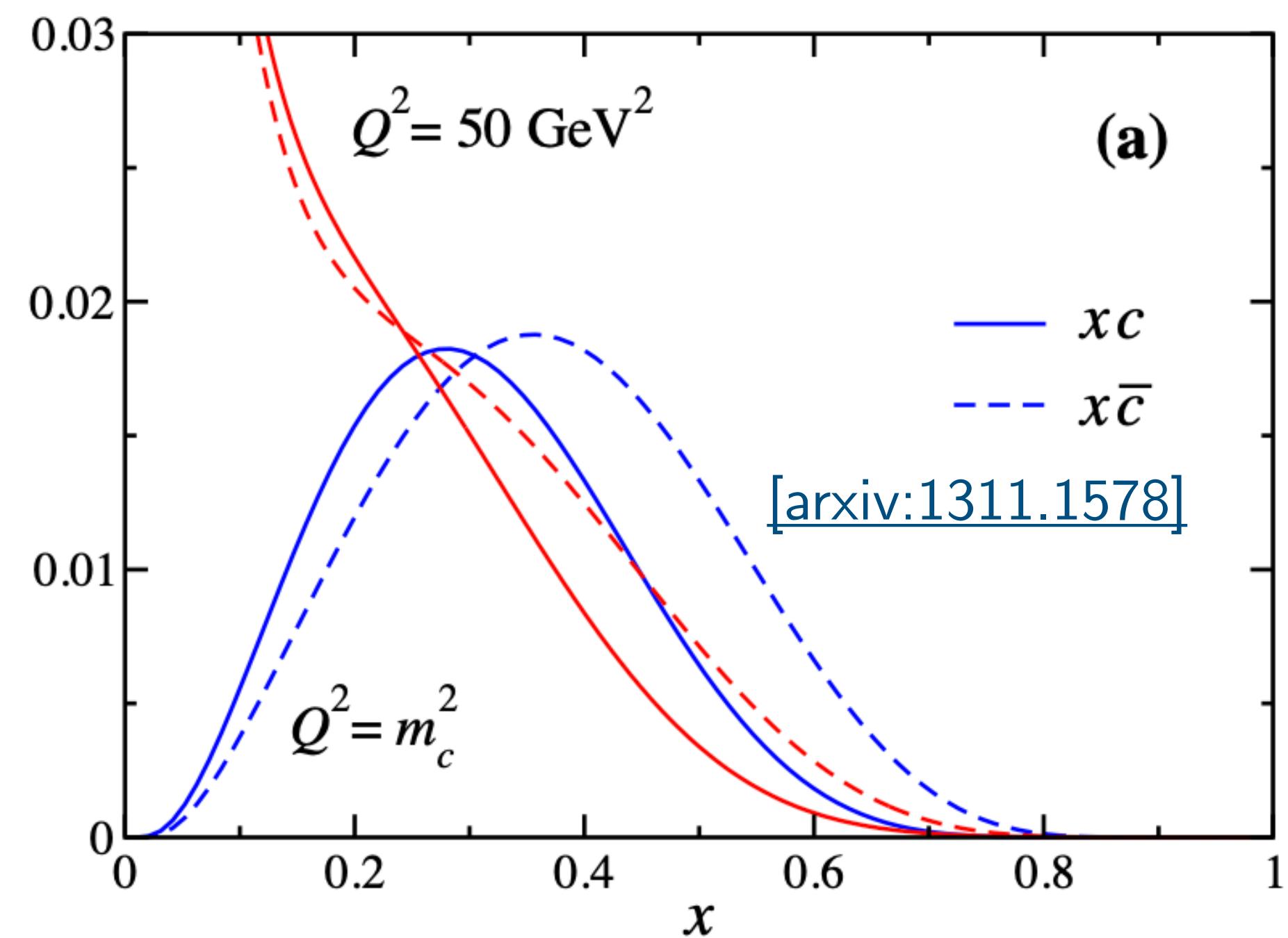
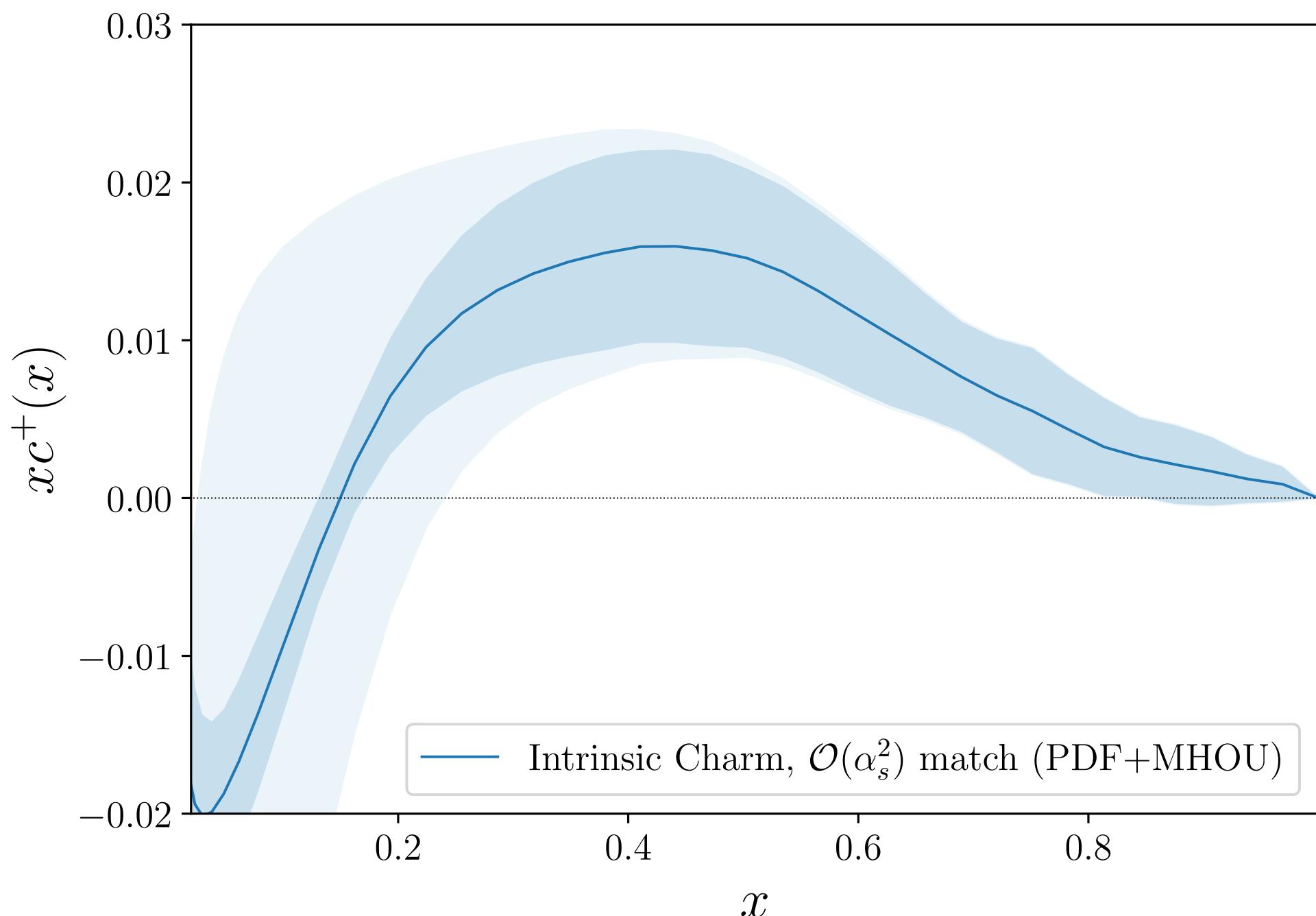
m_c	Dataset	$[c](Q)$ (%)
1.51 GeV	Baseline	$0.62 \pm 0.28_{\text{pdf}} \pm 0.54_{\text{mhou}}$
1.51 GeV	Baseline+EMC	$0.60 \pm 0.18_{\text{pdf}} \pm 0.54_{\text{mhou}}$
1.51 GeV	Baseline+EMC+LHCb Zc	$0.60 \pm 0.17_{\text{pdf}} \pm 0.59_{\text{mhou}}$
1.38 GeV	Baseline	$0.47 \pm 0.27_{\text{pdf}} \pm 0.62_{\text{mhou}}$
1.64 GeV	Baseline	$0.77 \pm 0.28_{\text{pdf}} \pm 0.48_{\text{mhou}}$



Summary and outlook

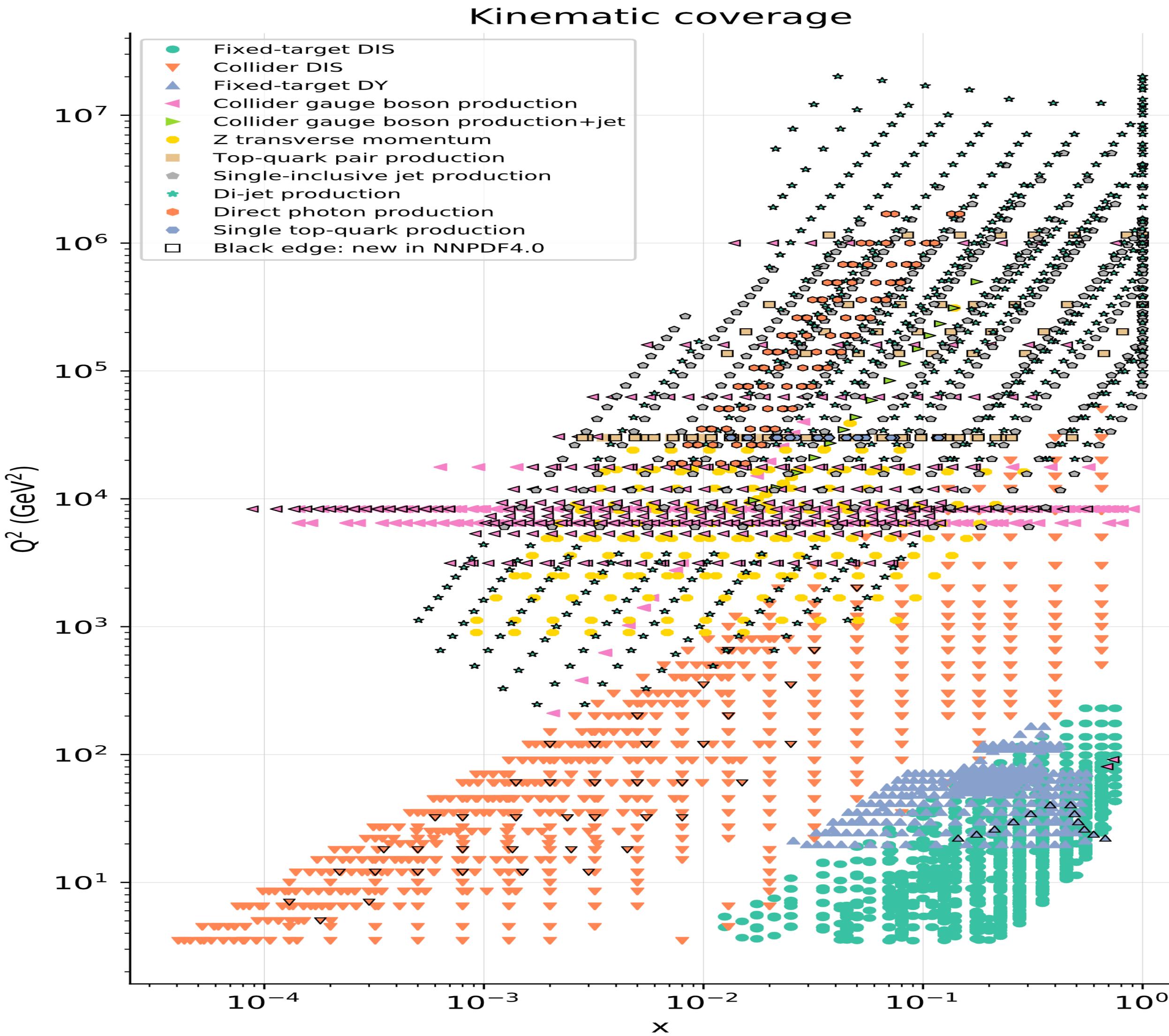
- Evidence of a non zero intrinsic charm c^+ in $n_f = 3$, carrying a momentum fraction total within 1%.
- Our intrinsic charm is in agreement with most recent LHC results.
- Impact of the N³LO matching conditions is relevant.
Need to proper quantify MHOU and possibly move towards N³LO pdf fit.
- Try a fit with independent c^- parametrisation as suggested by the Meson/Baryon models.
- Possible validation by an independent PDFs study.

Thank you for the attention!



Backup slides

NNPDF4.0 [arxiv:2109.02653]



- Theoretical framework [[EPJ C79 \(2019\) 282](#); [EPJ C81 \(2021\) 37](#); [EPJC80 \(2020\) 1168](#)]
 - nuclear uncertainties for both deuteron and heavy nuclei included by default
 - NNLO charm-quark massive corrections implemented
 - EW corrections not included to ensure consistency with data, but carefully checked
- Implementation of PDF properties [[JHEP 11 \(2020\) 129](#)]
 - extended positivity constraints for light quark/antiquark and gluon PDFs
 - extended integrability constraints of non-singlet light quark PDF combinations
- PDF parametrisation and optimisation [[EPJ C79 \(2019\) 676](#)]
 - single neural network to parametrise eight independent PDF combinations
 - check of the independence of the results from the chosen parametrisation basis
 - new optimisation strategy based on gradient descent rather than genetic algorithms
 - scan of the hyperparameter space to find the optimal minimisation settings
- Statistical validation of PDF uncertainties [[Acta Phys.Polon. B52 \(2021\) 243](#)]
 - (multi-)closure tests to validate PDF uncertainties in the data region
 - future tests to check the sensibleness of PDF uncertainties in extrapolation regions

From 4FNS to 3FNS

The matching conditions

$$\mathbf{A}^{(n_f)}(\mu_h^2) = \mathbf{I} + a_s^{(n_f+1)}(\mu_h^2)\mathbf{A}^{(n_f),(1)} + a_s^{(n_f+1),2}(\mu_h^2)\mathbf{A}^{(n_f),(2)} + a_s^{(n_f+1),3}(\mu_h^2)\mathbf{A}^{(n_f),(3)} + \mathcal{O}(a_s^4)$$

NLO

$$\mathbf{A}_{S,h^+}^{(n_f),(1)} = \begin{pmatrix} A_{gg,H}^{S,(1)} & 0 & A_{gH}^{S,(1)} \\ 0 & 0 & 0 \\ A_{Hg}^{S,(1)} & 0 & A_{HH}^{(1)} \end{pmatrix}$$

$$\mathbf{A}_{nsv,h^-}^{(n_f),(1)} = \begin{pmatrix} 0 & 0 \\ 0 & A_{HH}^{(1)} \end{pmatrix}$$

NNLO

$$\mathbf{A}_{S,h^+}^{(n_f),(2)} = \begin{pmatrix} A_{gg,H}^{S,(2)} & A_{gq,H}^{S,(2)} & 0 \\ 0 & A_{qq,H}^{ns,(2)} & 0 \\ A_{Hg}^{S,(2)} & A_{HQ}^{ps,(2)} & 0 \end{pmatrix}$$

$$\mathbf{A}_{nsv,h^-}^{(n_f),(2)} = \begin{pmatrix} A_{qq,H}^{ns,(2)} & 0 \\ 0 & 0 \end{pmatrix}$$

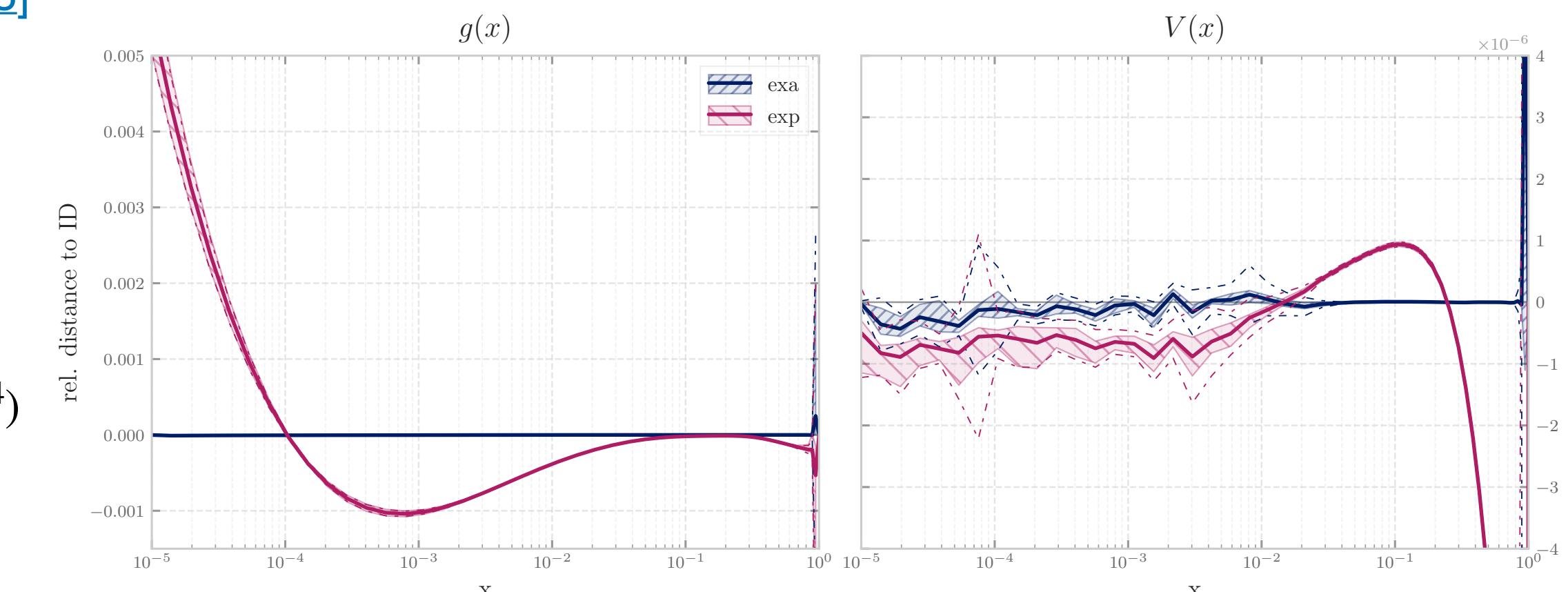
N³LO

$$\mathbf{A}_{S,h^+}^{(n_f),(3)} = \begin{pmatrix} A_{gg,H}^{S,(3)} & A_{gq,H}^{S,(3)} & 0 \\ A_{qg,H}^{S,(3)} & A_{qq,H}^{ns,(3)} + A_{qq,H}^{ps,(3)} & 0 \\ A_{Hg}^{S,(3)} & A_{HQ}^{ps,(3)} & 0 \end{pmatrix}$$

$$\mathbf{A}_{nsv,h^-}^{(n_f),(3)} = \begin{pmatrix} A_{qq,H}^{ns,(3)} & 0 \\ 0 & 0 \end{pmatrix}$$

[Eur.Phys.J.C 1 (1998) 301-320, Phys.Lett.B 754 (2016) 49-58]

[Nucl.Phys.B 820 (2009) 417-482 et al.]

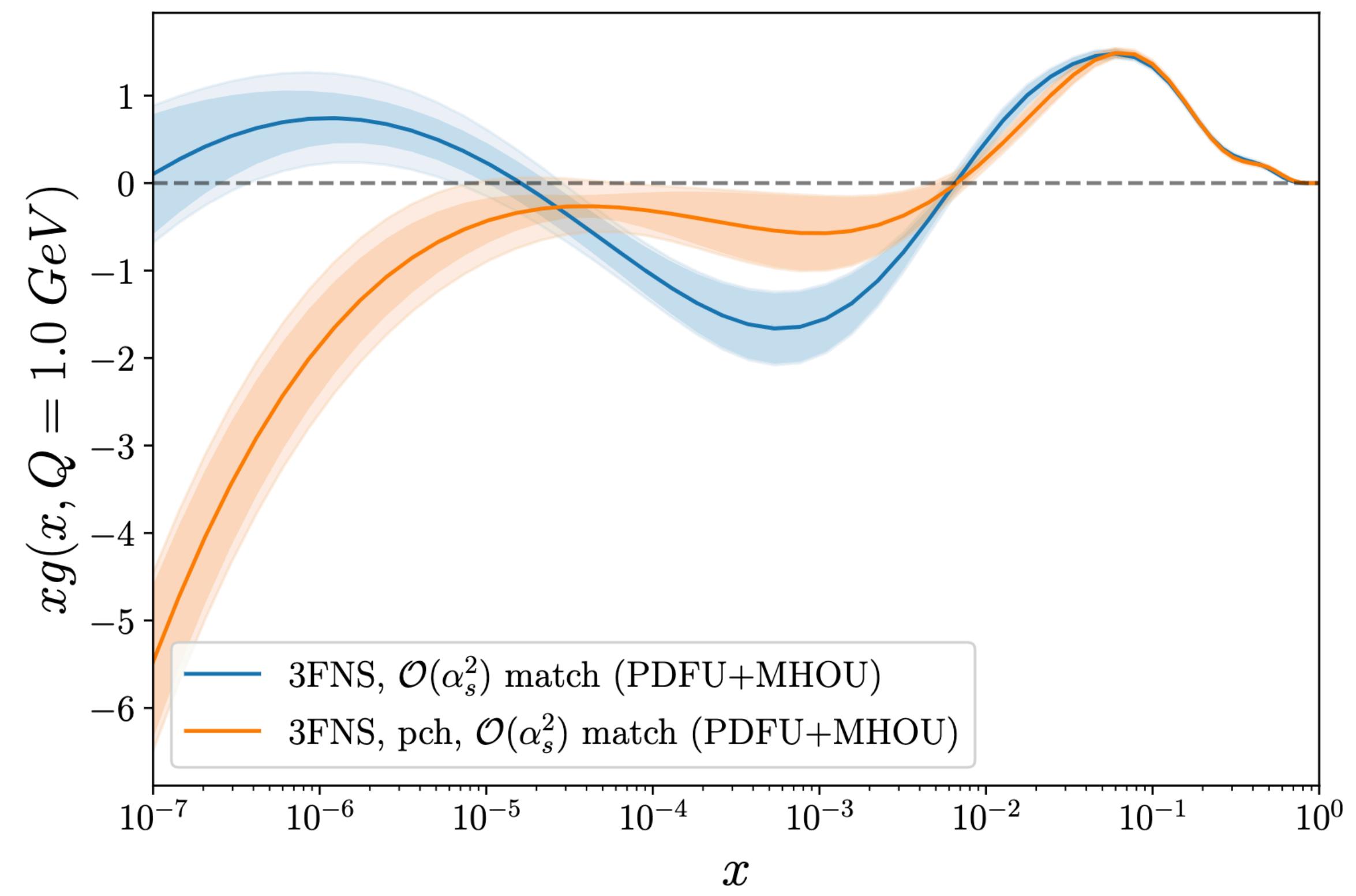


Inversion can be computed exactly or expanding in α_s :

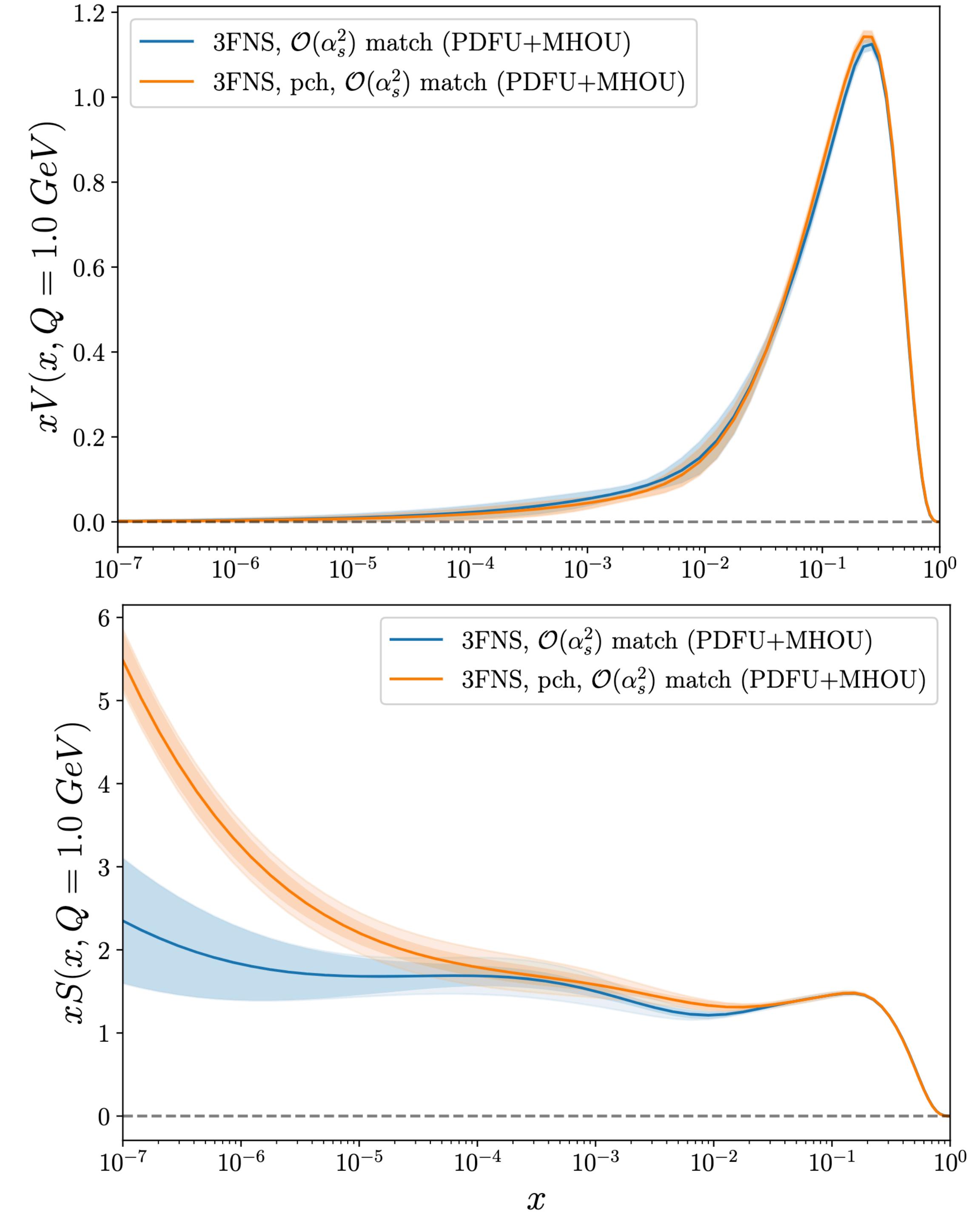
$$\mathbf{A}_{exp}^{-1}(\mu_h^2) = \mathbf{I} - a_s(\mu_h^2)\mathbf{A}^{(1)} + a_s^2(\mu_h^2)\left[\mathbf{A}^{(2)} - (\mathbf{A}^{(1)})^2\right] + a_s^3(\mu_h^2)\left[-\mathbf{A}^{(3)} + 2\mathbf{A}^{(1)}\mathbf{A}^{(2)} - (\mathbf{A}^{(1)})^3\right] + O(a_s^4)$$

PDFs in 3FNS

- Evolution range: $Q = 1.65 \text{ GeV} \rightarrow 1.0 \text{ GeV}$
- MHOU estimated from different matching order



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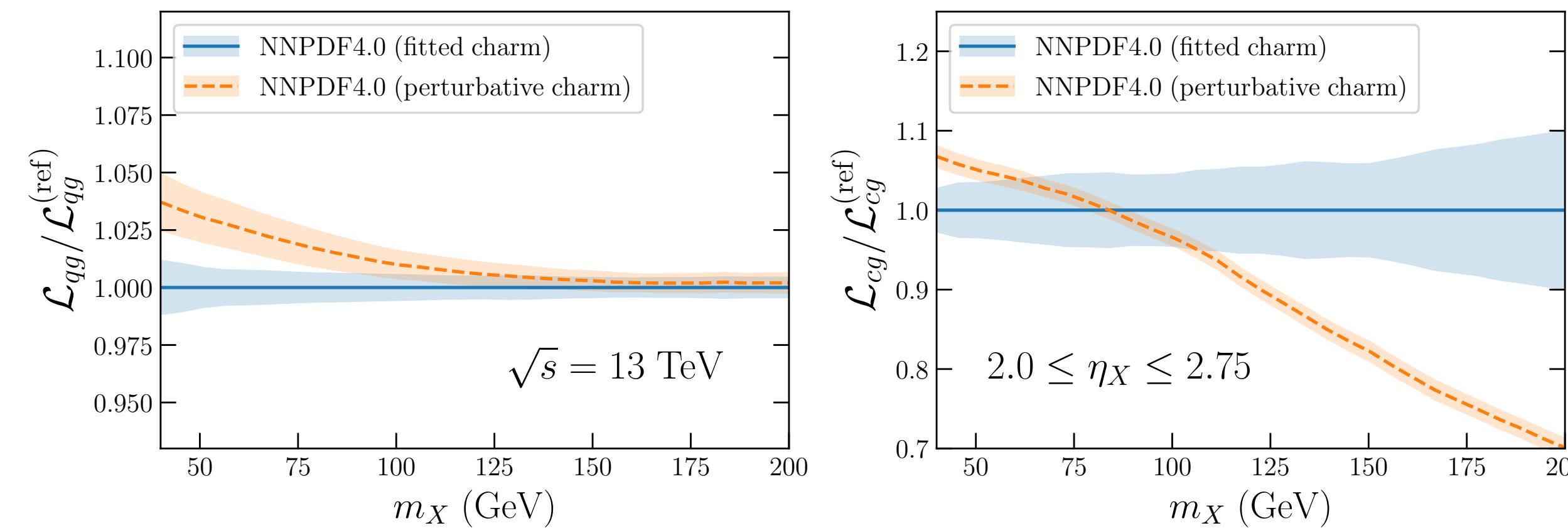
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Impact on LHC observables

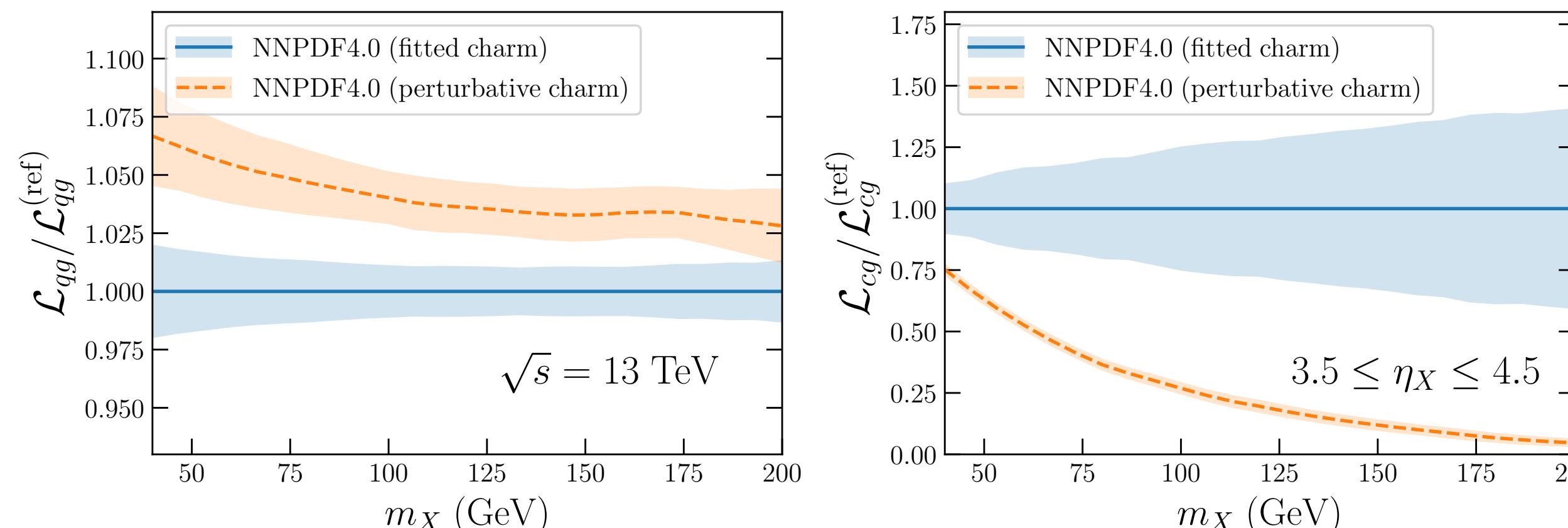
Partonic luminosities

To see where the differences between fitted and perturbative charm can be evident you can look at partonic lumi of: $pp \rightarrow X$

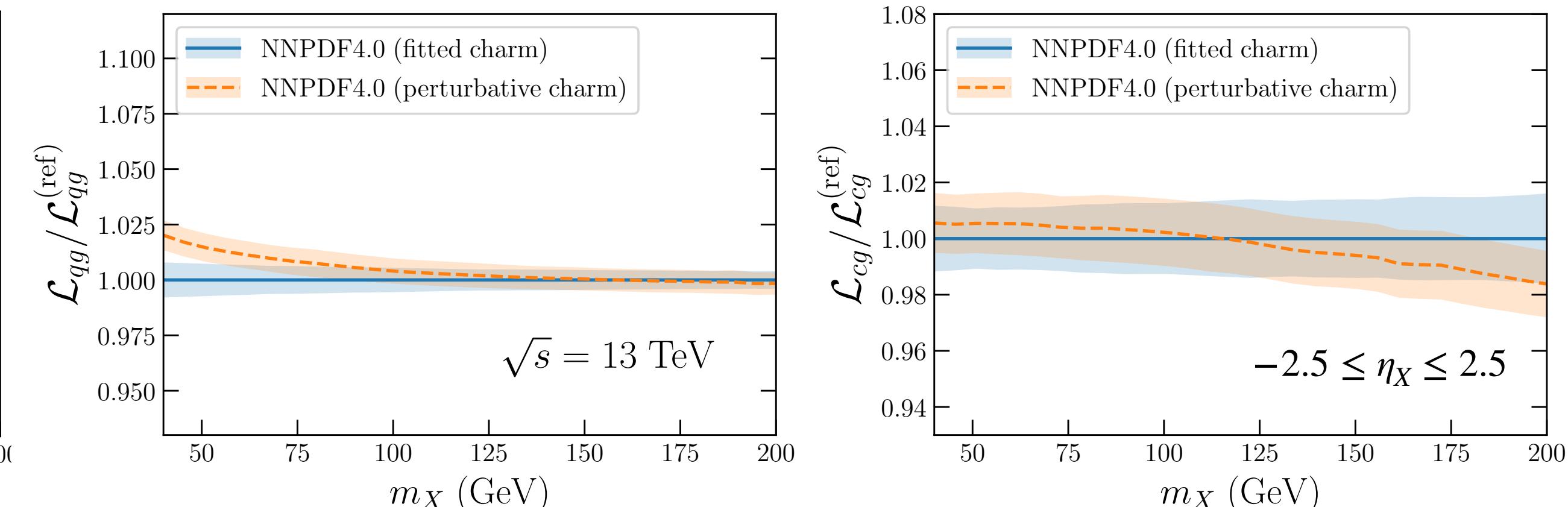
Central region LHCb



Forward region LHCb



Central region ATLAS-CMS



$$\mathcal{L}_{ab} = \frac{1}{s} \int_{\frac{m_X^2}{s}}^1 \frac{dx}{x} f_a(x, m_X^2) f_b(x, m_X^2) \theta(y_X - y_{min}) \theta(y_{max} - y_X)$$

$$\mathcal{L}_{cg} = \mathcal{L}_{cg} + \mathcal{L}_{\bar{c}g}$$

$$\mathcal{L}_{qg} = \sum_{i=1}^{n_f} \mathcal{L}_{qig} + \mathcal{L}_{\bar{q}ig}$$