

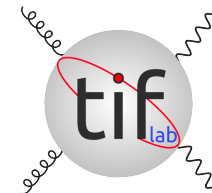


CAN WE TRUST MACHINE LEARNING? PDFS AS A CASE STUDY

STEFANO FORTE
UNIVERSITÀ DI MILANO & INFN



UNIVERSITÀ DEGLI STUDI DI MILANO
DIPARTIMENTO DI FISICA



PRECISION QCD FOR THE EIC

STONY BROOK, SEPTEMBER 19, 2023



THE PROBLEM GENERALIZATION

Machine learning

Contents [hide]

[Article](#) [Talk](#)

From Wikipedia, the free encyclopedia

1)

Generalization [\[edit\]](#)

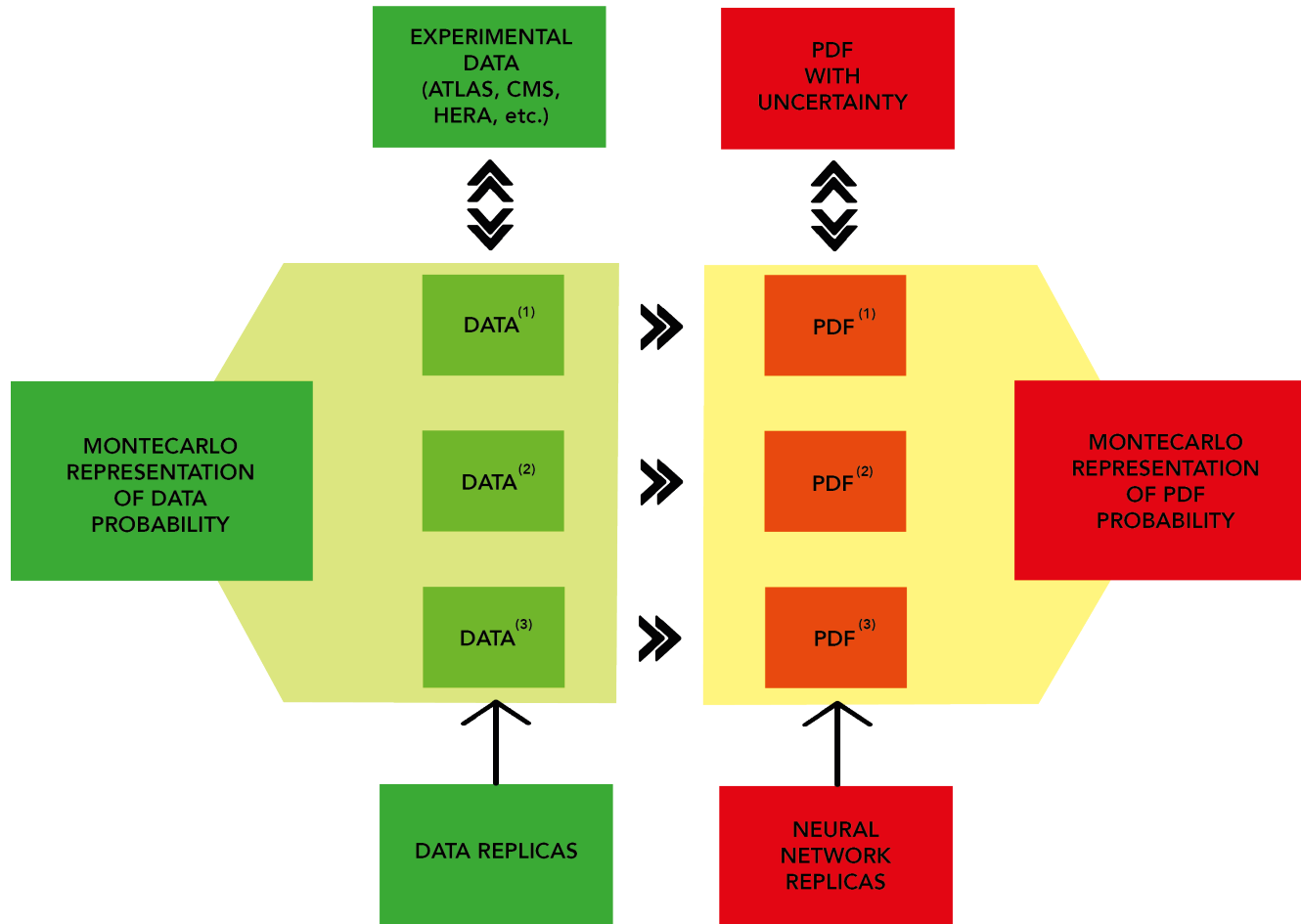
The difference between optimization and machine learning arises from the goal of **generalization**: while optimization algorithms can minimize the loss on a training set, machine learning is concerned with minimizing the loss on unseen samples. Characterizing the generalization of various learning algorithms is an active topic of current research, especially for **deep learning** algorithms.

- CAN WE **TEST IT?** \Rightarrow **VALIDATION**
- CAN WE **UNDERSTAND IT?** \Rightarrow **EXPLANATION (XML)**

PDF/NNPDF RECAP SEQUENCE

THE FUNCTIONAL MONTE CARLO

REPLICA SAMPLE OF FUNCTIONS \Leftrightarrow PROBABILITY DENSITY IN FUNCTION SPACE
 KNOWLEDGE OF LIKELIHOOD SHAPE (FUNCTIONAL FORM) NOT NECESSARY

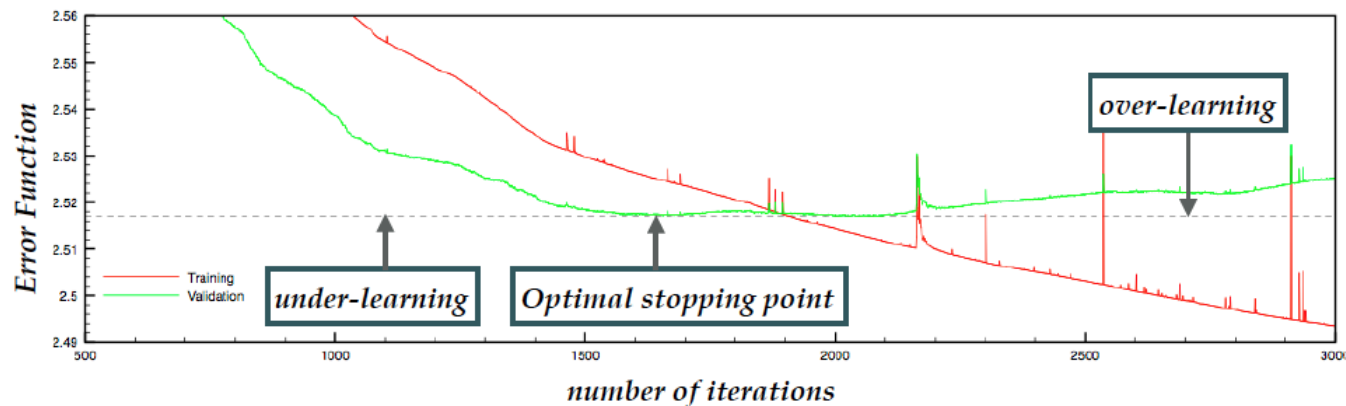
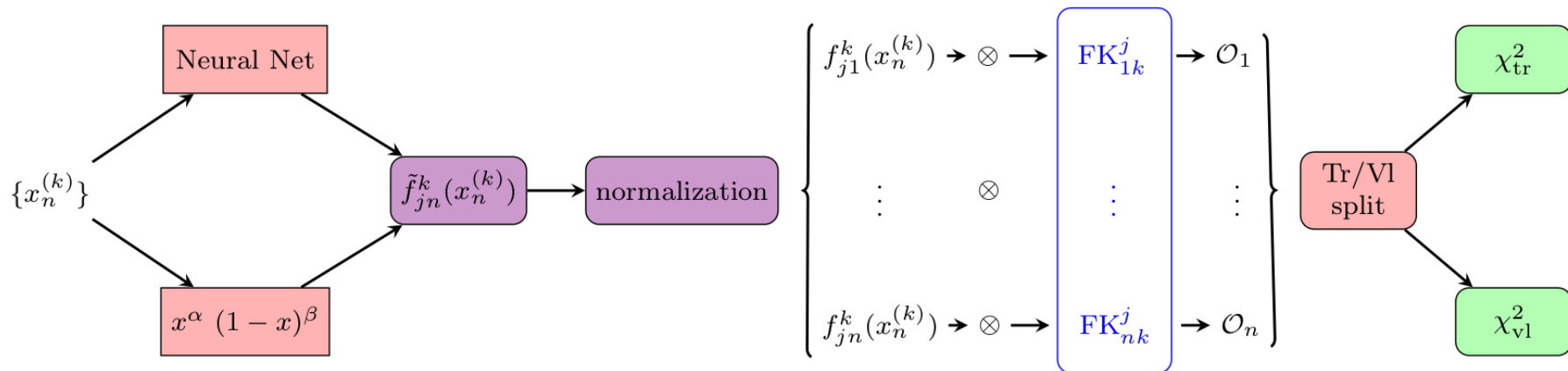


FINAL PDF SET: $f_i^{(a)}(x, \mu)$;

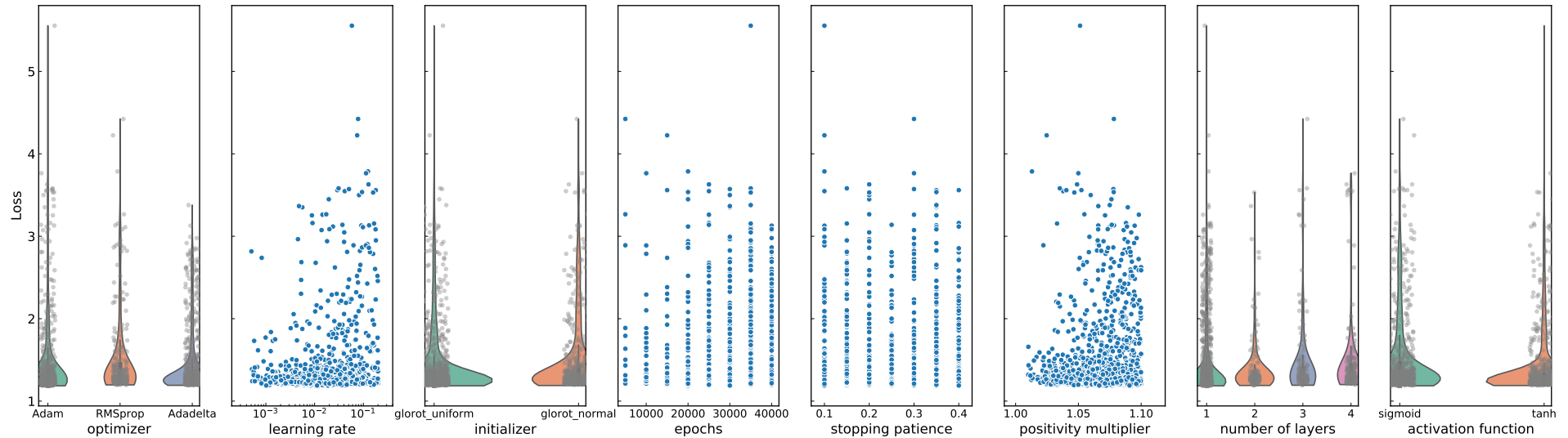
$i = \text{up, antiup, down, antidown, strange, antistrange, charm, gluon}; j = 1, 2, \dots, N_{\text{rep}}$

MINIMIZATION AND CROSS-VALIDATION

- NEURAL NET PARAMETERS DETERMINED BY χ^2 MINIMIZATION THROUGH GRADIENT DESCENT
- RANDOM TRAINING-VALIDATION SPLIT, χ^2 TO TRAINING DATA REPLICAS MINIMIZED
- TRAINING STOPS IF VALIDATION χ^2 GROWS FOR A WHILE (PATIENCE)
- LOWEST VALIDATION $\chi^2 \Rightarrow$ OPTIMAL FIT



FITTING THE METHODOLOGY HYPEROPTIMIZATION

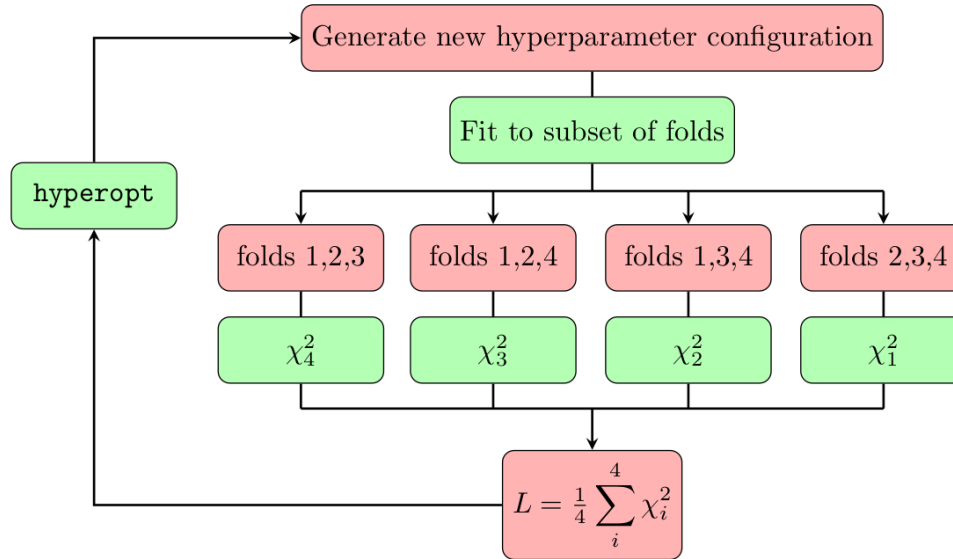


HYPEROPT PARAMETERS

NEURAL NETWORK	FIT OPTIONS
NUMBER OF LAYERS (*)	OPTIMIZER (*)
SIZE OF EACH LAYER	INITIAL LEARNING RATE (*)
DROPOUT	MAXIMUM NUMBER OF EPOCHS (*)
ACTIVATION FUNCTIONS (*)	STOPPING PATIENCE (*)
INITIALIZATION FUNCTIONS (*)	POSITIVITY MULTIPLIER (*)

- **SCAN** PARAMETER SPACE
- **OPTIMIZE** FIGURE OF MERIT: **K-FOLDING** LOSS

K-FOLDING



- EACH FOLD REPRODUCES FEATURES OF FULL DATASET
- LOSS: AVERAGE χ^2 OF NON-FITTED FOLDS
- OVERFITTING REMOVED \Rightarrow CORRECT GENERALIZATION

Fold 1		
CHORUS σ_{CC}^e	HERA I+II inc NC e^+p 920 GeV	BCDMS p
LHCb Z 940 pb	ATLAS W, Z 7 TeV 2010	CMS Z pp 8 TeV (p_T^H, y_H)
DY E605 σ_{DY}^p	CMS Drell-Yan 2D 7 TeV 2011	CMS 3D dijets 8 TeV
ATLAS single- t y (normalised)	ATLAS single top R_t 7 TeV	CMS $t\bar{t}$ rapidity $y_{t\bar{t}}$
CMS single top R_t 8 TeV		

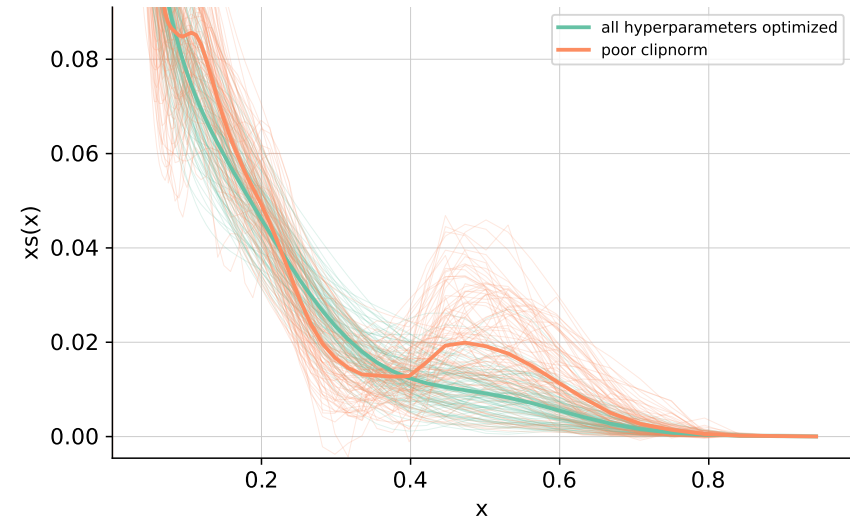
Fold 2		
HERA I+II inc CC e^-p	HERA I+II inc NC e^+p 460 GeV	HERA comb. σ_{bb}^{had}
NuTeV p	NuTeV σ_e^e	LHCb $Z \rightarrow ee$ 2 fb
CMS W asymmetry 840 pb	ATLAS Z pp 8 TeV (p_T^H, M_{Hl})	D0 $W \rightarrow \mu\nu$ asymmetry
DY E886 σ_{DY}^p	ATLAS direct photon 13 TeV	ATLAS dijets 7 TeV, $R=0.6$
ATLAS single antitop y (normalised)	CMS $\sigma_{t\bar{t}}^e$	CMS single top $\sigma_t + \sigma_{\bar{t}}$ 7 TeV

Fold 3		
HERA I+II inc CC e^+p	HERA I+II inc NC e^+p 575 GeV	NMC d/p
NuTeV σ_e^e	LHCb $W, Z \rightarrow \mu$ 7 TeV	LHCb $Z \rightarrow ee$
ATLAS W, Z 7 TeV 2011 Central selection	ATLAS W^+ +jet 8 TeV	ATLAS HM DY 7 TeV
CMS W asymmetry 4.7 fb	DYE 866 $\sigma_{DY}^d / \sigma_{DY}^p$	CDF Z rapidity (new)
ATLAS $\sigma_{t\bar{t}}^e$	ATLAS single top y_t (normalised)	CMS $\sigma_{t\bar{t}}^{had}$ 5 TeV
CMS $t\bar{t}$ double diff. $(m_{t\bar{t}}, y_t)$		

Fold 4		
CHORUS σ_{CC}^e	HERA I+II inc NC e^+p 820 GeV	LHCb $W, Z \rightarrow \mu$ 8 TeV
LHCb $Z \rightarrow \mu\mu$	ATLAS W, Z 7 TeV 2011 Fwd	ATLAS W^- +jet 8 TeV
ATLAS low-mass DY 2011	ATLAS Z pp 8 TeV (p_T^H, y_H)	CMS W rapidity 8 TeV
D0 Z rapidity	CMS dijets 7 TeV	ATLAS single top y_t (normalised)
ATLAS single top R_t 13 TeV	CMS single top R_t 13 TeV	

K-FOLDING VS NO K-FOLDING

s at 1.7 GeV

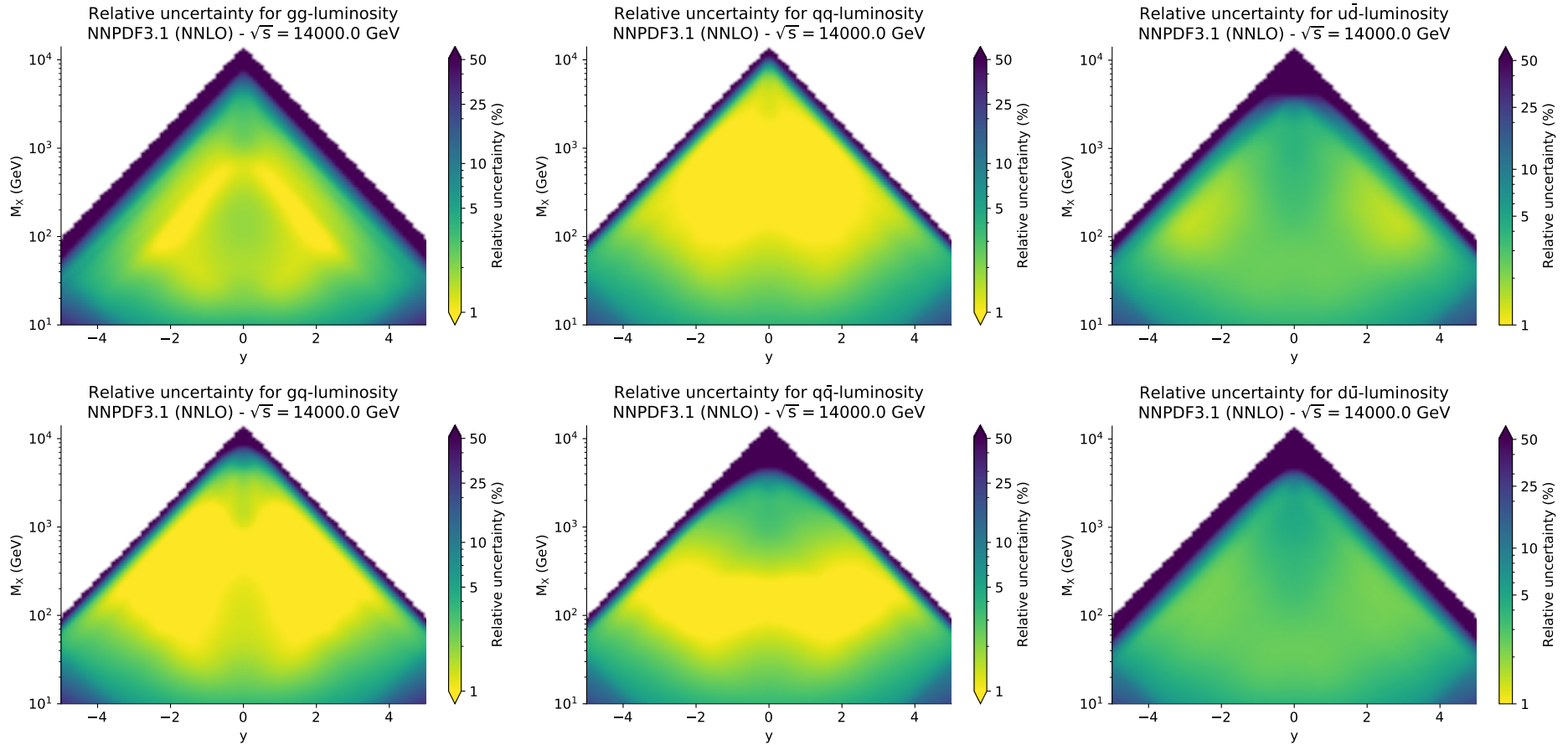


UNCERTAINTIES 2016

GLUON

SINGLET

FLAVORS



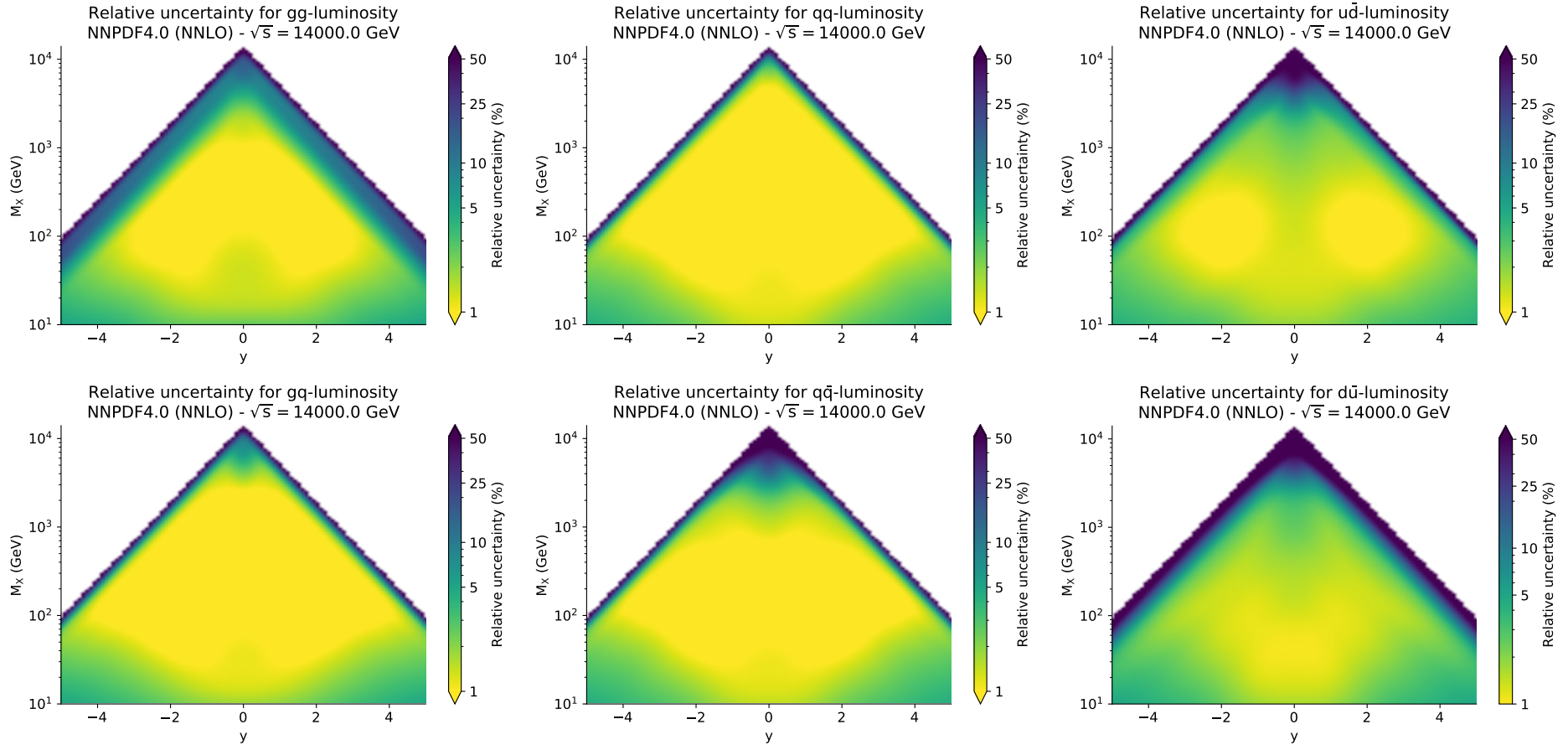
- TYPICAL UNCERTAINTIES IN DATA REGION: SINGLET $\sim 3\%$, NONSINGLET $\sim 5\%$
- DATA REGION: $10^2 \lesssim M_X \lesssim 10^3$ TeV, $-2 \lesssim y \lesssim 2$

UNCERTAINTIES 2022

GLUON

SINGLET

FLAVORS

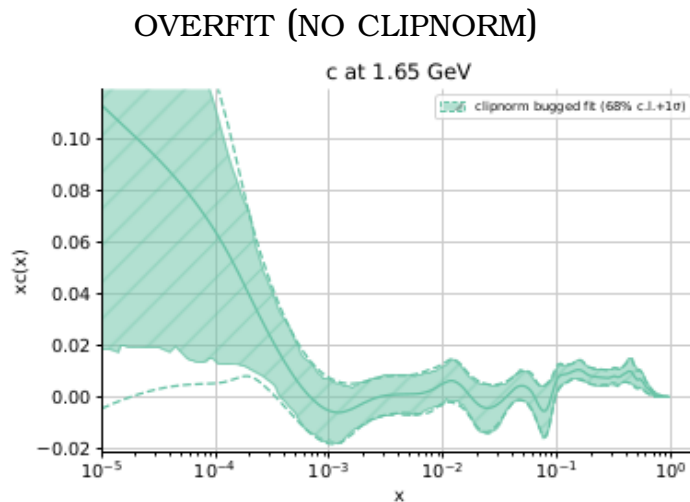


- TYPICAL UNCERTAINTIES IN DATA REGION: SINGLET $\sim 1\%$, NONSINGLET $\sim 2 - 3\%$
- DATA REGION: $10 \lesssim M_X \lesssim 3 \cdot 10^3$ TEV, $-4 \lesssim y \lesssim 4$

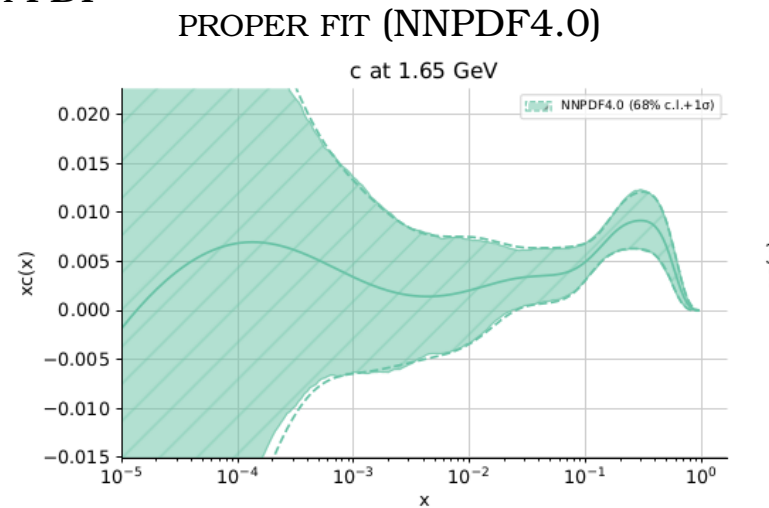
ONLINE VALIDATION: OVERFITTING METRIC

- RECOMPUTE VALIDATION χ_{val}^2 FOR ALL DATA REPLICAS
 - KEEPING SAME TRAINING-VALIDATION SPLIT
 - BUT DIFFERENT FLUCTUATED VALIDATION DATA
- COMPUTE AVERAGE OVER REPLICAS $\langle \chi_{\text{val}}^2 \rangle$ & DETERMINE DIFFERENCE TO STANDARD VALIDATION χ_{val}^2
OVERFITNESS: $\mathcal{R}_O = \chi_{\text{val}}^2 - \langle \chi_{\text{val}}^2 \rangle$
- NEGATIVE OVERFITNESS $\mathcal{R}_O \Rightarrow$ OVERFIT

CHARM PDF



$$\mathcal{R}_O = -0.024 \pm 0.012$$



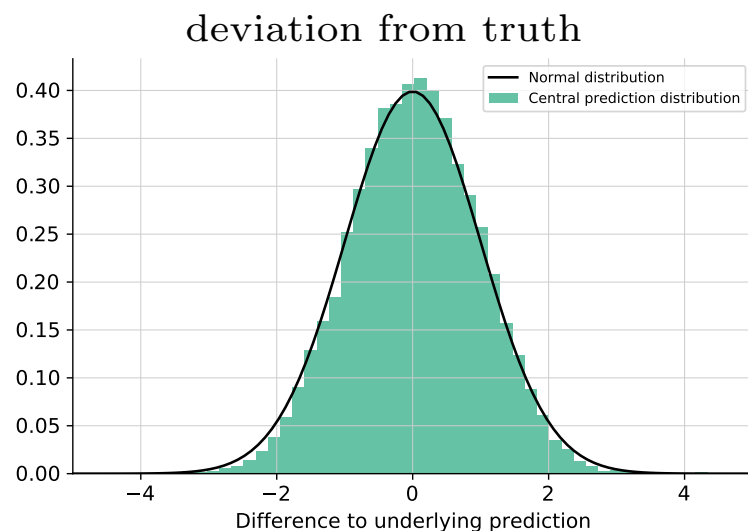
$$\mathcal{R}_O = -0.001 \pm 0.013$$

OFFLINE VALIDATION: CLOSURE TESTS

FAITHFUL UNCERTAINTIES IN DATA REGION?

- ASSUME “TRUE” UNDERLYING PDF \Rightarrow E.G. SOME RANDOM PDF REPLICA
- GENERATE DATA DISTRIBUTED ACCORDING TO EXPERIMENTAL COVARIANCE MATRIX
- RUN WHOLE METHDOLOGY ON THESE DATA
- DO STATISTICS ON “RUNS OF THE UNIVERSE”, POSSIBLE THANKS TO EFFICIENT METHDOLOGY: COMPARE TO TRUE VALUES OF OBSERVABLES (NOT FITTED)
 - BIAS/VARIANCE: MEAN SQUARE DEVIATION WR TO TRUTH VS UNCERTAINTY
 - IS TRUTH WITHIN ONE SIGMA 68% OF TIMES?

RESULTS



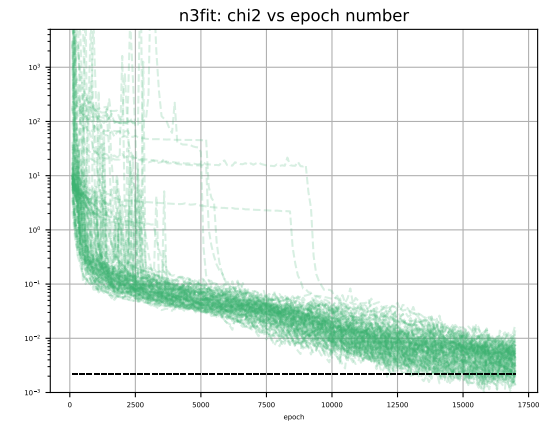
Dataset	$\sqrt{\text{bias}/\text{variance}}$	$\xi_{1\sigma}^{(\text{data})}$
DY	0.99 ± 0.08	0.69 ± 0.02
Top-pair	0.75 ± 0.06	0.75 ± 0.03
Jets	1.14 ± 0.05	0.63 ± 0.03
Dijets	0.99 ± 0.07	0.70 ± 0.03
Direct photon	0.71 ± 0.06	0.81 ± 0.03
Single top	0.87 ± 0.07	0.69 ± 0.04
Total	1.03 ± 0.05	0.68 ± 0.02

UNCERTAINTIES: TYPE AND SIZE

CLOSURE TEST RESULTS (NNPDF4.0)

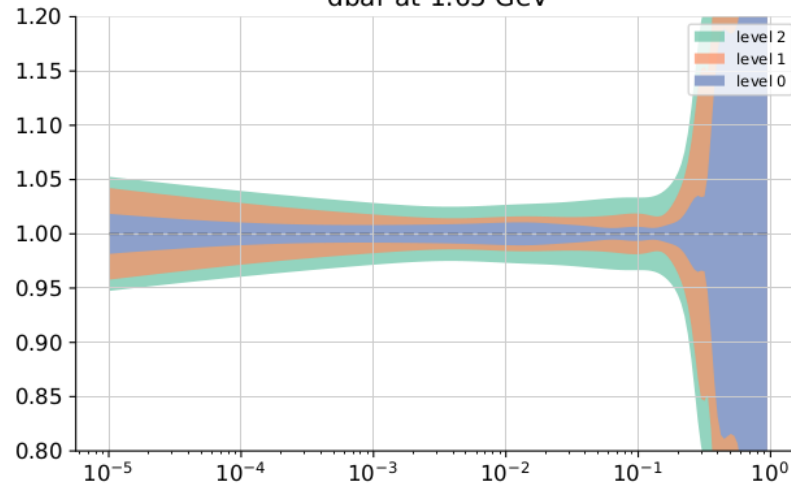
- **LEVEL 0** (TRUTH DATA) $\Rightarrow \chi^2 \approx 0$, YET **UNCERTAINTY NONZERO**
 \Rightarrow NEURAL NETS \Leftrightarrow **MANY FUNCTIONAL FORMS**
- **LEVEL 1** (RUNS OF UNIVERSE) \Rightarrow REPLICAS ALL FITTED TO SAME DATA, YET **UNCERTAINTY NONZERO**
 \Rightarrow **DITTO**
- **LEVEL 0, 1 AND 2 UNCERTAINTIES COMPARABLE IN SIZE**

LEVEL 0 χ^2 VS TRAINING

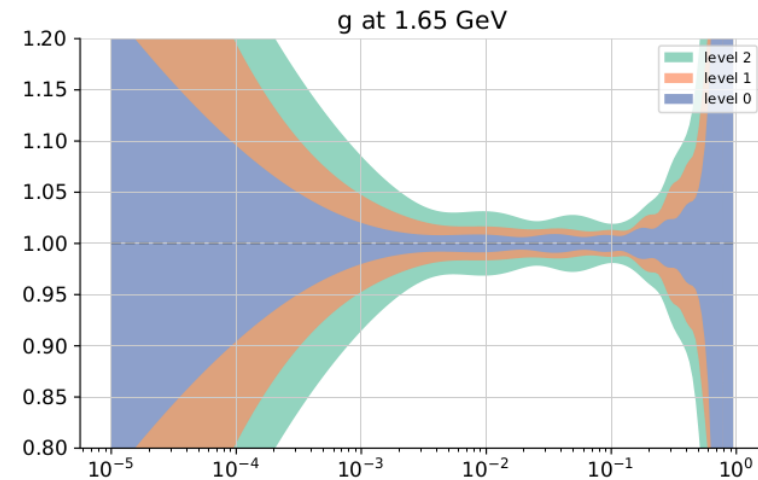


LEVEL 0/1/2 UNCERTAINTIES

ANTIDOWN
d \bar{b} at 1.65 GeV



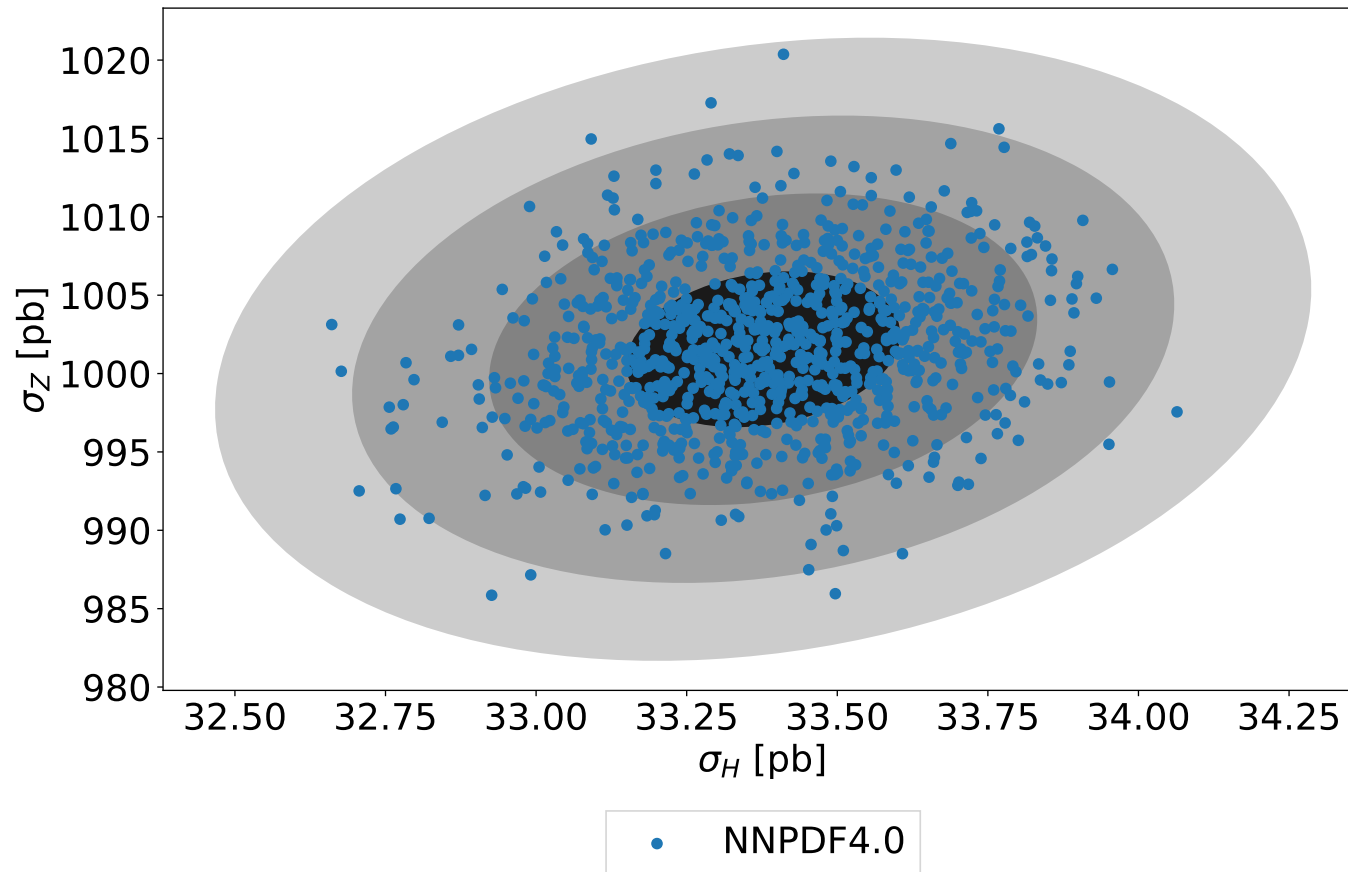
GLUON
g at 1.65 GeV



THE MC DISTRIBUTION: UNCERTAINTIES

DISTRIBUTION OF RESULTS HOW DOES IT LOOK LIKE?

- PLOT RESULTS IN (σ_H, σ_Z) PREDICTION SPACE \Rightarrow GAUSSIAN!
- DISTRIBUTION OF REPLICAS \Rightarrow OPTIMAL IMPORTANCE SAMPLING

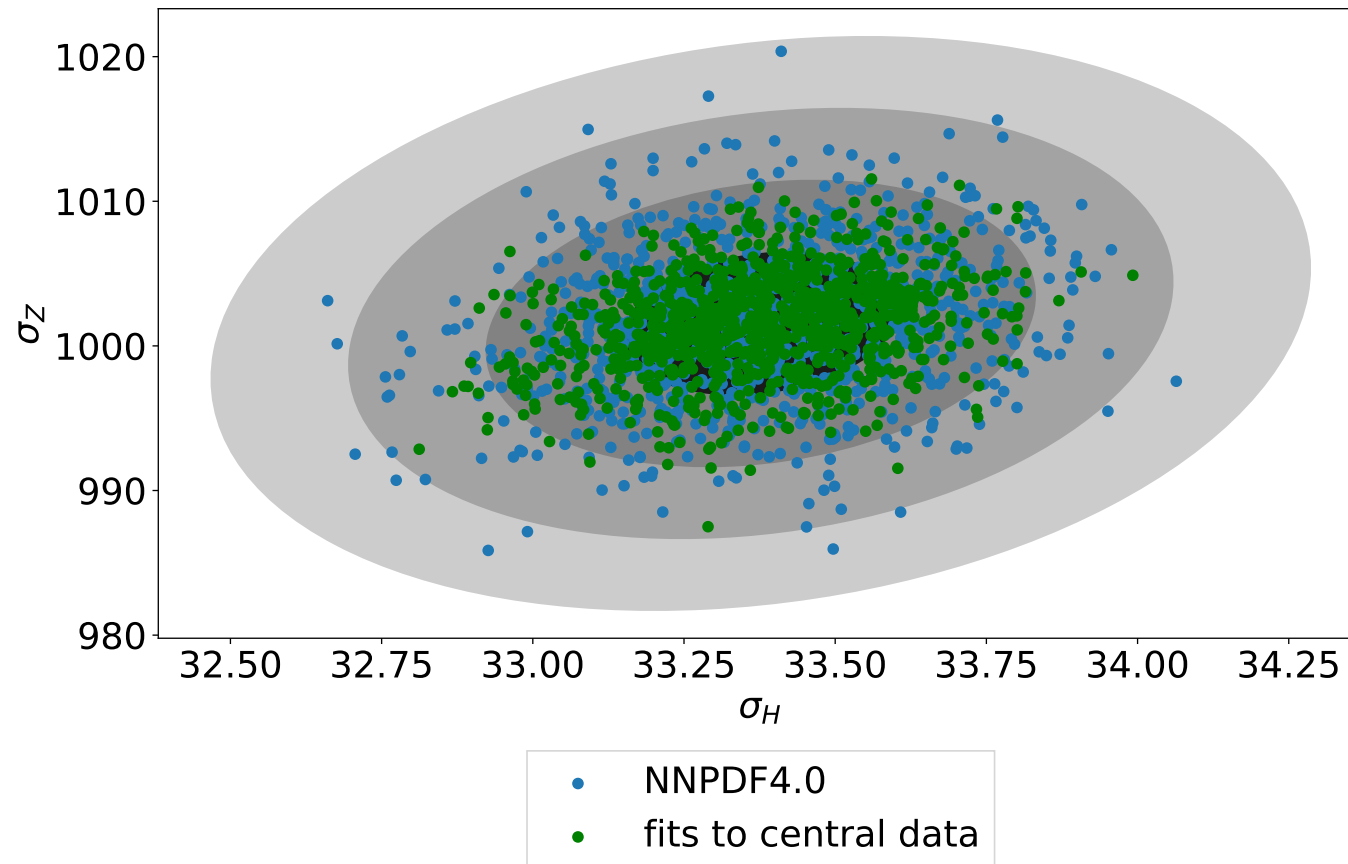


DISTRIBUTION OF REPLICAS DRIVEN BY

- DATA UNCERTAINTIES \Rightarrow DATA REPLICA FLUCTUATION
- INTERPOLATION, EXTRAPOLATION AND FUNCTIONAL UNCERTAINTIES \Rightarrow BEST FIT DEGENERACY

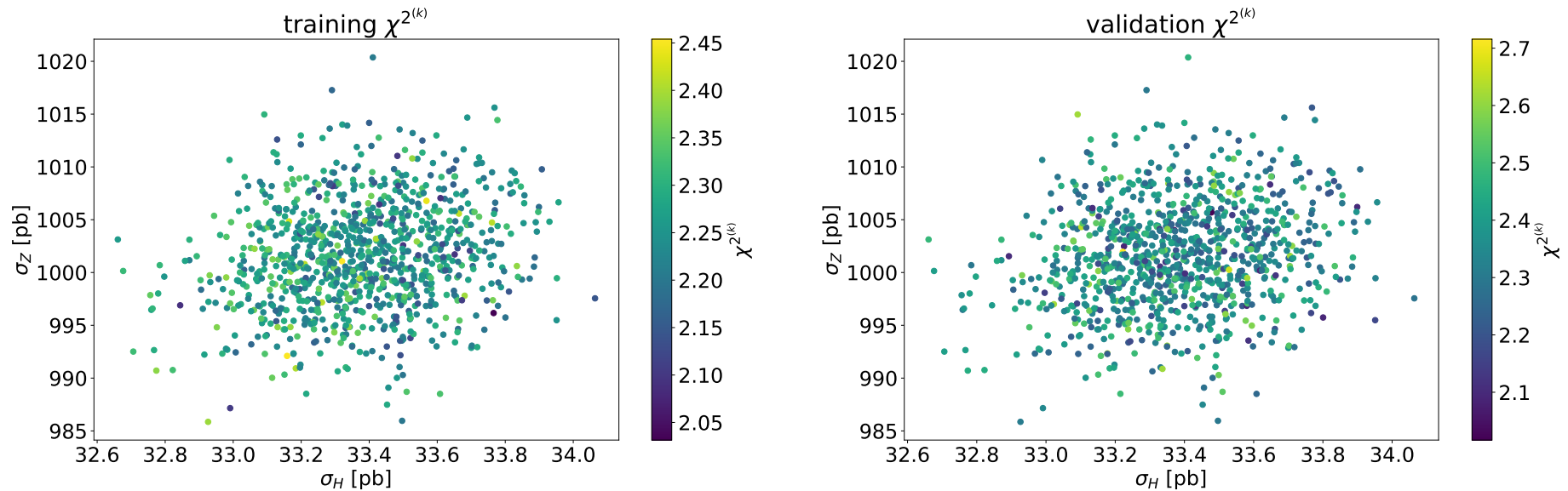
EXPLANATION THE REPLICA DISTRIBUTION

- REPLICA FLUCTUATION \Rightarrow DATA UNCERTAINTIES
- NO REPLICA FLUCTUATION \Rightarrow FIT DEGENERACY



EXPLANATION THE REPLICA DISTRIBUTION

ARE ALL FITS EQUALLY GOOD?



- COMPARE TRAINING AND VALIDATION χ^2 FOR EACH REPLICA
- NO CORRELATION BETWEEN FIT QUALITY AND POSITION IN THE (σ_H, σ_Z) PLANE
- UNIFORM FIT QUALITY

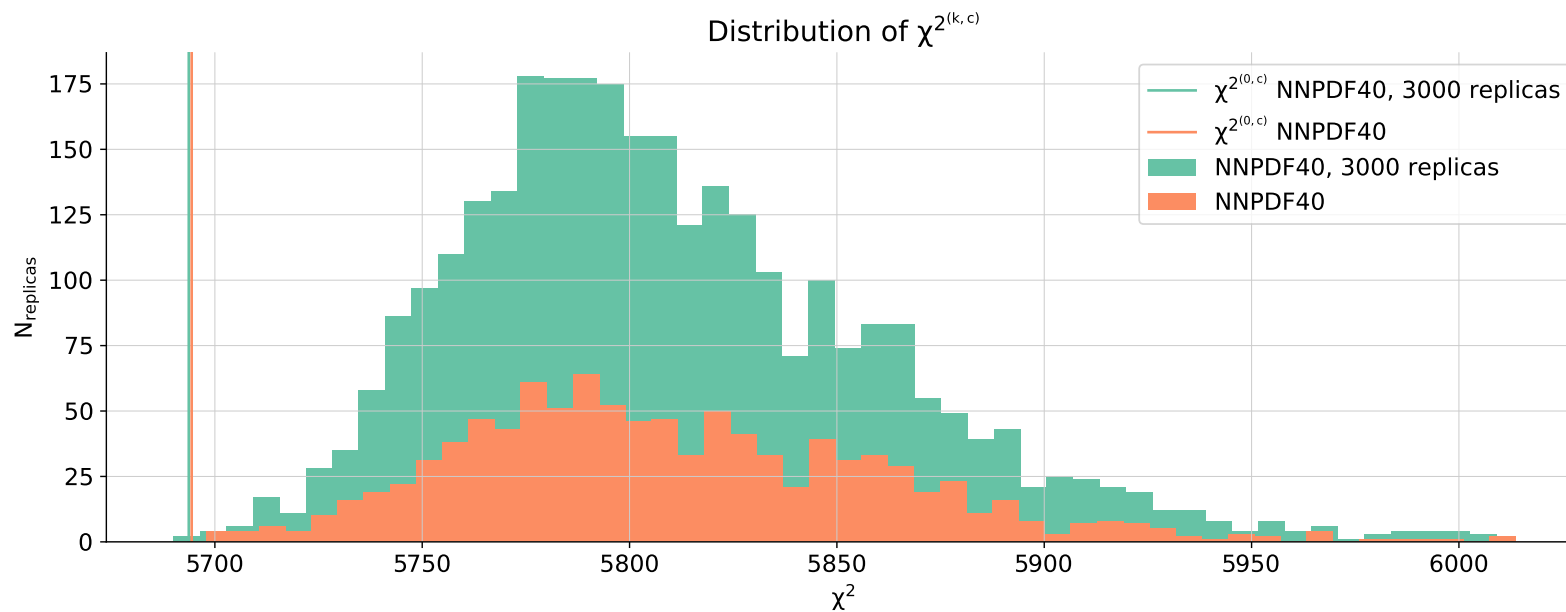
METRICS IN REPLICA SPACE

THE REPLICA DISTRIBUTION

COMPARISON TO CENTRAL DATA

- EACH PDF REPLICA FITTED TO A DATA REPLICA
- FIT QUALITY TO CENTRAL DATA STATISTICALLY DISTRIBUTED

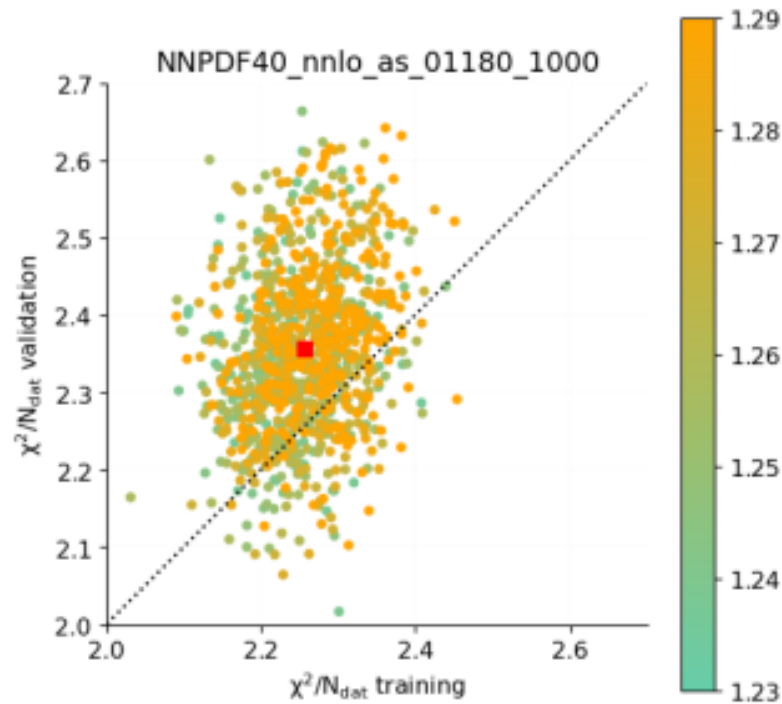
1000 REPLICAS VS. 3000 REPLICAS



- AVERAGE BEST FIT PDF \Rightarrow LOW χ^2
- NOT NECESSARILY LOWEST

THE REPLICA DISTRIBUTION COMPARISON TO CENTRAL DATA

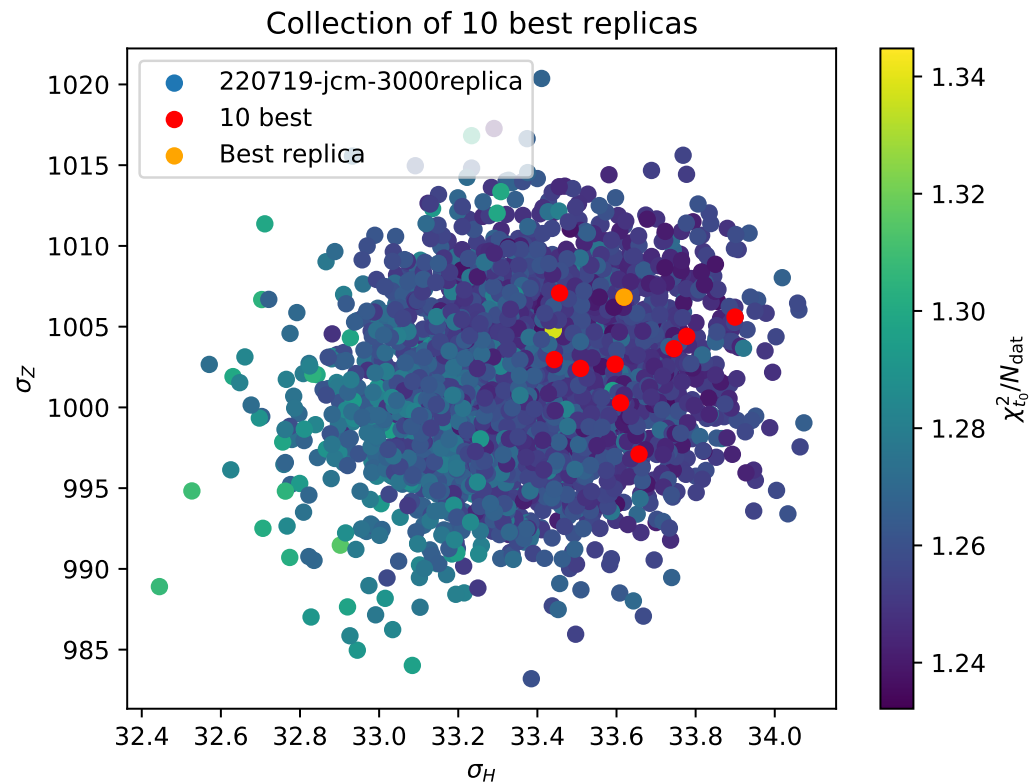
- ARE FITS WITH HIGH χ^2 TO CENTRAL DATA POOR (UNDERLEARNT)?



- NO CORRELATION BETWEEN χ^2 TO CENTRAL DATA AND TRAINING, VALIDATION χ^2
- UNIFORM FIT QUALITY
- DISPERSION DUE
 - DATA REPLICA FLUCTUATION \Rightarrow DATA UNCERTAINTIES
 - BEST FIT DEGENERACY
 \Rightarrow INTERPOLATION, EXTRAPOLATION AND FUNCTIONAL UNCERTAINTIES

REPLICA LOSS DISTRIBUTION

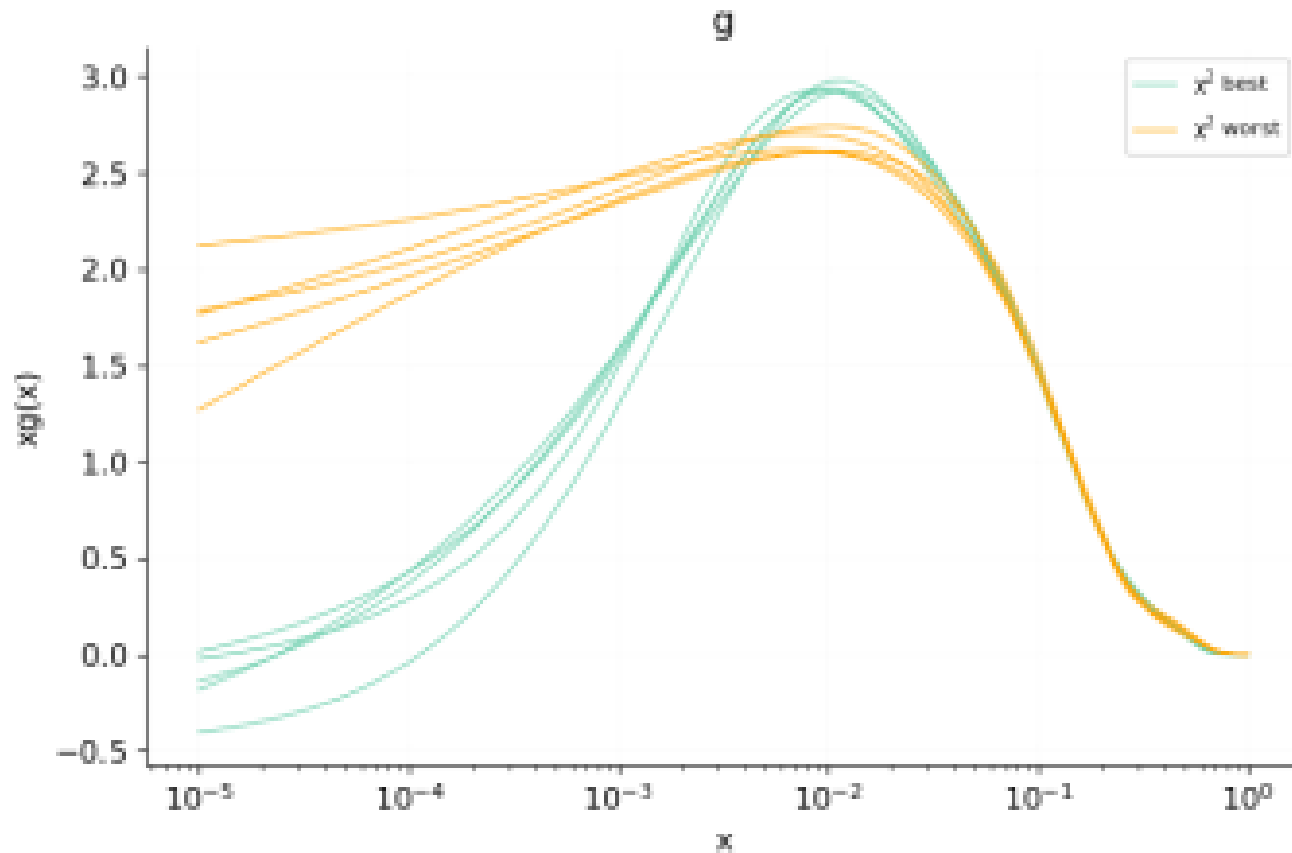
CORRELATION TO FEATURES



χ^2 TO CENTRAL DATA

- CORRELATED TO POSITION IN (σ_H, σ_z) PLANE
- CORRELATED TO A FEATURE?

EXPLANATION
LOOKING FOR FEATURES
REPLICAS WITH LOWEST & HIGHEST χ^2 TO CENTRAL DATA
THE GLUON

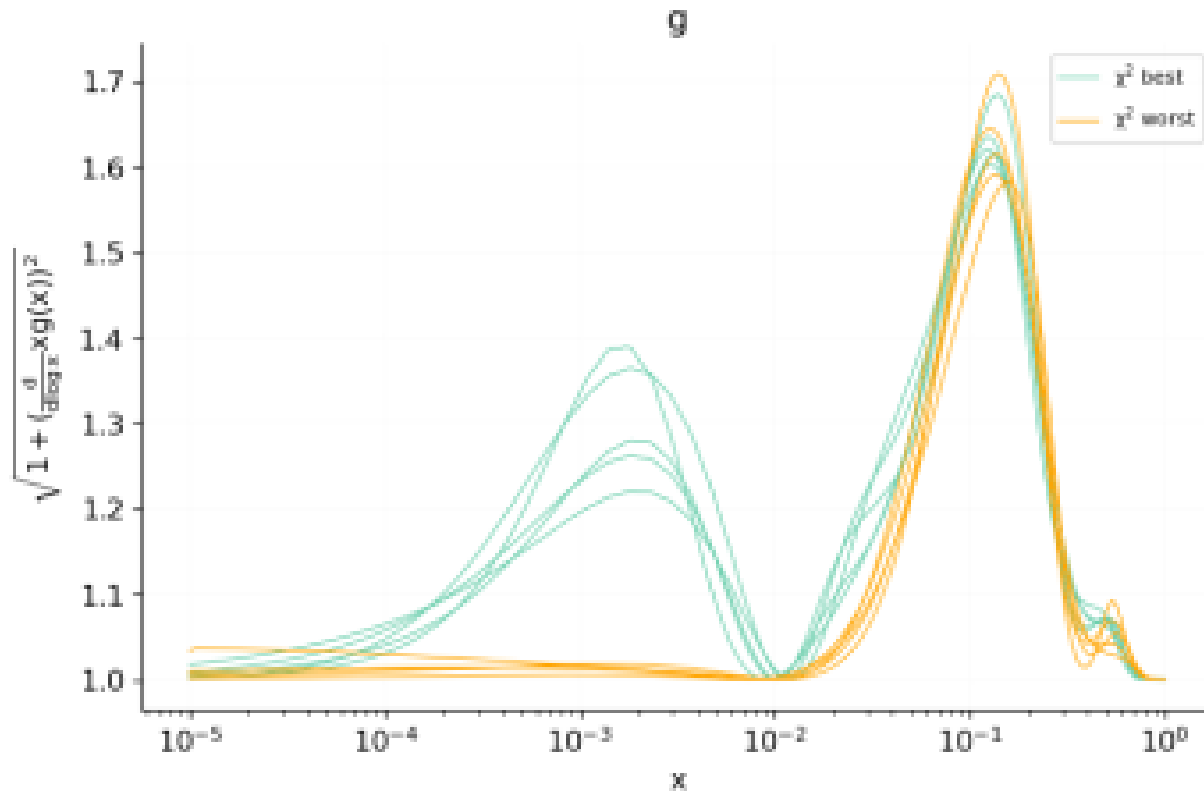


- REPLICAS CLOSER TO CENTRAL DATA \Rightarrow MORE STRUCTURE
- CORRELATED TO A FEATURE?

EXPLANATION
THE PDF KINETIC ENERGY
REPLICAS WITH LOWEST & HIGHEST χ^2 TO CENTRAL DATA

$$\text{KE} = \sqrt{1 + \left(\frac{d}{d \ln x} x f(x, Q^2) \right)^2}$$

ARCLENGTH OF THE NN OUTPUT IN TERMS OF INPUT
THE GLUON



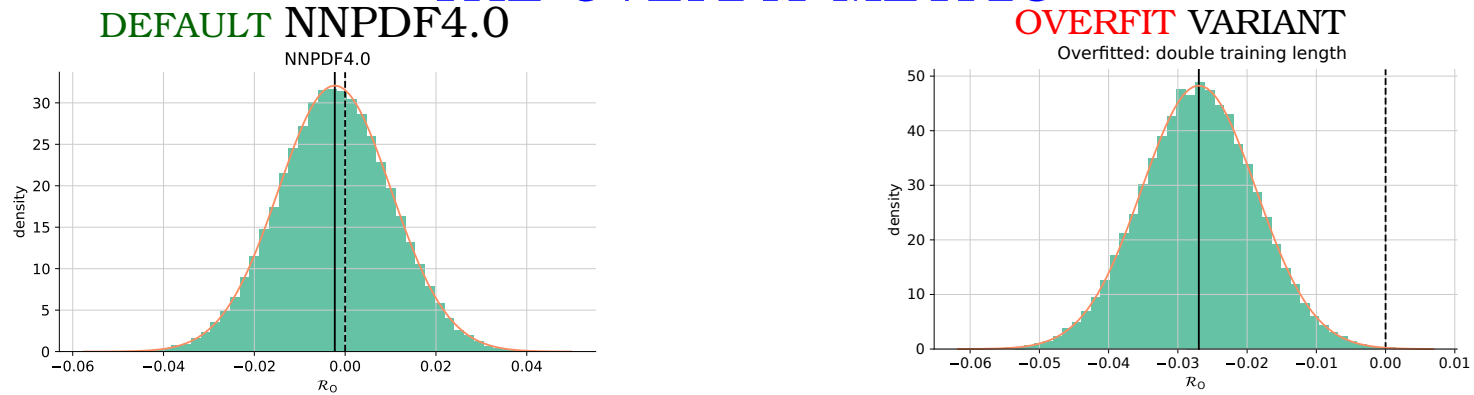
- REPLICAS CLOSER TO CENTRAL DATA \Rightarrow MORE STRUCTURE
- HIGHER KINETIC ENERGY

GENERALIZATION

EXPLANATION OVERLEARNING?

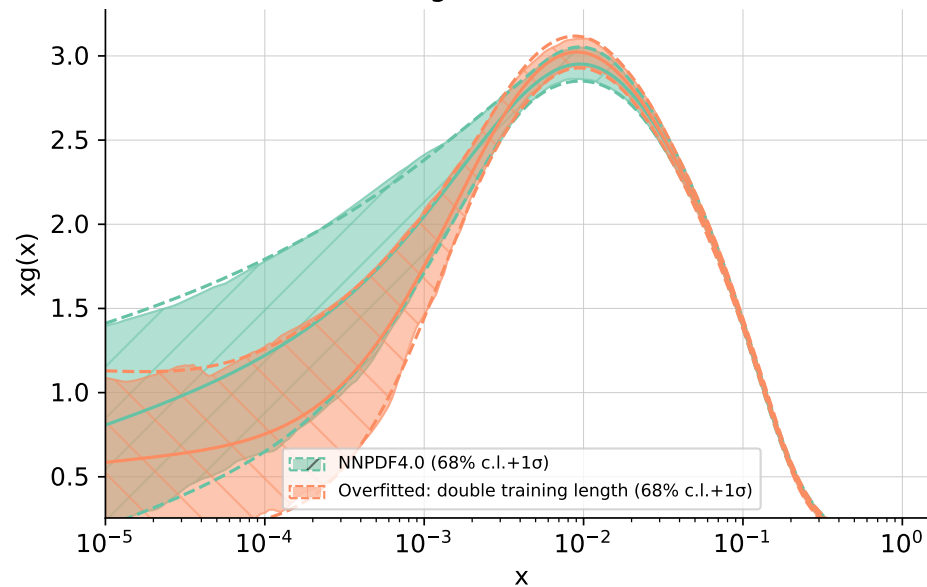
- INDUCE **OVERLEARNING**: DOUBLE TRAINING LENGTH

THE OVERFIT METRIC



THE GLUON

g at 1.7 GeV



- LOOK AT THE **OUTPUT** \Rightarrow **MORE STRUCTURE IN GLUON**

EXPLANATION A PARADOX?

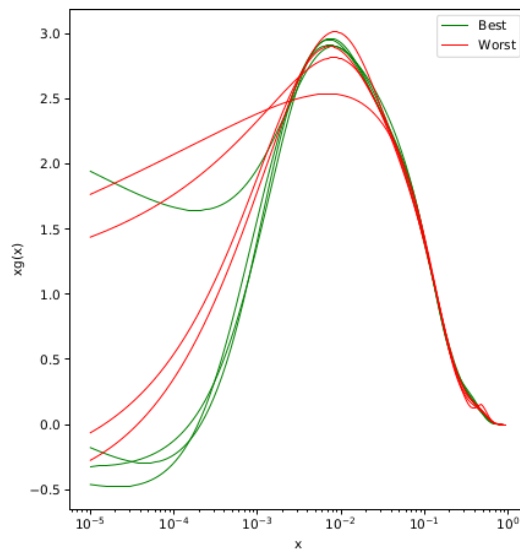
- BEST FIT TO CENTRAL DATA CORRELATED TO HIGH ARCLENGTH
- HIGH ARCLENGTH CORRELATED TO OVERLEARNING
- TRAINING/VALIDATION LOSS
UNCORRELATED TO QUALITY OF FIT TO CENTRAL DATA

EXPLANATION GENERALIZATION!

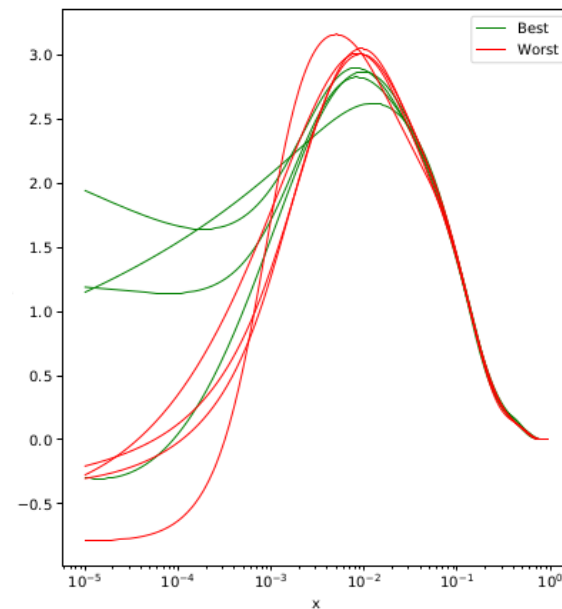
- OVERFITTING CAN MEAN POOR GENERALIZATION
- KEPT IN CHECK BY K-FOLDING (NOT CROSS-VALIDATION)
- LOOK AT BEST χ^2 TO FITTED VS. EXCLUDED FOLDS

THE GLUON

FITTED FOLDS



EXCLUDED FOLD



- BEST VS WORST REVERSED
- HIGH K.E. SOLUTIONS DO NOT GENERALIZE

THE FUTURE

WHY ML?

- MULTIDIMENSIONAL REGRESSION
- UNCERTAINTY CONTROL
- EXPLAINABILITY
- GENERALIZATION

EIC AND MACHINE LEARNING

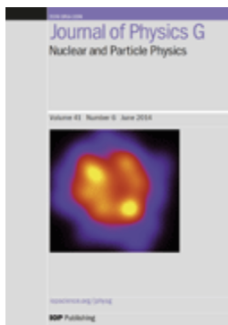
Artificial Intelligence for the Electron Ion Collider (AI4EIC)

C. Allaire^{61||}, R. Ammendola^{24||}, E.-C. Aschenauer^{3||}, M. Balandat^{35||}, M. Battaglieri^{38§}, J. Bernauer^{6,45§}, M. Bondi^{37||}, N. Branson^{34,15||}, T. Britton^{29||}, A. Butter^{30||}, I. Chahrour⁵⁶, P. Chatagnon²⁹, E. Cisbani^{39§}, E. W. Cline⁴⁸, S. Dash^{25§}, C. Dean^{33||}, W. Deconinck^{53§}, A. Deshpande^{6,4}, M. Diefenthaler^{29§||}, R. Ent^{29||}, C. Fanelli^{64,29††‡*}, M. Finger¹⁰, M. Finger, Jr.¹⁰, E. Fol^{5||}, S. Furletov^{29||}, Y. Gao³, J. Giroux^{64,57||††}, N. C. Gunawardhana Waduge⁵⁹, R. Harish^{9,12}, O. Hassan^{55,58}, P. L. Hegde⁹, R. J. Hernández-Pinto¹⁷, A. Hiller Blin^{27||}, T. Horn^{49‡}, J. Huang^{3||}, D. Jayakodige^{22,29}, B. Joo^{41||}, M. Junaid⁵⁷, P. Karande³², B. Kriesten⁸, R. Kunnawalkam Elayavalli^{62||}, M. Lin³, F. Liu^{41||}, S. Liuti^{59||}, G. Matousek¹⁶, M. McEneaney^{16||}, D. McSpadden^{29††}, T. Menzo^{53||}, T. Miceli^{18||}, V. Mikuni^{31||}, R. Montgomery^{54§}, B. Nachman^{31§||}, R. R. Nair³⁶, J. Niestroy⁶⁴, S. A. Ochoa Oregon¹⁷, J. Oleniacz⁶³, J. D. Osborn^{3§}, C. Paudel¹⁹, C. Pecar^{16||}, C. Peng^{1||}, G. N. Perdue^{18§}, W. Phelps^{11,29||}, M. L. Purschke³, K. Rajput^{29||††}, Y. Ren^{31§||}, D. F. Renteria-Estrada¹⁷, D. Richford², B. J. Roy^{40,23}, D. Roy⁴⁷, N. Sato^{29||}, T. Satogata^{29,42||}, G. Sborlini^{43,21}, M. Schram^{29§}, D. Shih^{46||}, J. Singh⁴⁴, R. Singh^{4,7}, A. Siodmok²⁸, P. Stone⁶⁴, J. Stevens^{64§}, L. Suarez⁶⁴, K. Suresh^{57††}, A.-N. Tawfik²⁰, F. Torales Acosta^{31||}, N. Tran^{18||}, R. Trotta⁴⁹, F. J. Twagirayezu⁵², R. Tyson⁵⁴, S. Volkova^{43||}, A. Vossen^{29,16§}, E. Walter^{64††}, D. Whiteson^{51||}, M. Williams^{33||}, S. Wu⁵⁵ and N. Zachariou⁶⁰ and P. Zurita^{14,26§}

13v1 [physics.acc-ph] 17 Jul 2023

- PDFs: COLLINEAR AND GPDs
- MONTE CARLO EVENT GENERATORS
- DETECTOR SIMULATION
- CROSS-SECTION INFERENCE
- EVENT RECONSTRUCTION AND PARTICLE IDENTIFICATION
- HARDWARE ACCELERATION
- STREAMING READOUT DATA AQUISITION

Journal of Physics G: Nuclear and Particle Physics



ISSN: 1361-6471

SUPPORTS OPEN ACCESS

Journal of Physics G: Nuclear and Particle Physics publishes theoretical and experimental research in nuclear and particle physics including all interface areas between these fields. The journal also publishes articles on nuclear and particle astrophysics.

[Submit an article](#)[Track my article](#)

RSS

[Sign up for new issue notifications](#)

Current volume

Number 10, October 2023

[Go](#)

Journal archive

Vol 50, 2023

[Go](#)

Focus issues

Focus on Neutrino-Nucleus Inter

[Go](#)**9 days**

Median submission to first decision before peer review

[Full list of journal metrics](#)**62 days**

Median submission to first decision after peer review

3.5

Impact factor

7.2

Citescore

[Most read](#)**Latest articles**[Review articles](#)[Accepted manuscripts](#)[Open Access](#)[Open all abstracts](#)**OPEN ACCESS****The exploration of hot and dense nuclear matter: introduction to relativistic heavy-ion physics**Hannah Elfner and Berndt Müller 2023 *J. Phys. G: Nucl. Part. Phys.* **50** 103001[+ Open abstract](#)[View article](#)[PDF](#)

EXTRAS

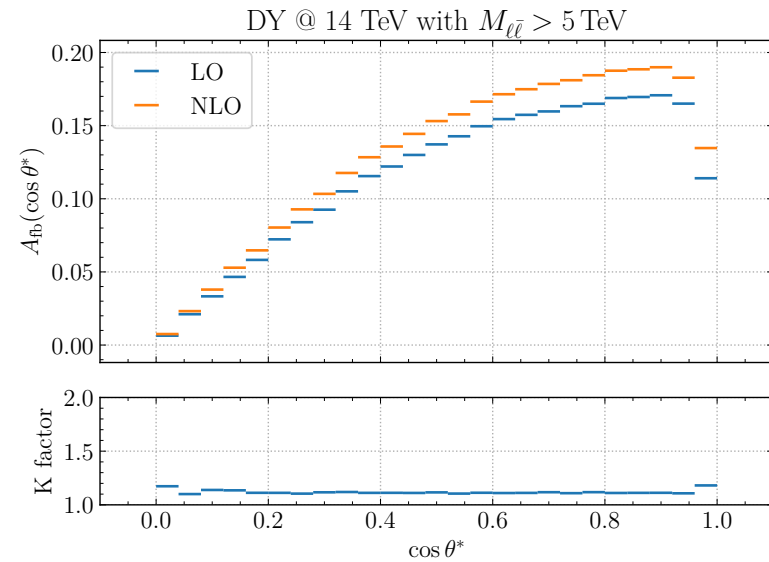
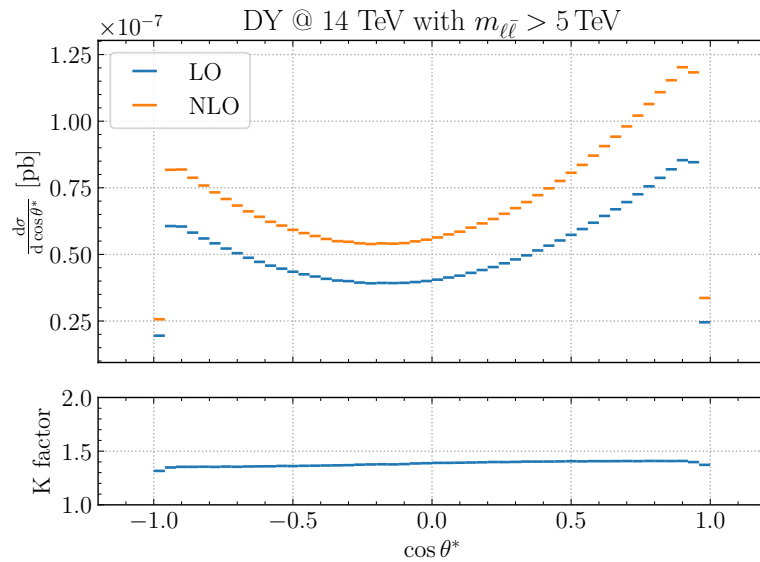
QUALITATIVE BEHAVIOR: NLO vs. LO LO INTEGRATED RESULT (HIGH MASS)

$$A_{\text{fb}}(\cos \theta^*) = \frac{\cos \theta^*}{(1 + \cos^2(\theta^*))} \frac{g_A}{g_{S,q'}}; \quad g_{A,S} \propto \int \frac{dm_{\ell\bar{\ell}}}{m_{\ell\bar{\ell}}} \frac{dx_1}{x_1} \mathcal{L}_{A,S}(m_{\ell\bar{\ell}}, x_1)$$

LO vs. NLO FOR $M_{z'} = 5\text{TeV}$

CROSS-SECTION

FORWARD-BACKWARD ASYMMETRY



- AT LO, $A_{\text{fb}} \propto \cos \theta$, **EFFECTIVE COUPLING** DETERMINED BY PDF **LUMINOSITY**
- NLO **K-FACTOR ALMOST θ -INDEPENDENT**

QUALITATIVE BEHAVIOR:

$$A_{\text{fb}} \propto \mathcal{L}_{A,q} = f_q(x_1)f_{\bar{q}}(x_2) - f_q(x_2)f_{\bar{q}}(x_1) = \frac{1}{2} \left(f_q^-(x_1)f_q^+(x_2) - f_q^-(x_2)f_q^+(x_1) \right)$$

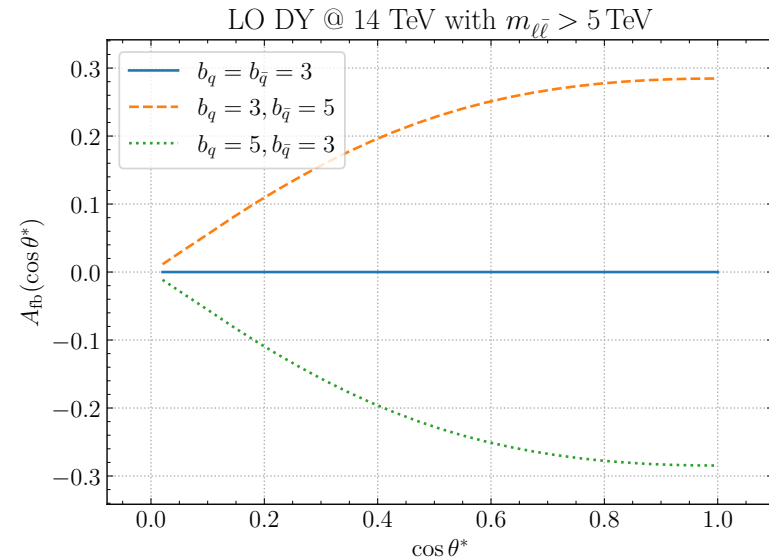
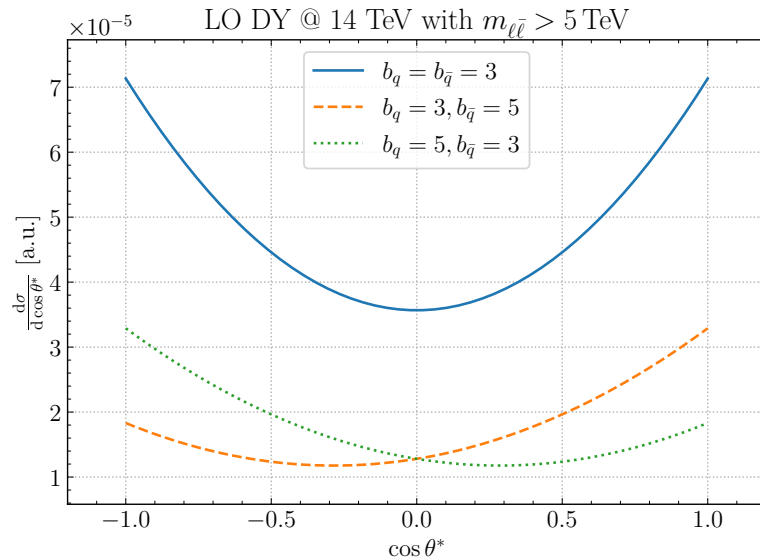
$$f_q^\pm = f_q \pm f_{\bar{q}}; f^- \rightarrow \text{VALENCE}; f^+ \rightarrow \text{SEA}$$

TOY PDFS

$$x f_q^\pm = x^{-1} \left[(1-x)^{b_q} \pm (1-x)^{b_{\bar{q}}} \right]$$

CROSS-SECTION

FORWARD-BACKWARD ASYMMETRY



- TOY: SIGN OF ASYM \Leftrightarrow SIGN OF VALENCE

- GENERAL: SIGN OF ASYM \Leftrightarrow DROP OF VALENCE VS. SEA

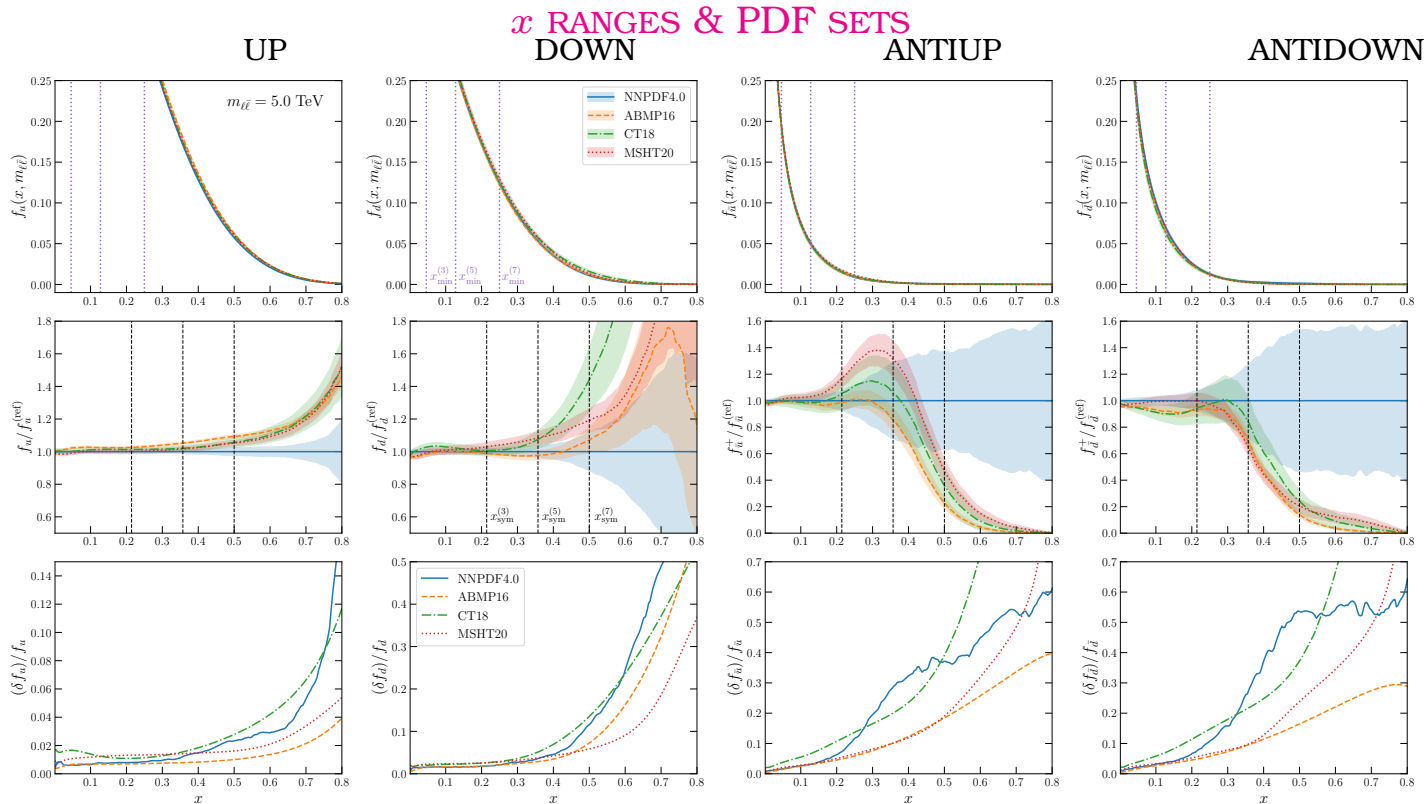
$$\text{sign} [\mathcal{L}_{A,q}] = \text{sign} \left[\frac{f_q^+(x_2)}{f_q^+(x_1)} - \frac{f_q^-(x_2)}{f_q^-(x_1)} \right] = \text{sign} \left[\frac{f_q(x_2)}{f_q(x_1)} - \frac{f_{\bar{q}}(x_2)}{f_{\bar{q}}(x_1)} \right], x_1 > x_2$$

- VALENCE DROPS FASTER \Rightarrow NEGATIVE ASYM

CANNOT HAVE NEGATIVE VALENCE, BUT FAST-DROPPING VALENCE ALLOWED

QUALITATIVE BEHAVIOR: EXISTING PDF SETS

- DOMINANT CONTRIBUTION \Rightarrow up AND down QUARKS, ANTIQUARKS
- AS Z' MASS CHANGES, x RANGE CHANGES: $x_1 x_2 = \frac{m_{\ell\bar{\ell}}}{\sqrt{s}}$
BUT PDFS (LARGE x) CHANGE VERY LITTLE

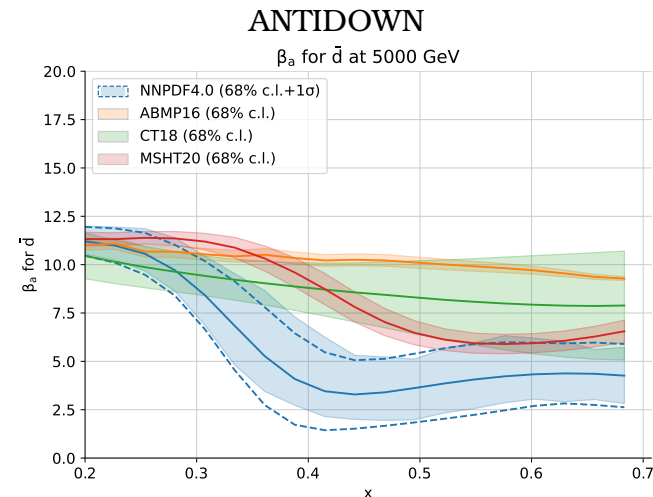
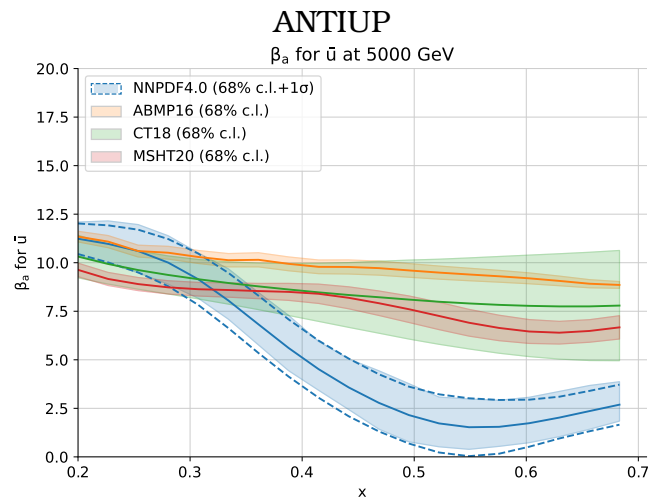
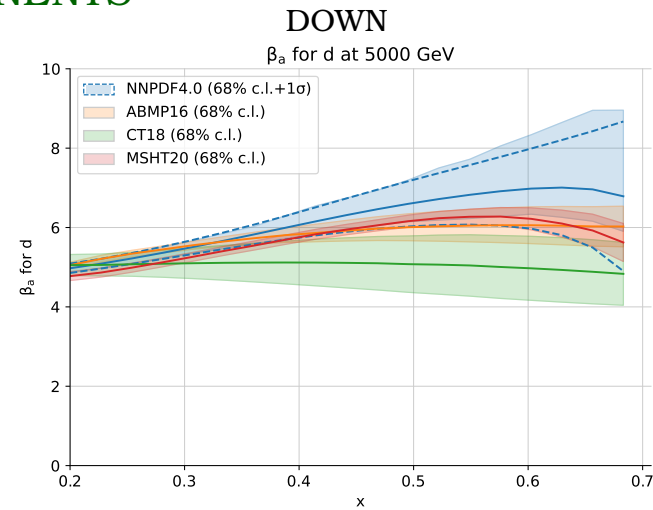
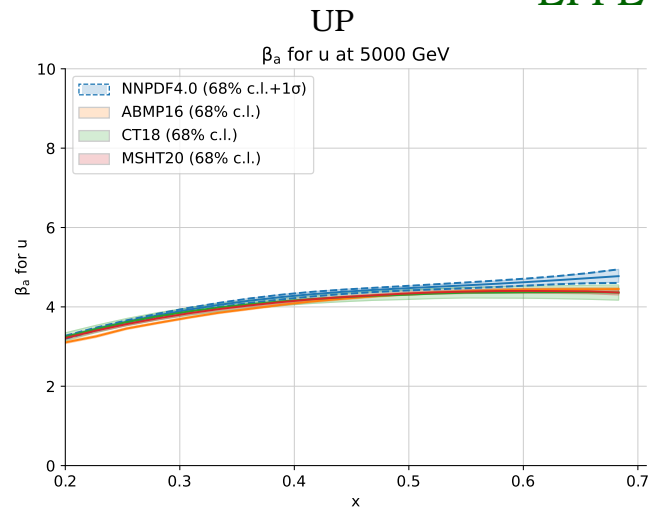


- $M \lesssim 3$ TEV \Rightarrow DATA REGION, ALL PDF SETS AGREE
- $M \gtrsim 5$ TEV \Rightarrow EXTRAPOLATION, NNPDF DISAGREES
 - DIFFERENT CENTRAL VALUE
 - LARGER UNCERTAINTY

PDF BEHAVIOR: WHAT'S GOING ON?

- CT, MSHT, ABMP PARAMETRIZATION: $f(x) = x^\alpha (1-x)^\beta g(x)$; NNPDF NEURAL NETWORK
- DEFINE **EFFECTIVE EXPONENT** $\beta(x) \equiv \frac{\partial \ln |x f(x)|}{\partial \ln(1-x)}$

EFFECTIVE EXPONENTS

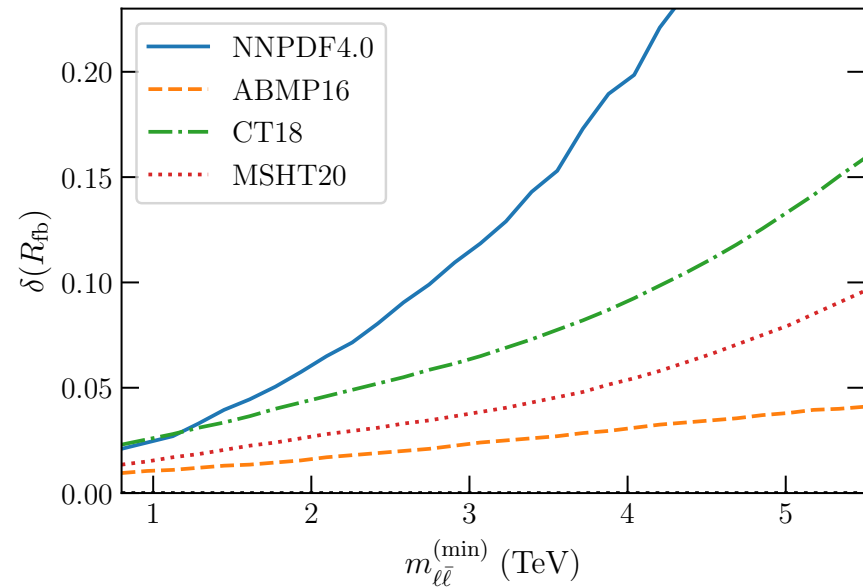
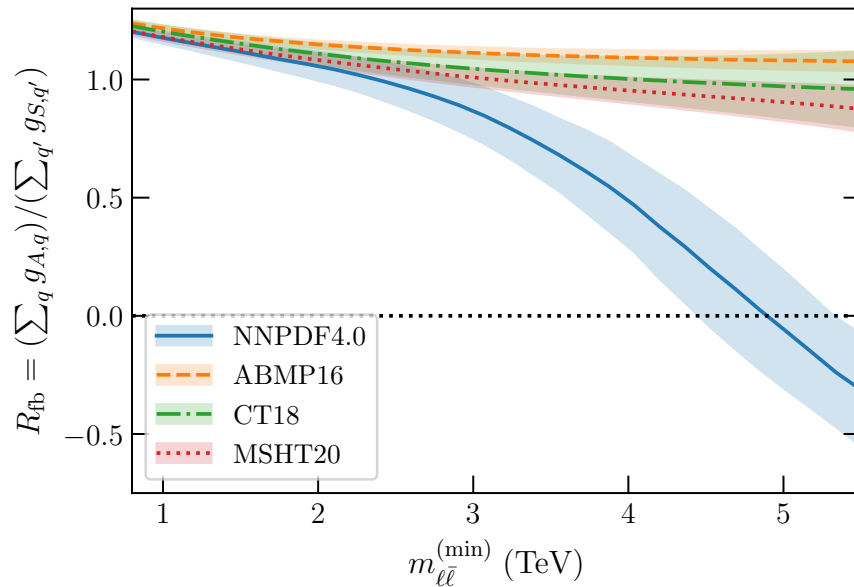


- **CT, MSHT, ABMP: LARGE x β APPROX. CONSTANT**
- **NNPDF: β NOT FIXED BY PARAMETRIZATION**

WHAT'S GOING ON? THE EFFECTIVE COUPLING

RECALL $A_{\text{fb}}(\cos \theta^*) = \frac{\cos \theta^*}{(1 + \cos^2(\theta^*))} \frac{g_A}{g_{S,q'}}$; $g_{A,S} \propto \int \frac{dm_{\ell\bar{\ell}}}{m_{\ell\bar{\ell}}} \frac{dx_1}{x_1} \mathcal{L}_{A,S}(m_{\ell\bar{\ell}}, x_1)$

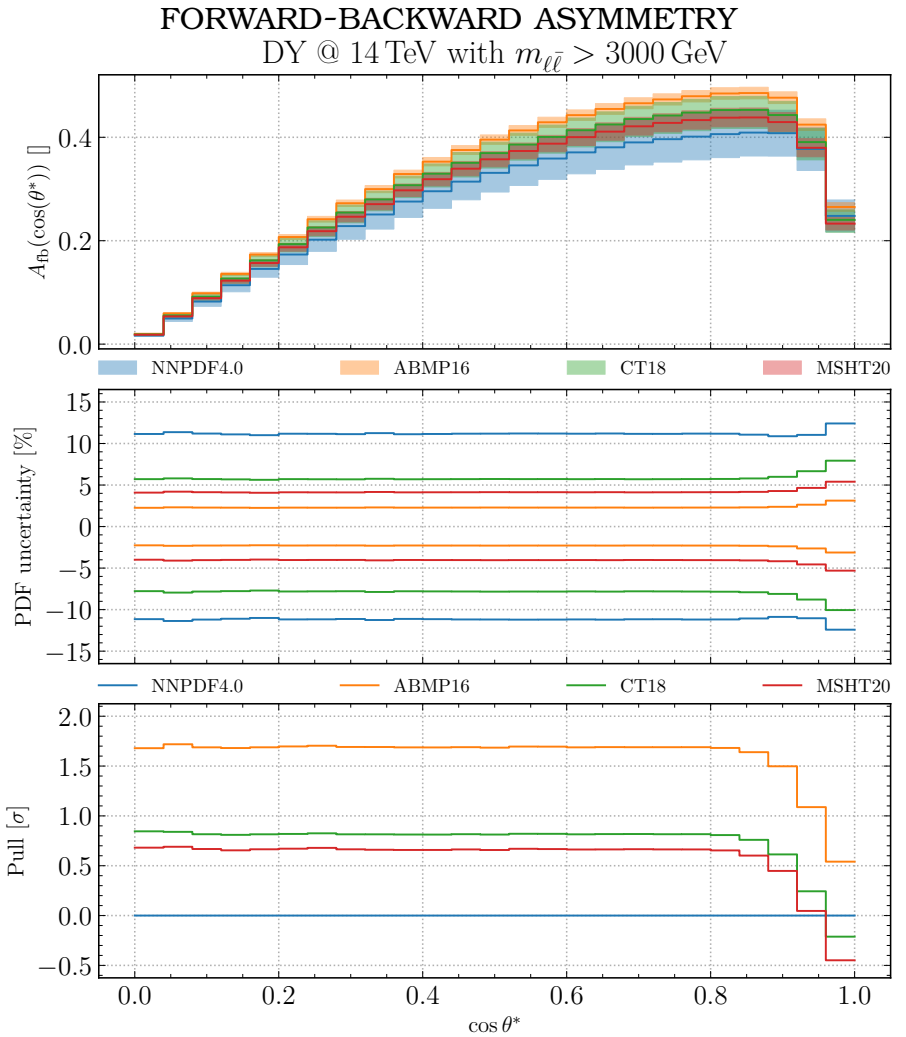
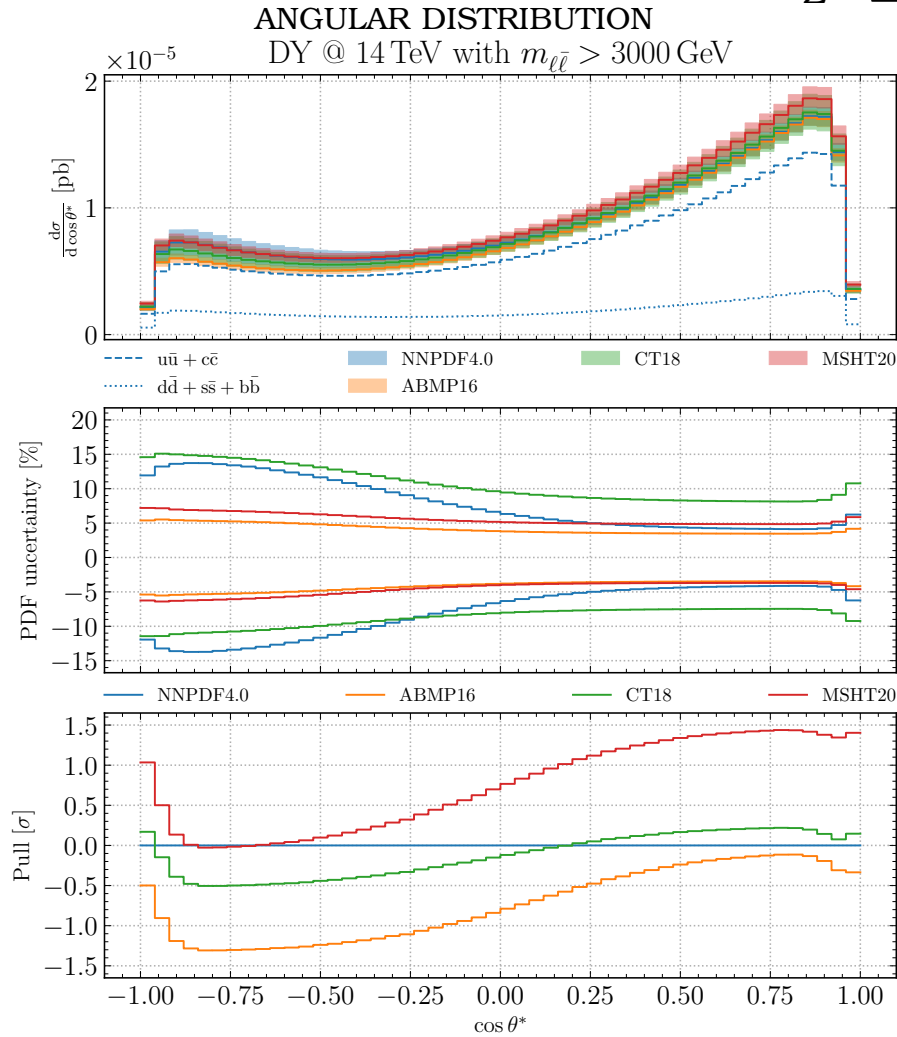
COUPLING
ABSOLUTE UNCERTAINTY



- AS SCALE INCREASES, LARGER x PROBED
- CT, MSHT, ABMP: COUPLING APPROX. SCALE INDEP.
- NNPDF: COUPLING DEPENDS ON SCALE, LARGER UNCERTAINTY

THE FORWARD-BACKWARD ASYMMETRY

$$M_{Z'} \geq 3 \text{ TeV}$$

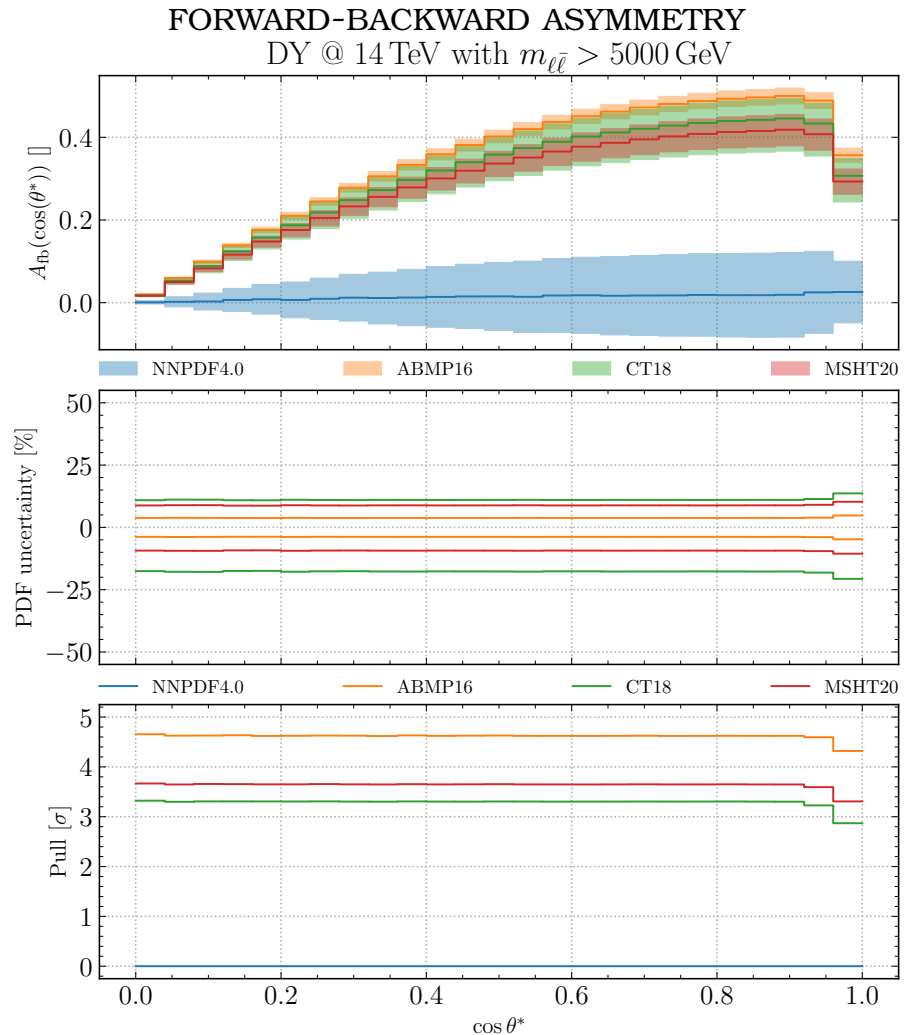
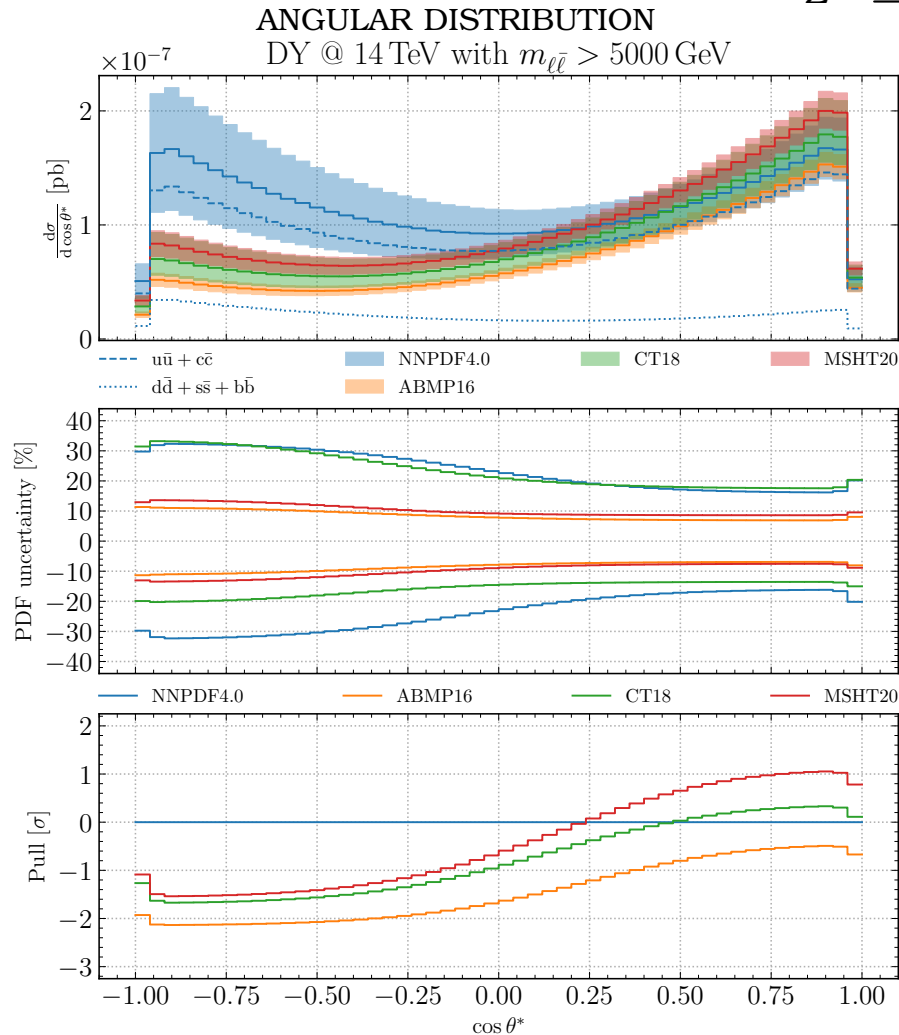


- $M_{Z'} \geq 3 \text{ TeV}$: DATA REGION, ALL PDF SETS AGREE

- .

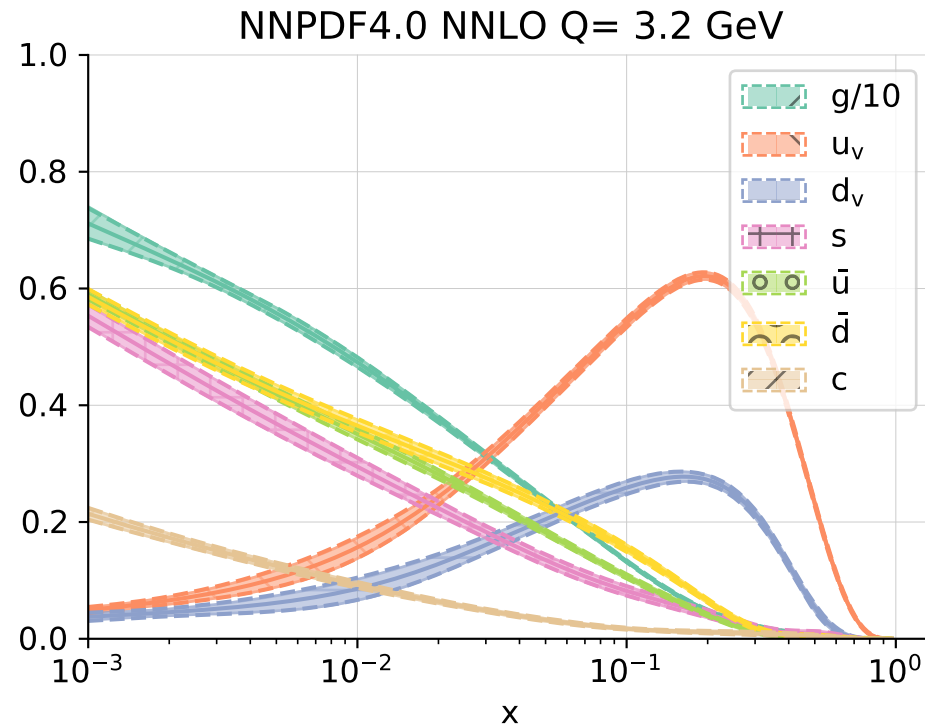
THE FORWARD-BACKWARD ASYMMETRY

$M_{Z'} \geq 5 \text{ TeV}$



- $M_{Z'} \geq 3 \text{ TeV}$: DATA REGION, ALL PDF SETS AGREE
- $M_{Z'} \geq 5 \text{ TeV}$
 - CT, MSHT, ABMP \Rightarrow ASYMMETRY UNCHANGED WITH INCREASING SCALE
 - NNPDF \Rightarrow ASYMMETRY DISAPPEARS AS SCALE INCREASES

PDFs: THE STATE OF THE ART (NNPDF4.0, 2021)



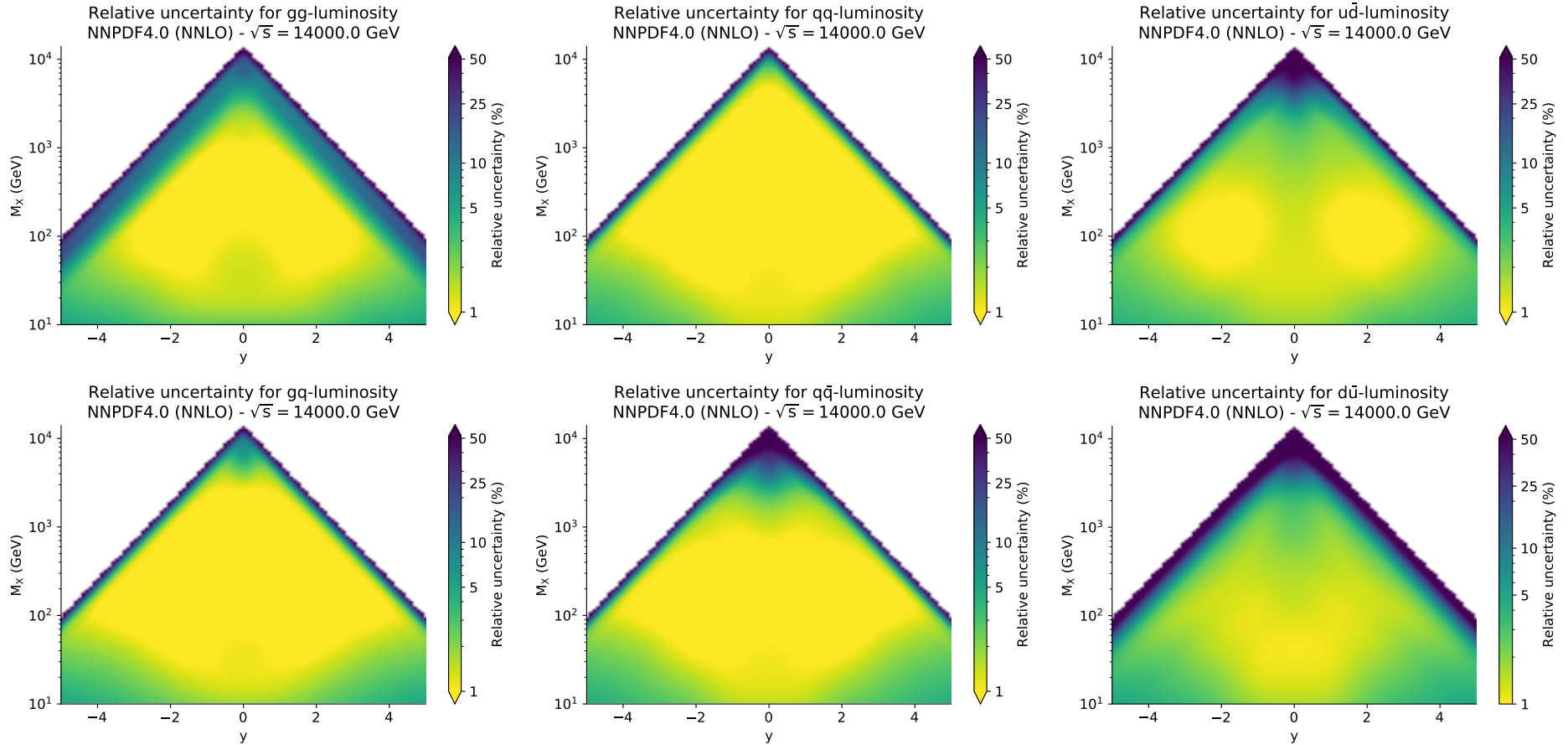
- A SET OF **PROBABILITY DISTRIBUTIONS** OF PROBABILITY DISTRIBUTIONS
- **FULL** (INFINITE DIMENSIONAL) **COVARIANCE MATRIX**
- MUST BE **DETERMINED** FROM FINITE SET OF **DISCRETE DATA**

UNCERTAINTIES: STATE OF THE ART (NNPDF4.0, 2021)

GLUON

SINGLET

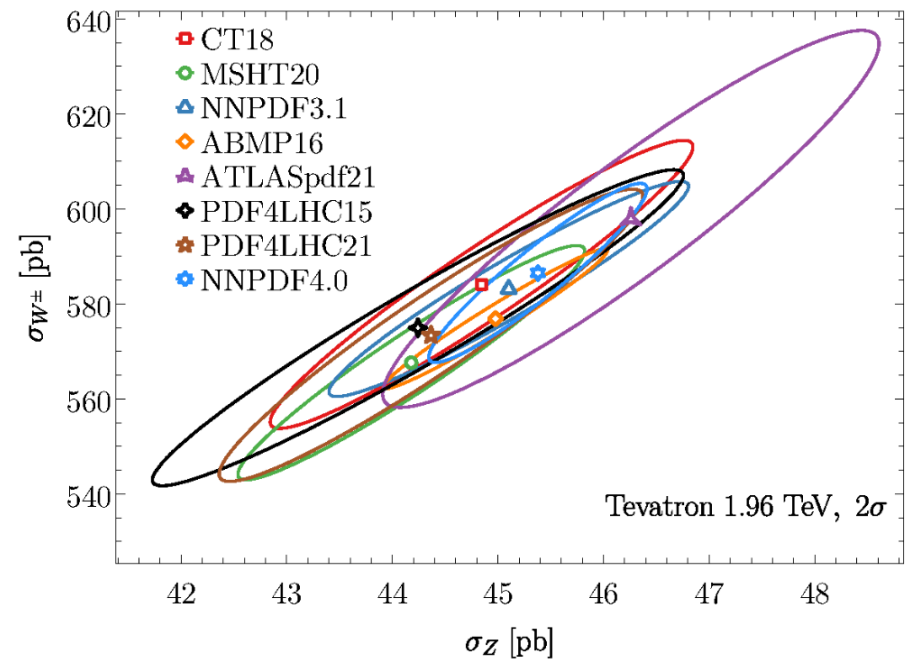
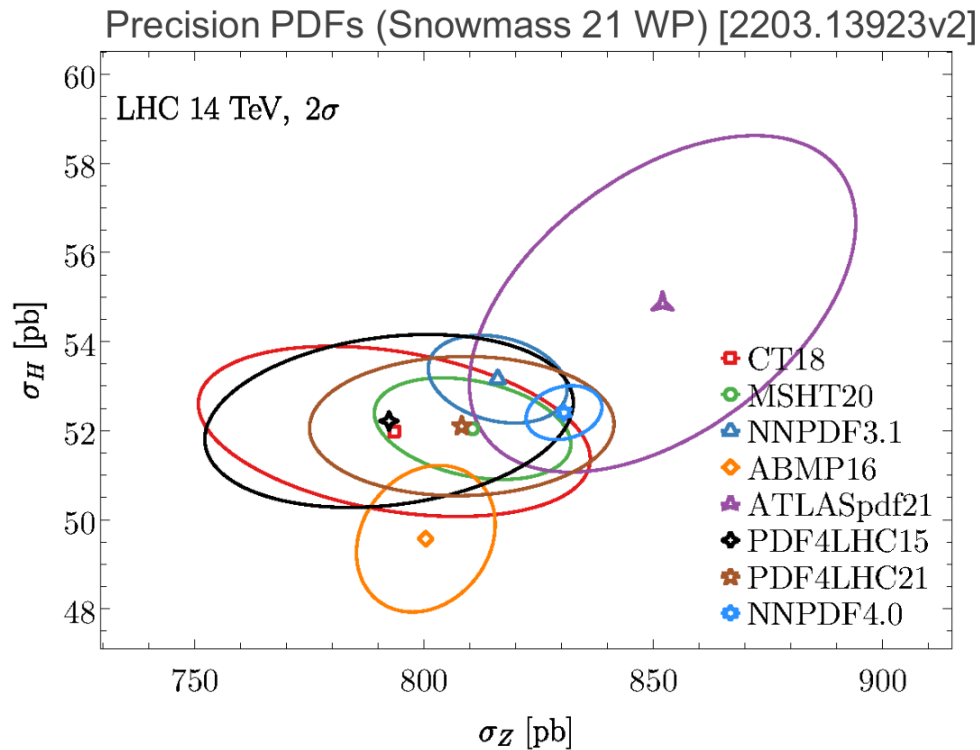
FLAVORS



- TYPICAL UNCERTAINTIES IN DATA REGION: SINGLET $\sim 1\%$, NONSINGLET $\sim 2 - 3\%$
- DATA REGION: $10 \lesssim M_X \lesssim 3 \cdot 10^3$ TEV, $-4 \lesssim y \lesssim 4$

UNCERTAINTIES: STATE OF THE ART (NNPDF4.0, 2021)

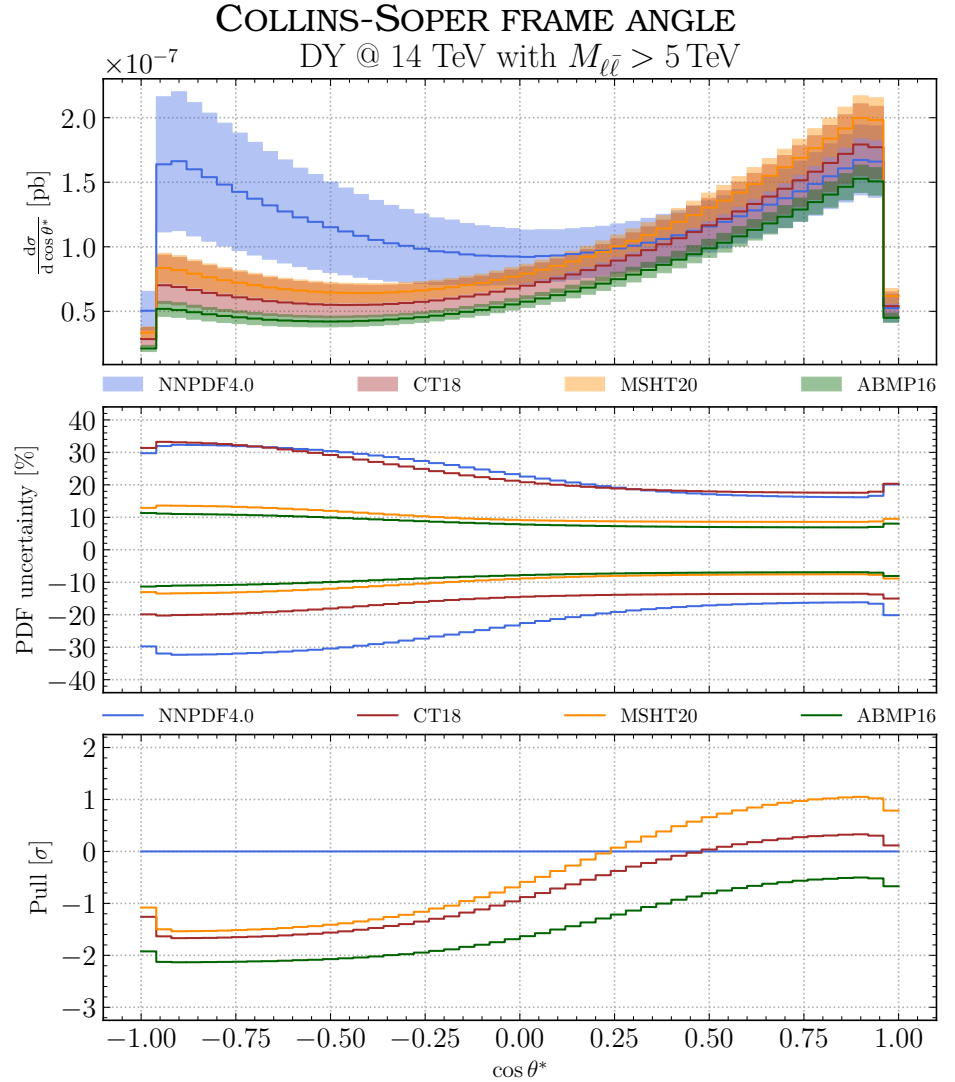
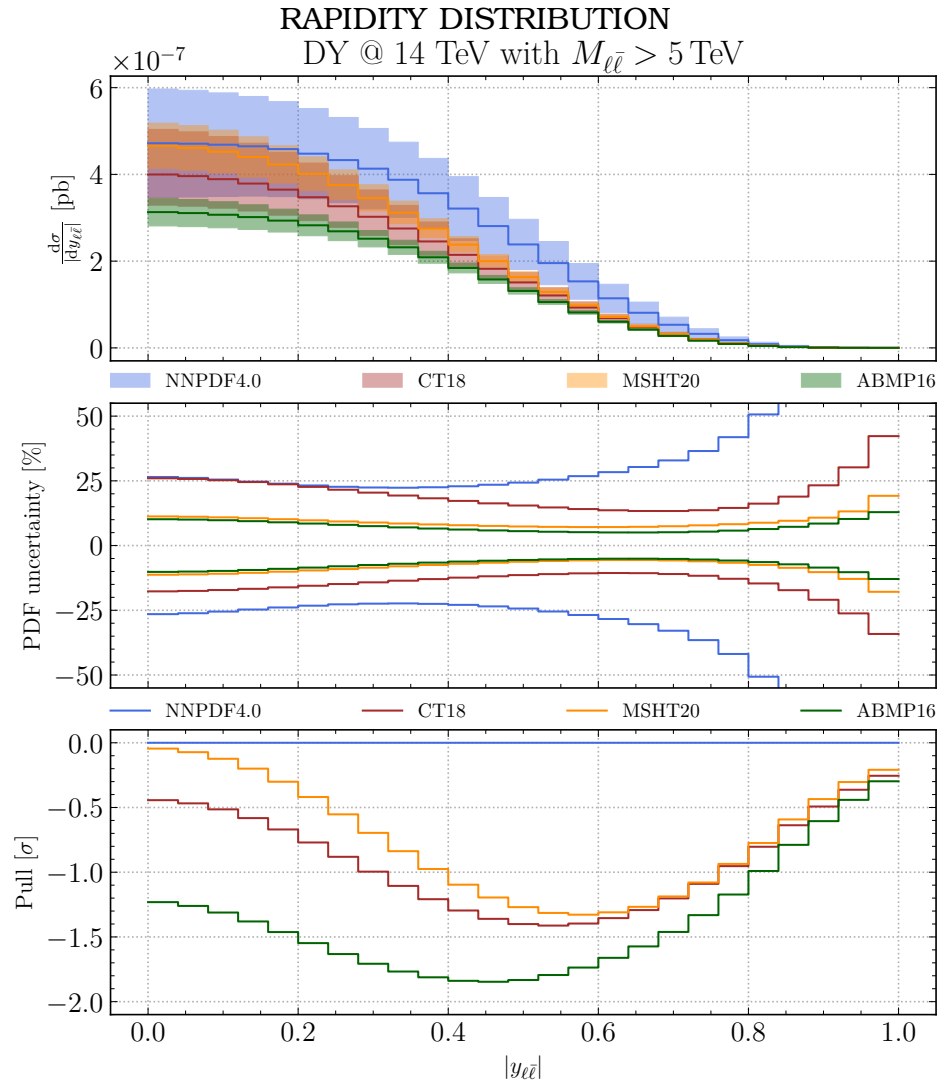
Higgs, W, Z production



DATA REGION: NNPDF4.0 UNCERTAINTIES \Rightarrow **SMALLER**
THAN OTHER PDF SETS
BACKWARD CONSISTENT WITH NNPDF3.1

UNCERTAINTIES: STATE OF THE ART (NNPDF4.0, 2021)

Z' production



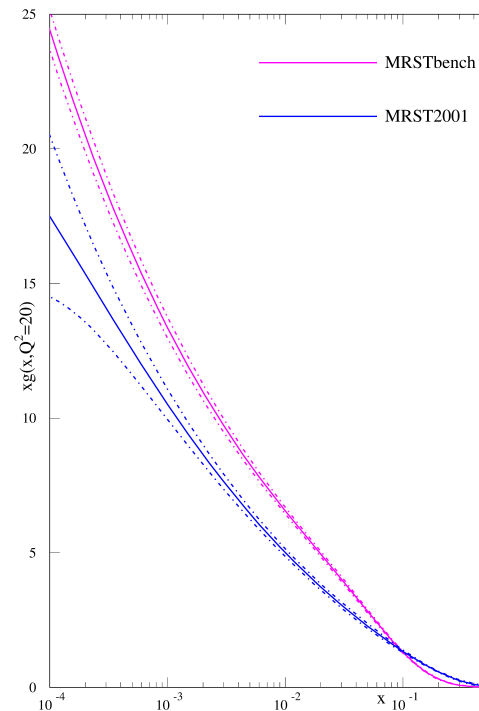
EXTRAPOLATION REGION: NNPDF4.0 UNCERTAINTIES \Rightarrow **LARGER**
THAN OTHER PDF SETS
UNBIASED PDF BEHAVIOR

UNCERTAINTY ESTIMATION

THE PDF UNCERTAINTY PROBLEM: THE HERA-LHC BENCHMARK (2005)

- RESTRICTED AND VERY CONSISTENT DATASET USED
- RESULTS COMPARED TO THEN-BEST RESULT FROM FULL DATASET

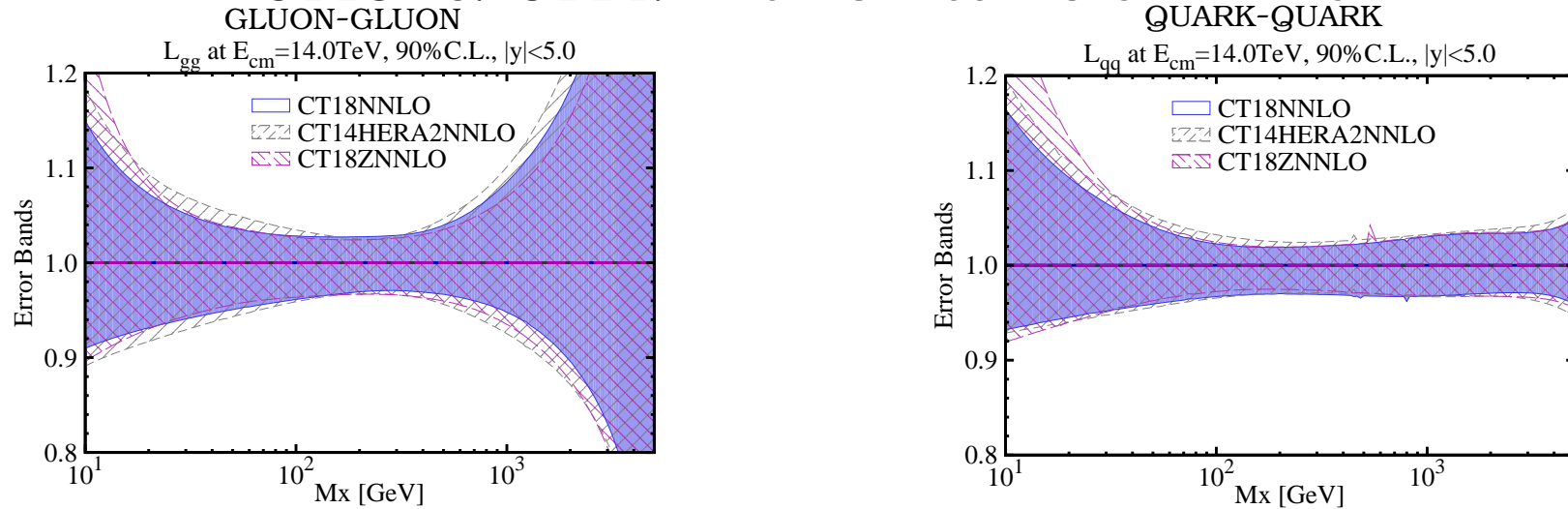
BENCHMARK VS DEFAULT GLUON



“...the partons extracted using a very limited data set are completely incompatible, even allowing for the uncertainties, with those obtained from a global fit with an identical treatment of errors...The comparison illustrates the problems in determining the true uncertainty on parton distributions.” (R.Thorne, HERALHC, 2005)

THE PDF UNCERTAINTY PROBLEM: THE PRE-ML APPROACH

CT18 vs. CT14: PARTON LUMINOSITY UNCERTAINTIES

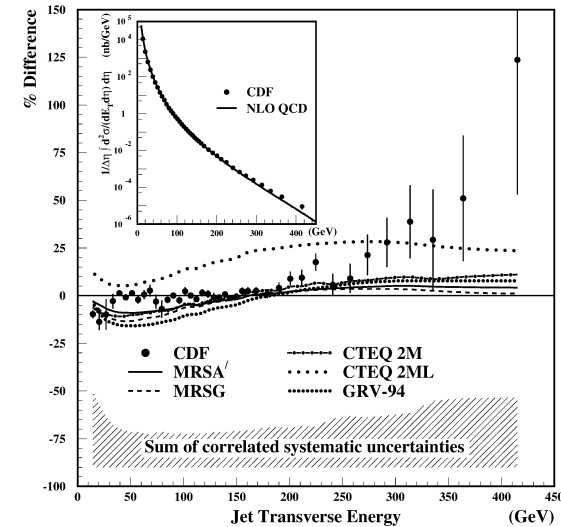


MORE DATA \Rightarrow BIGGER UNCERTAINTIES (!)
PARTON PARAMETRIZATIONS

- CTEQ5 2002: $xg(x, Q_0^2) = A_0 x^{A_1} (1-x)^{A_2} (1 + A_3 x^{A_4})$
- MRST-HERALHC 2005: $xg(x, Q_0^2) = A_g x^{\delta_g} (1-x)^{\eta_g} (1 + \epsilon_g x^{0.5} + \gamma_g x) + A_{g'} x^{\delta_{g'}} (1-x)^{\eta_{g'}}$
- CT18: $g(x, Q = Q_0) = x^{a_1-1} (1-x)^{a_2} [a_3(1-y)^3 + a_4 3y(1-y)^2 + a_5 3y^2(1-y) + y^3]$;
 $y = \sqrt{x}$; $a_5 = (3 + 2a_1)/3$.

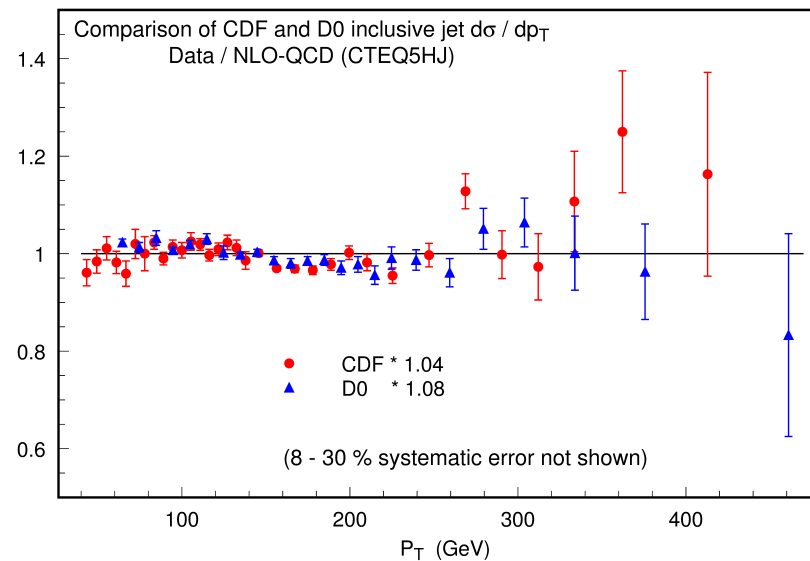
PDF UNCERTAINTIES AND NEW PHYSICS

- **DISCREPANCY** BETWEEN QCD CALCULATION AND CDF JET DATA (1995)
- EVIDENCE FOR **QUARK COMPOSITENESS?**
- RESULT **STRONGLY DEPENDS** ON GLUON AT $x \gtrsim 0.1$
- PDF MUST VANISH AT $x = 0$, BUT (THEN) NO DATA FOR $x \gtrsim 0.05!$



DISCREPANCY REMOVED IF JET DATA USED FOR GLUON DETERMINATION

NEW CTEQ GLUON (1998)

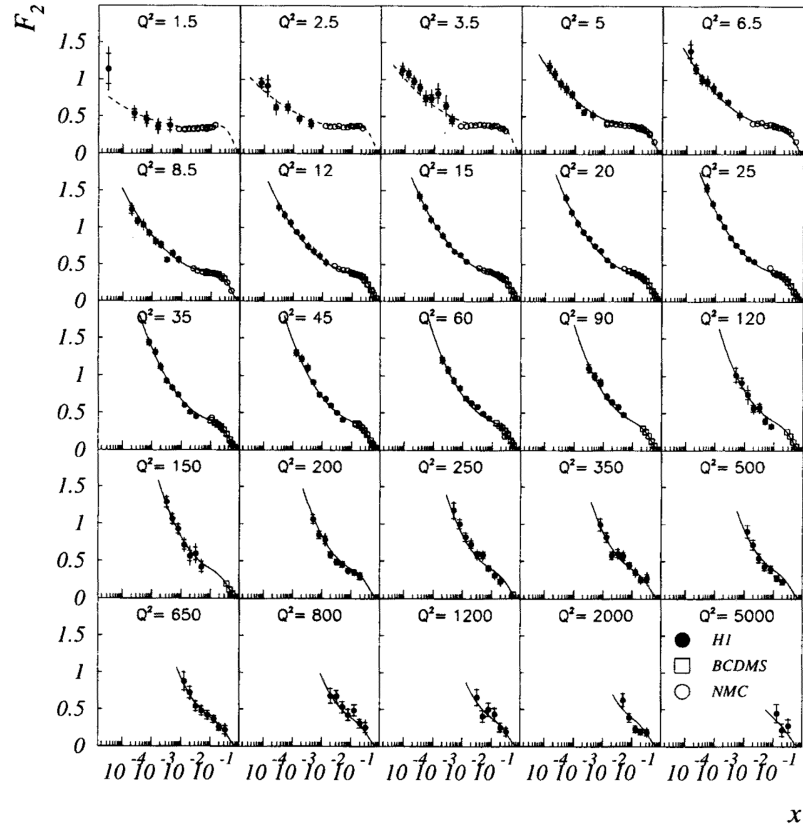


NOW: NO DATA FOR $x \gtrsim 0.5 \Rightarrow$ **DISCOVERY** (THRESHOLD) REGION!

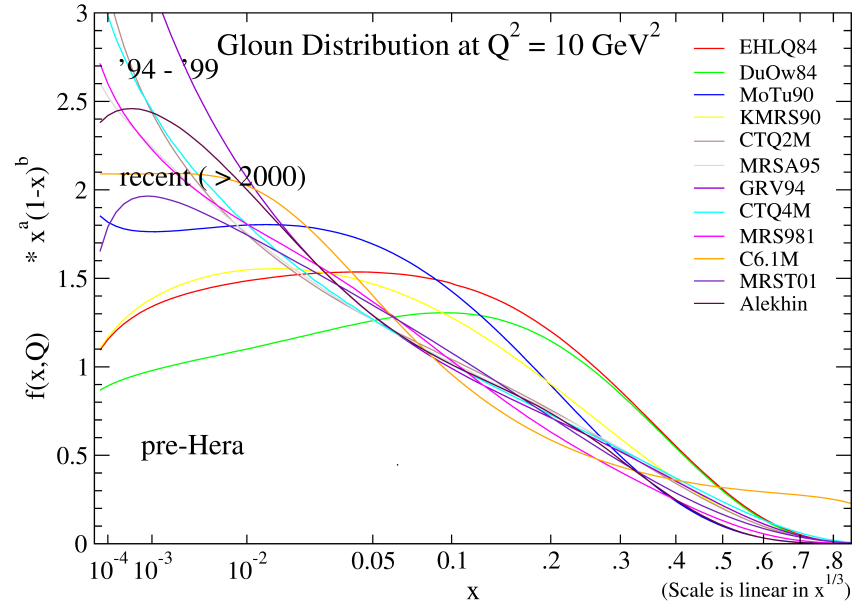
EXTRAPOLATION AND THEORY BIAS

1995: THE RISE OF STRUCTURE FUNCTIONS AT HERA

FIRST HERA DATA VS OLDER DATA



HISTORICAL COMPILATION OF GLUON PDFs



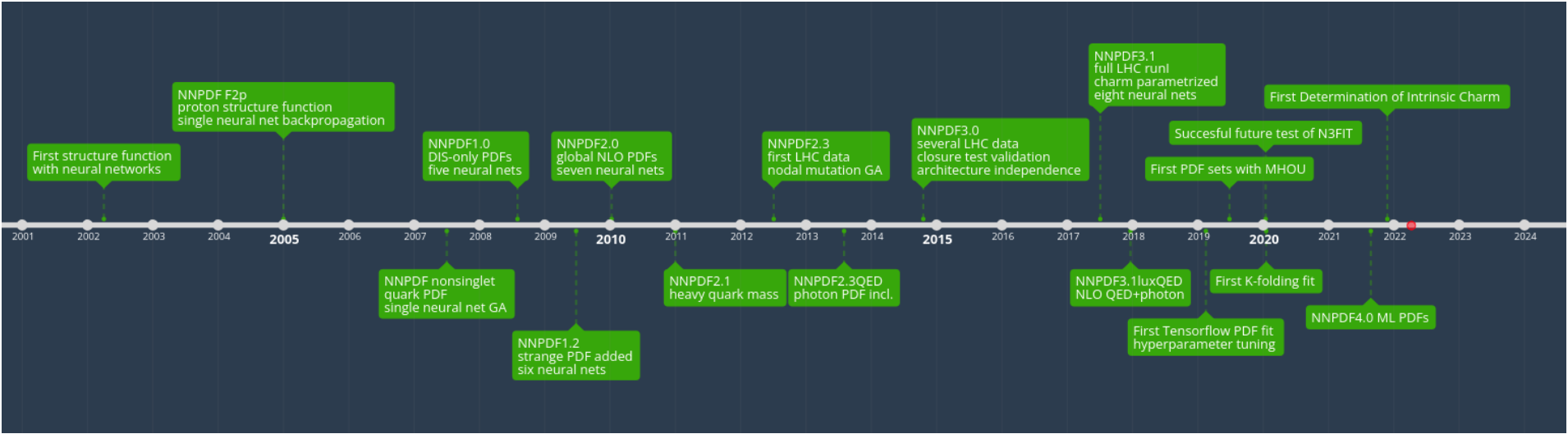
W.K.Tung, DIS 2004

A. de Roeck, Cracow epiphany conf. 1996

- **RISE** OF F_2 AT HERA CAME \Rightarrow **SURPRIZE**
- **HINTED** BY PRE-HERA **DATA**; **VETOED** BY **THEORETICAL BIAS**

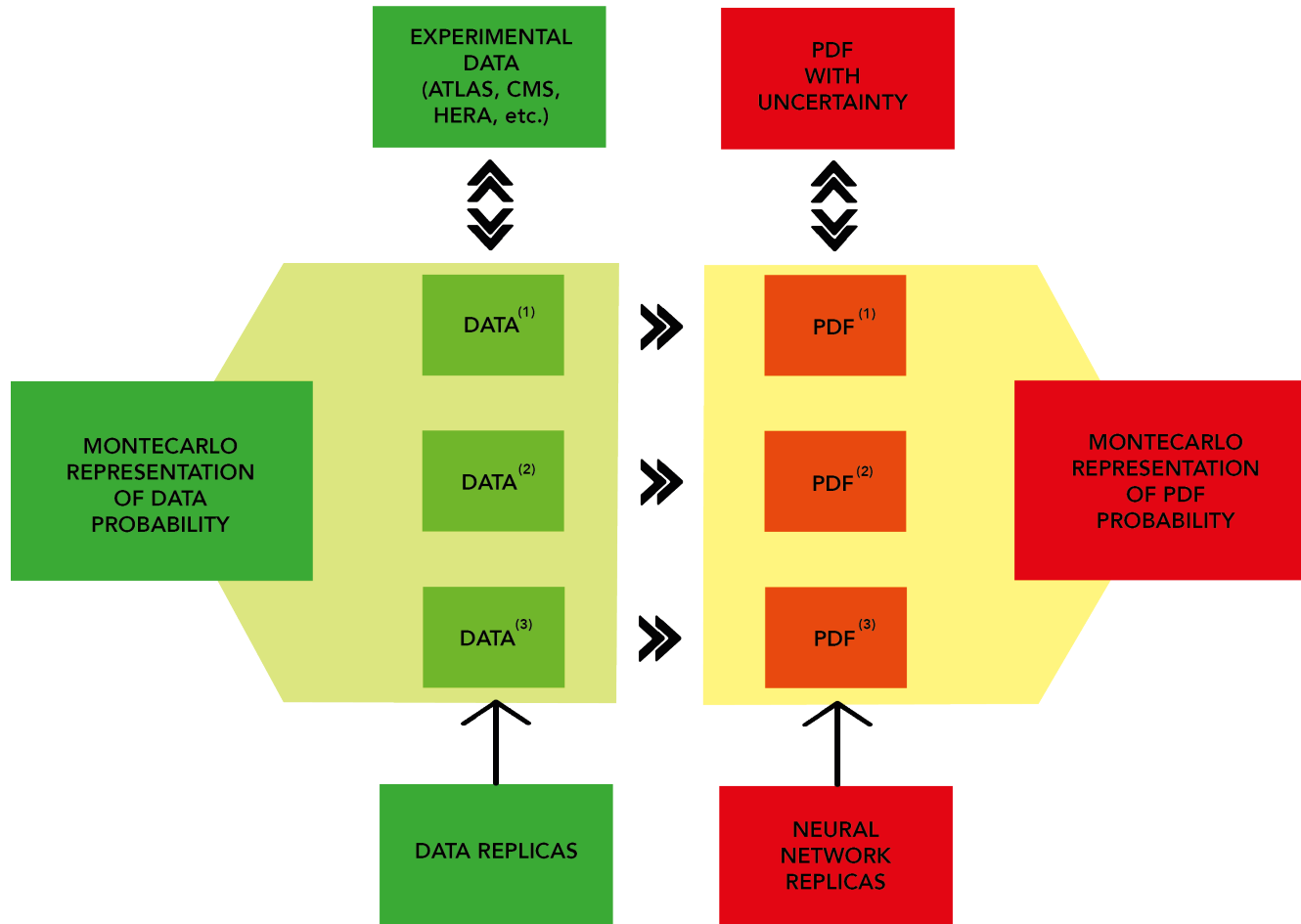
THE NNPDF METHODOLOGY

PROTON STRUCTURE AS AN AI PROBLEM: NNPDF



THE FUNCTIONAL MONTE CARLO

REPLICA SAMPLE OF FUNCTIONS \Leftrightarrow PROBABILITY DENSITY IN FUNCTION SPACE
 KNOWLEDGE OF LIKELIHOOD SHAPE (FUNCTIONAL FORM) NOT NECESSARY

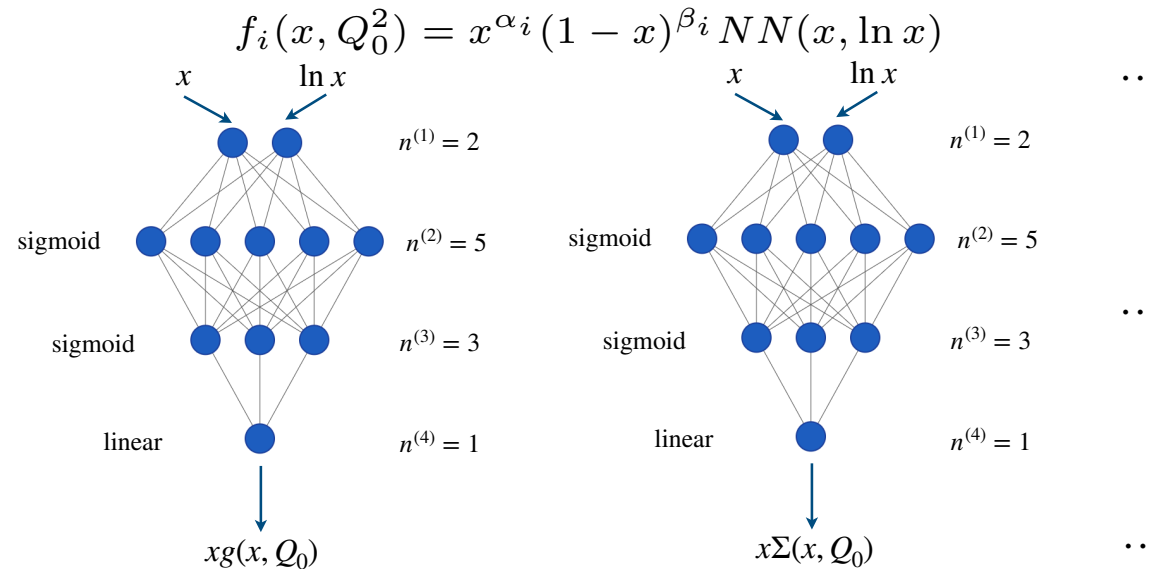


FINAL PDF SET: $f_i^{(a)}(x, \mu)$;

$i = \text{up, antiup, down, antidown, strange, antistrange, charm, gluon}; j = 1, 2, \dots, N_{\text{rep}}$

OLD NNPDF (UP TO 2021)

NEURAL NETWORKS



- 37 PARAMETERS \times 8 PDFS
- **PREPROCESSING** EXPONENTS RANDOMIZED REPLICAS PER REPLICAS, RANGE DETERMINED SELF-CONSISTENTLY

GENETIC MINIMIZATION

- **NODAL MUTATION** REPLACED POINT MUTATION
- SINGLE EPOCH WITH NO REWEIGHTING UNLIKE PREVIOUS

OPTIMAL FIT

- **CROSS-VALIDATION** WITH 50-50 TRAINING & VALIDATION FRACTIONS
- **LOOKBACK** STOPPING REPLACED THRESHOLD ON DERIVATIVE

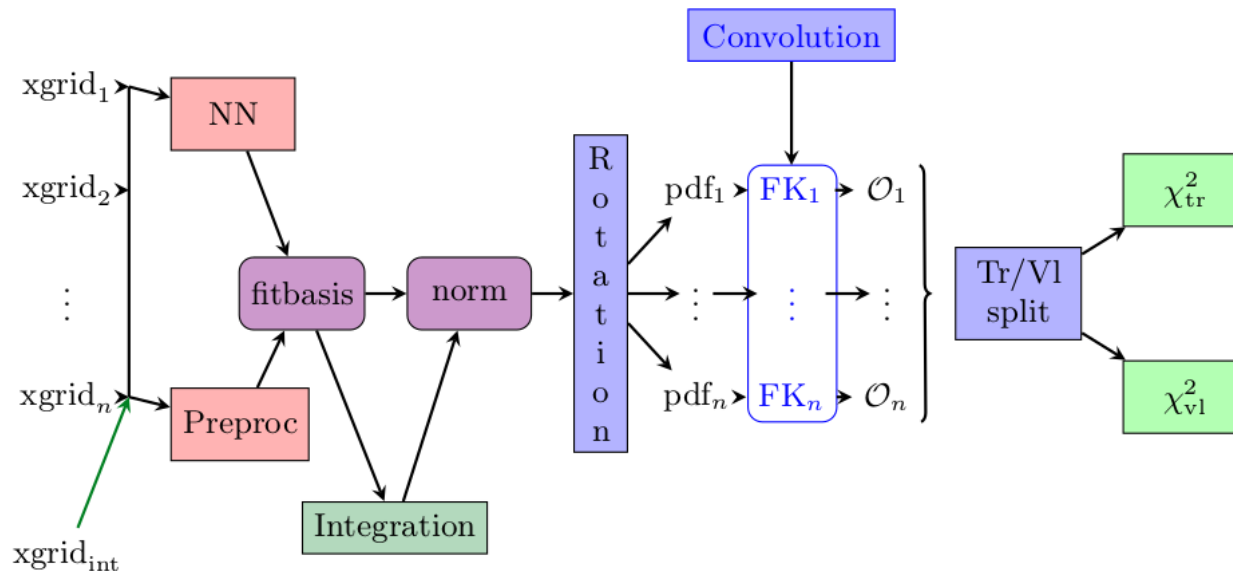
MACHINE LEARNING PDFs

LEARNING THE METHODOLOGY

THE N3FIT PROJECT

HOW DO WE KNOW THAT THE METHODOLOGY IS THE BEST?
“ACCUMULATED WISDOM” INEFFICIENT AND SLOW

CHANGE OF PHILOSOPHY \Rightarrow DETERMINISTIC MINIMIZATION (GRADIENT DESCENT)
GO FOR THE ABSOLUTE MINIMUM, AND (HYPER)OPTIMIZE



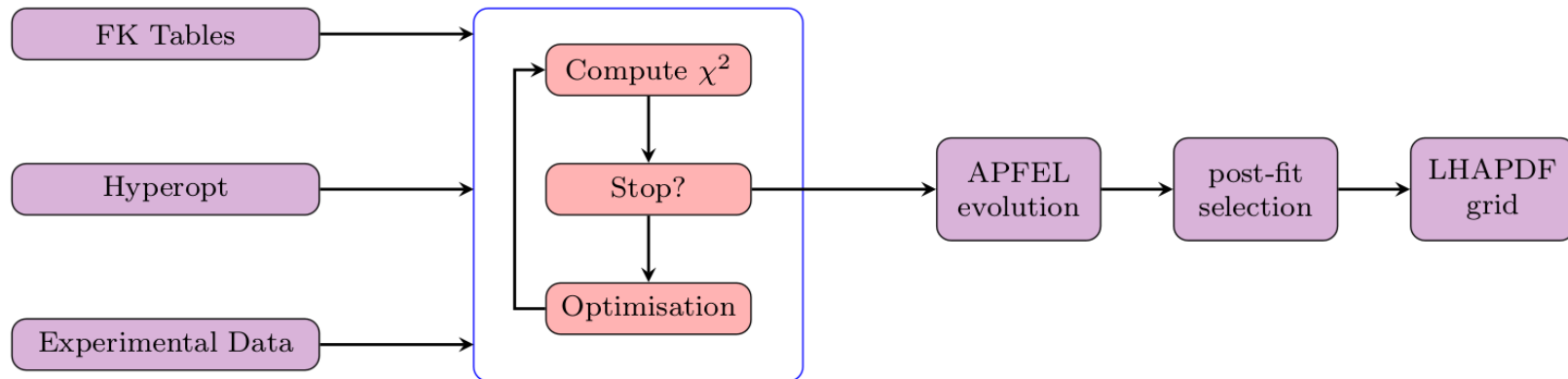
- PYTHON-BASED KERAS + TENSORFLOW FRAMEWORK
- EACH BLOCK INDEPENDENT LAYER
- CAN VARY ALL ASPECTS OF METHODOLOGY

THE NNPDF CODE STRUCTURE

- MODULAR PYTHON-BASED CODE
- HIGH DEGREE PARALLELIZATION & HARDWARE ACCELERATION

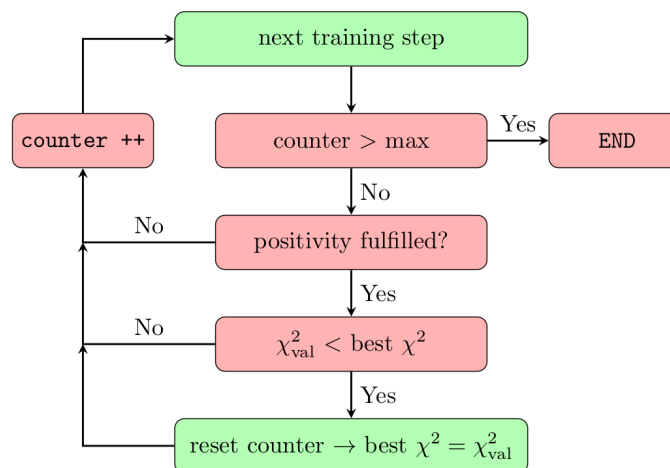
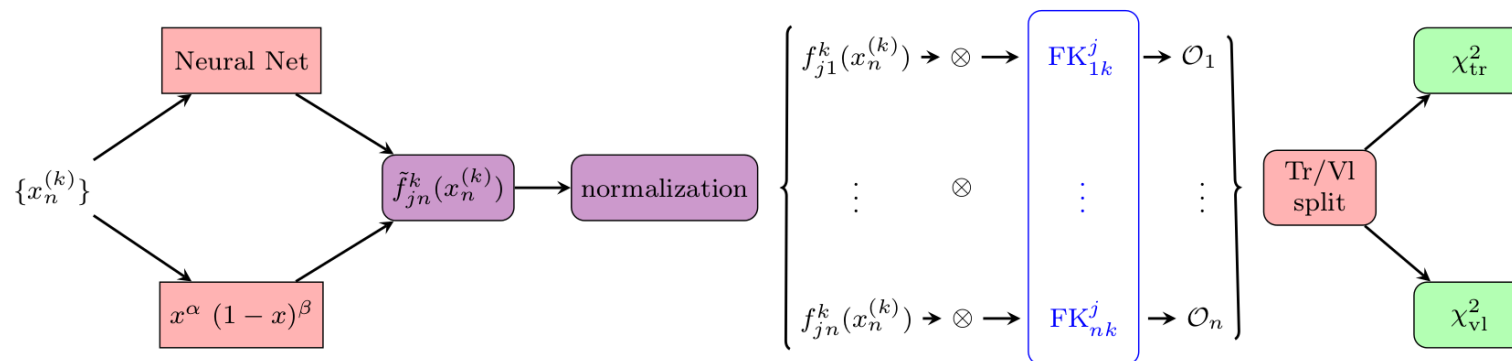
AVERAGE FITTING TIME PER REPLICAS AND USE OF RESOURCES
SAME DATASET FOR OLD AND NEW METHODOLOGIES IN CPU AND GPU
CPU: INTEL(R) CORE(TM) I7-4770 AT 3.40GHz; GPU: NVIDIA TITAN V

	NNPDF31 CODEBASE	NNPDF40 CODEBASE IN CPU	NNPDF40 CODEBASE IN GPU
TIME	15.2 H.	38 ± 5 MIN.	6.6 MIN.
RAM USE	1.5 GB	6.1 GB	NA

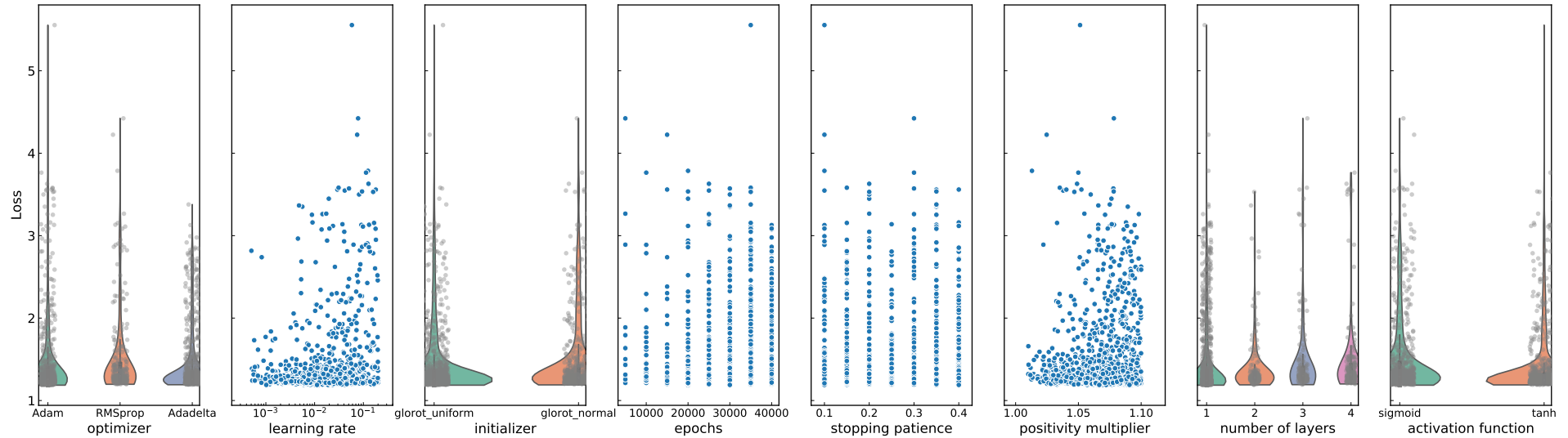


MINIMIZATION AND CROSS-VALIDATION

- DATA REPLICAS \Rightarrow PDF REPLICAS
- EACH PDF REPLICA: PREPROCESSED NEURAL NET
- NEURAL NET \Rightarrow OBSERVABLES
- RANDOM TRAINING-VALIDATION SPLIT, χ^2 TO TRAINING DATA REPLICAS MINIMIZED
- TRAINING STOPS IF VALIDATION χ^2 GROWS FOR A WHILE (PATIENCE)
- LOWEST VALIDATION $\chi^2 \Rightarrow$ OPTIMAL FIT



FITTING THE METHODOLOGY HYPEROPTIMIZATION SCANS



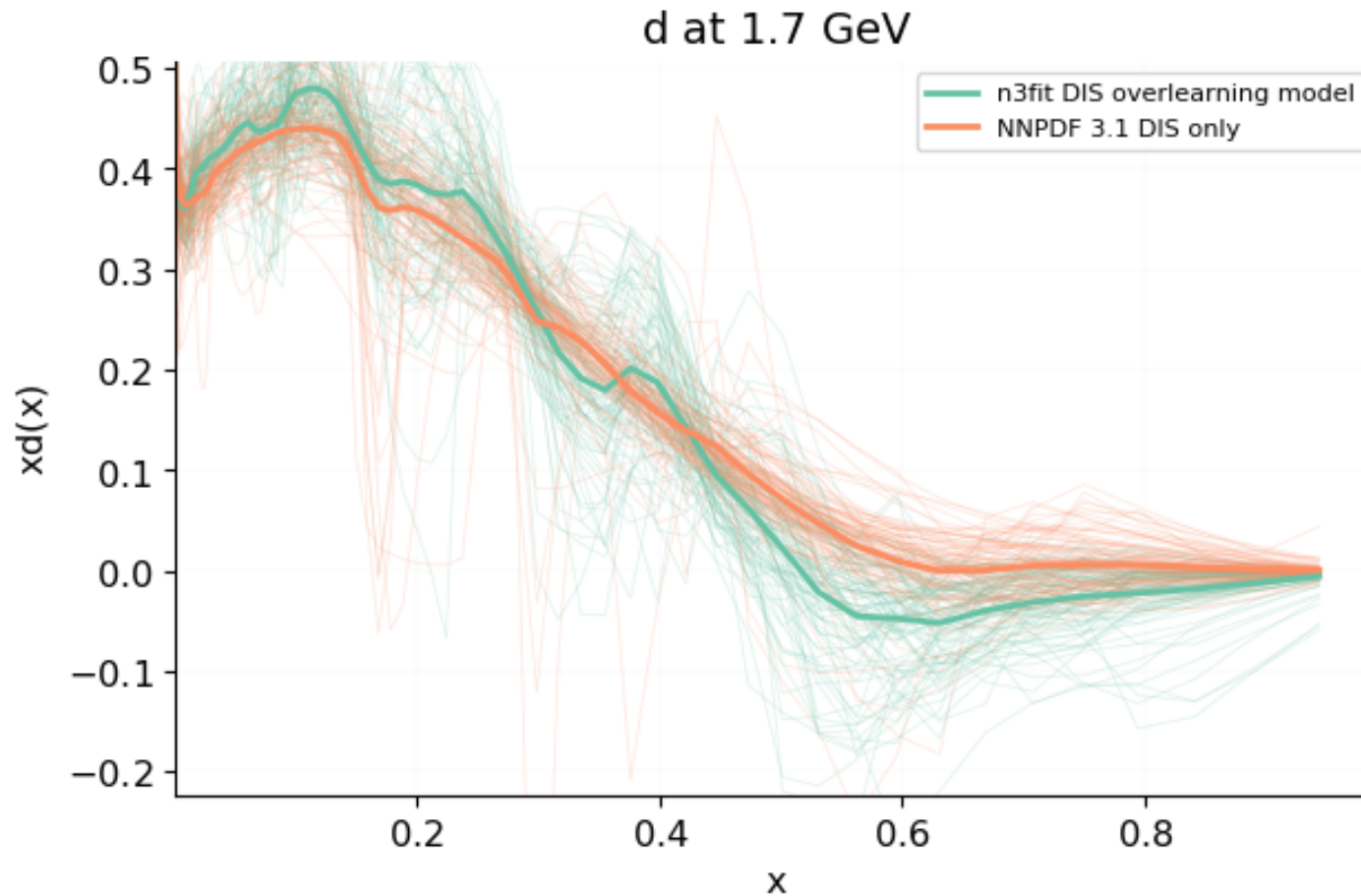
HYPEROPT PARAMETERS

NEURAL NETWORK	FIT OPTIONS
NUMBER OF LAYERS (*)	OPTIMIZER (*)
SIZE OF EACH LAYER	INITIAL LEARNING RATE (*)
DROPOUT	MAXIMUM NUMBER OF EPOCHS (*)
ACTIVATION FUNCTIONS (*)	STOPPING PATIENCE (*)
INITIALIZATION FUNCTIONS (*)	POSITIVITY MULTIPLIER (*)

- **SCAN** PARAMETER SPACE
- **OPTIMIZE** FIGURE OF MERIT: **VALIDATION** χ^2
- **BAYESIAN** UPDATING

HYPEROPTIMIZATION: OVERFITTING

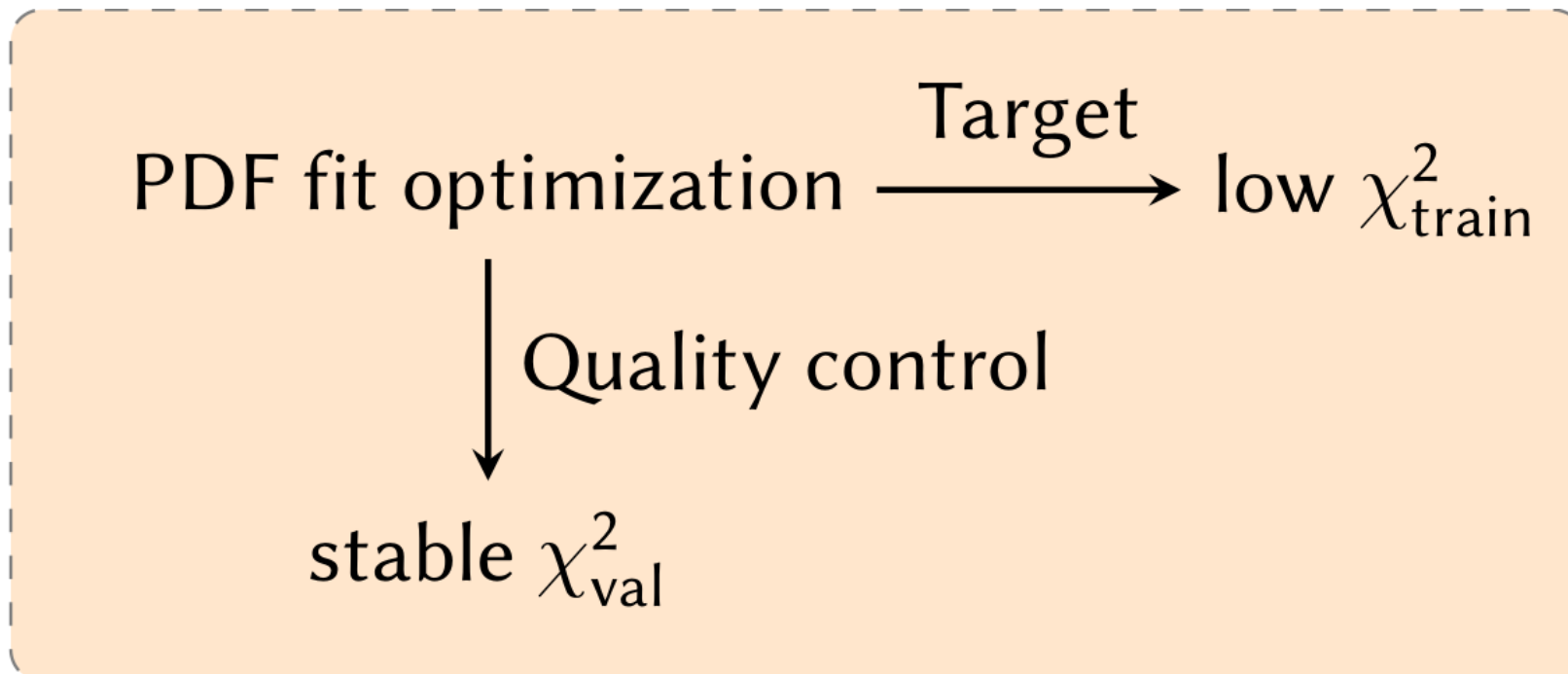
DOWN QUARK: HYPEROPTIMIZED VS. HAND-PICKED



- **NOT HYPEROPTIMIZED: WIGGLES: FINITE SIZE** \Rightarrow WILL GO AWAY AS N_{rep} GROWS
- **N3FIT: WIGGLY PDFS** \Leftrightarrow **OVERFITTING** \Rightarrow WILL **NOT** GO AWAY ($\chi^2_{\text{train}} \ll \chi^2_{\text{valid}}$!!)

WHAT HAPPENED?

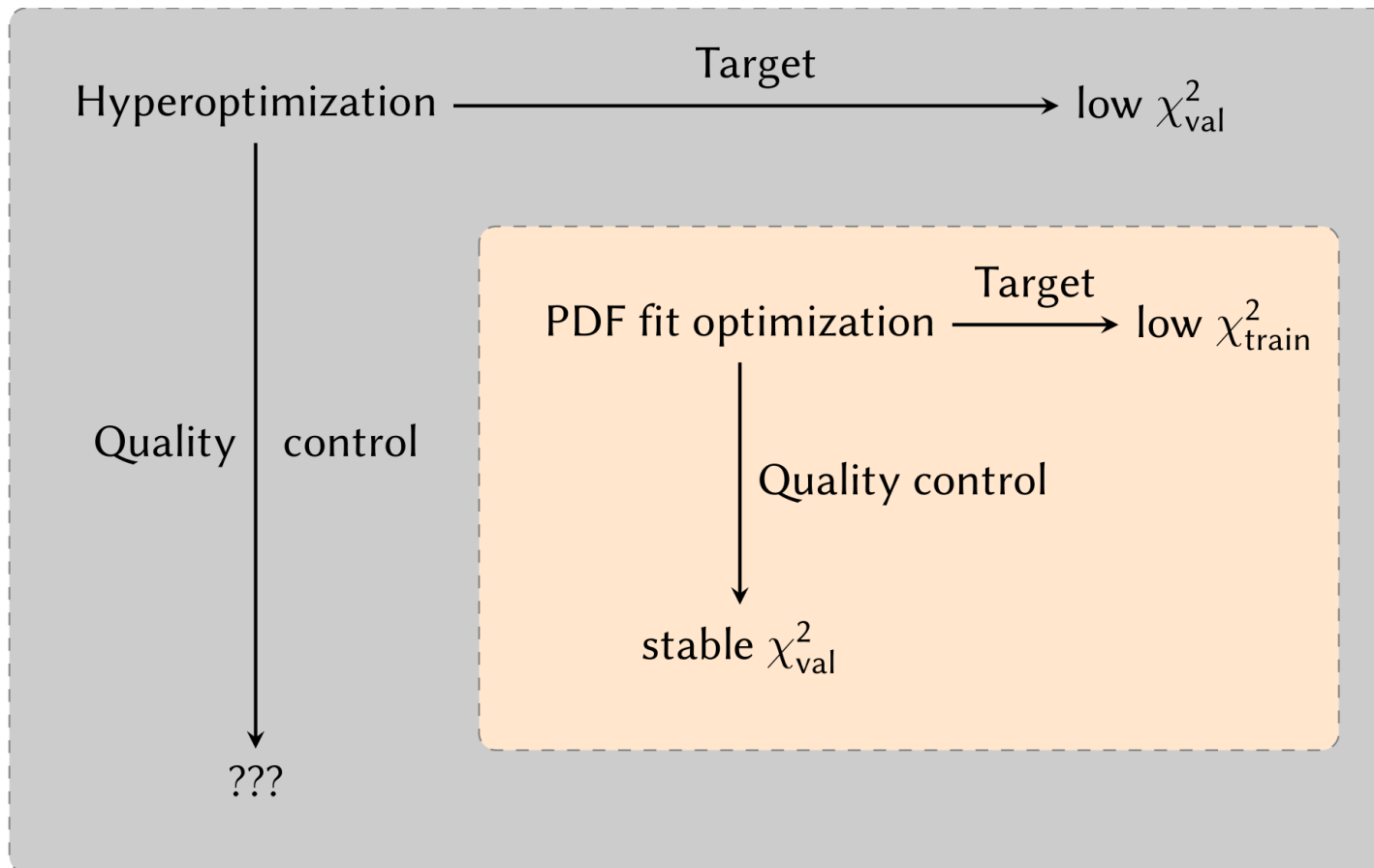
OPTIMIZATION



CROSS-VALIDATION SELECTS THE OPTIMAL MINIMUM

WHAT HAPPENED?

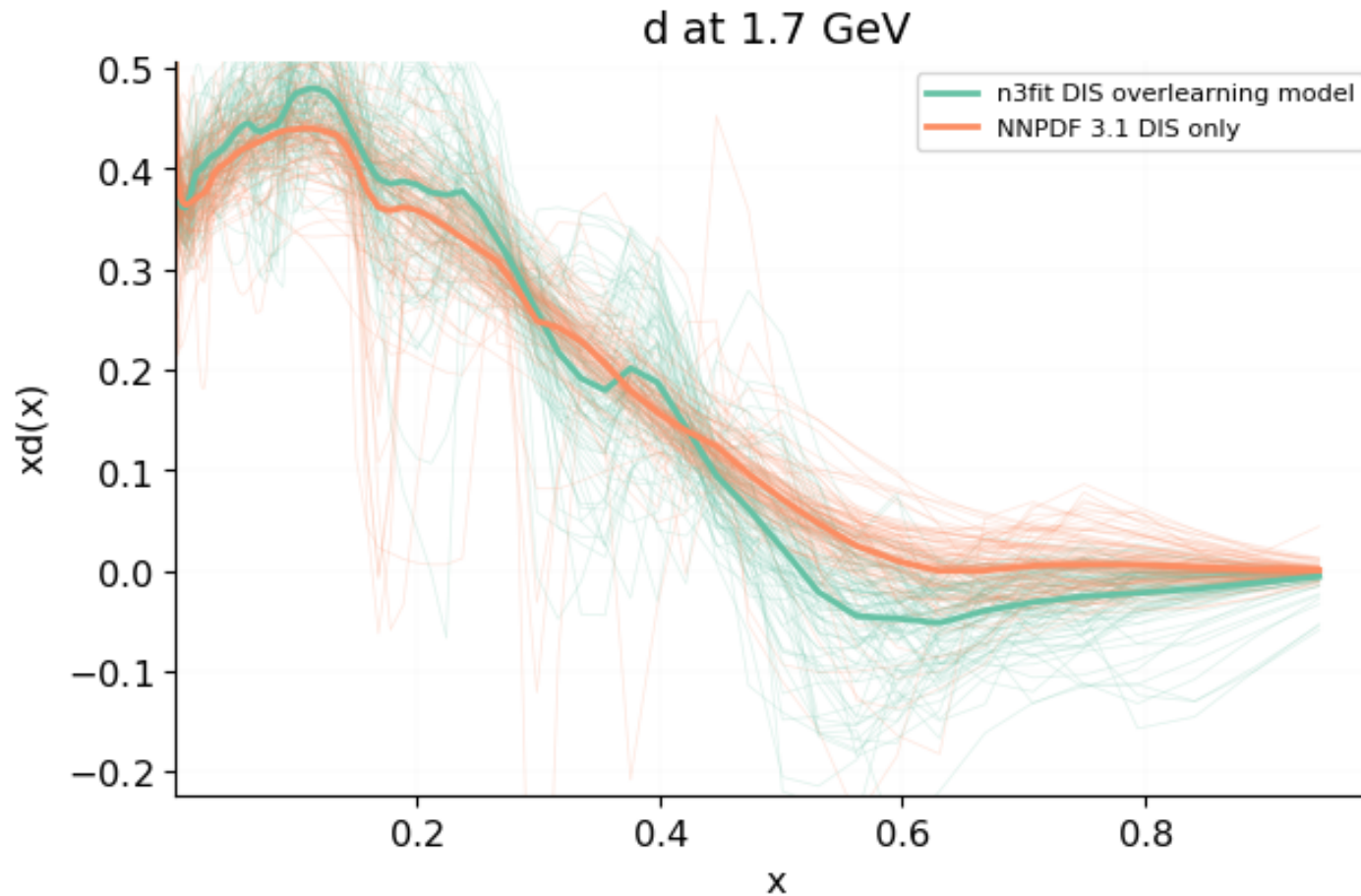
HYPEROPTIMIZATION



WE ARE MISSING A SELECTION CRITERION

HYPEROPTIMIZATION: OVERFITTING

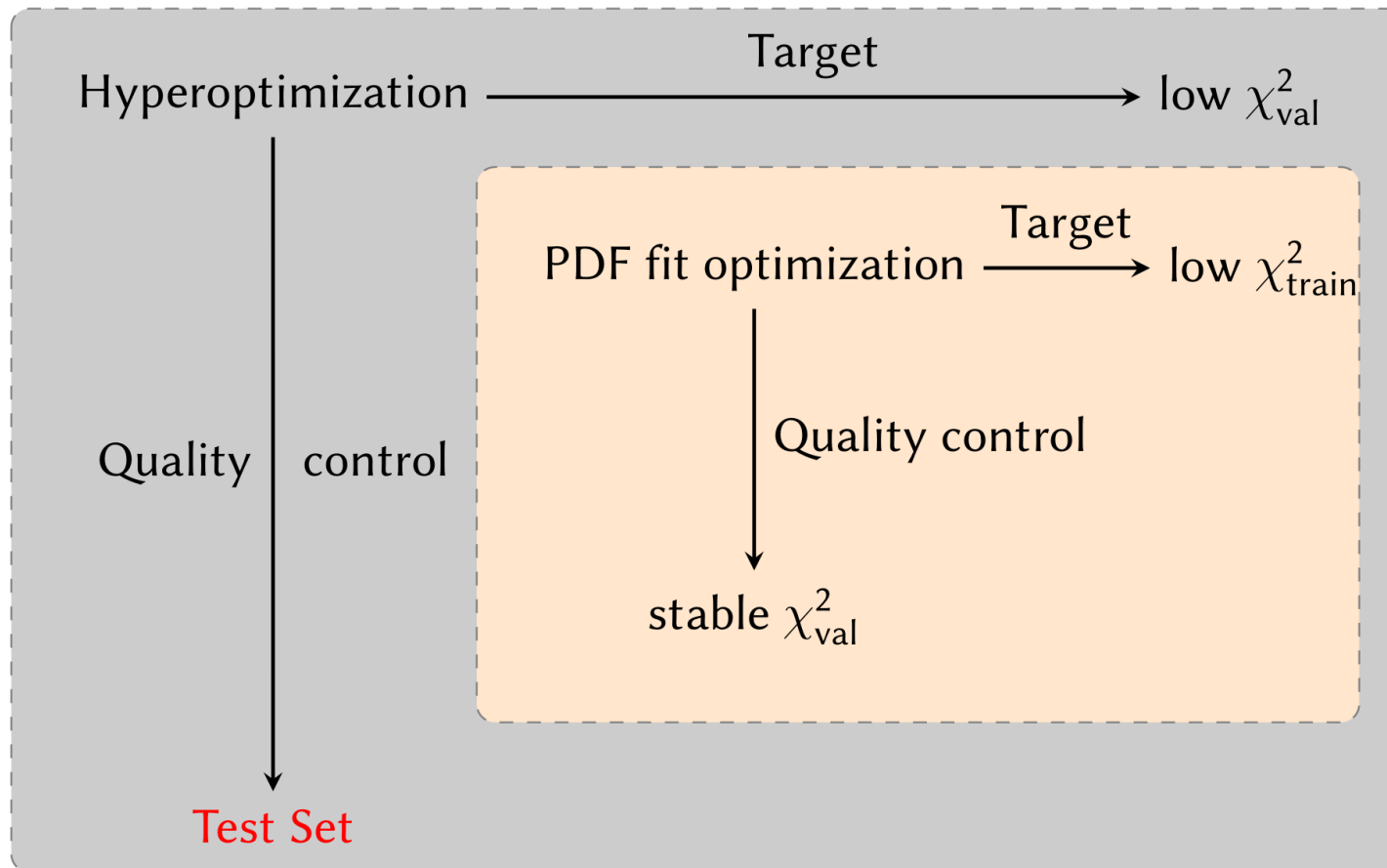
DOWN QUARK: HYPEROPTIMIZED VS. HANDPICKED



- **HANDPICKED:** WIGGLES: FINITE SIZE \Rightarrow WILL GO AWAY AS N_{rep} GROWS
- **N3FIT:** WIGGLY PDFS \Leftrightarrow OVERFITTING \Rightarrow WILL **NOT** GO AWAY ($\chi_{\text{train}}^2 \ll \chi_{\text{valid}}^2$!!)
- **CORRELATIONS** BETWEEN TRAINING AND VALIDATION DATA

THE SOLUTION

TUNED HYPEROPTIMIZATION

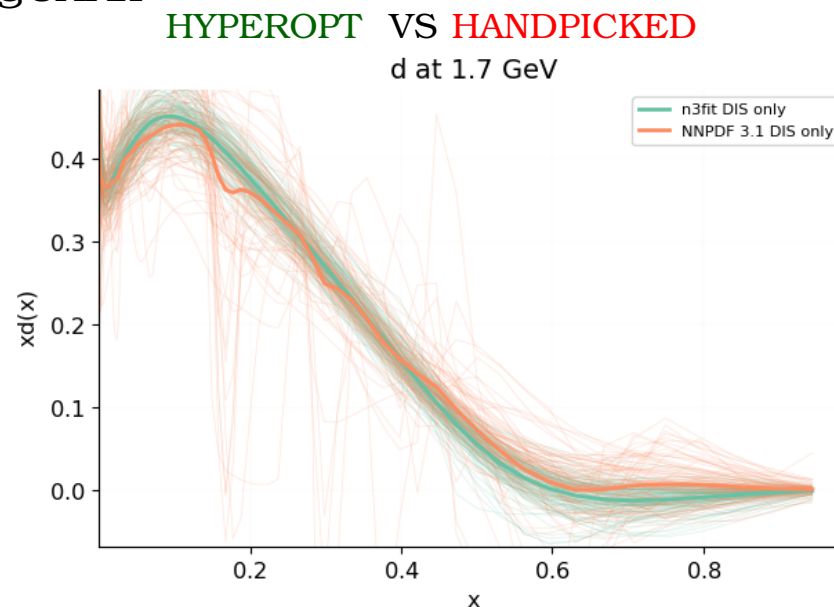
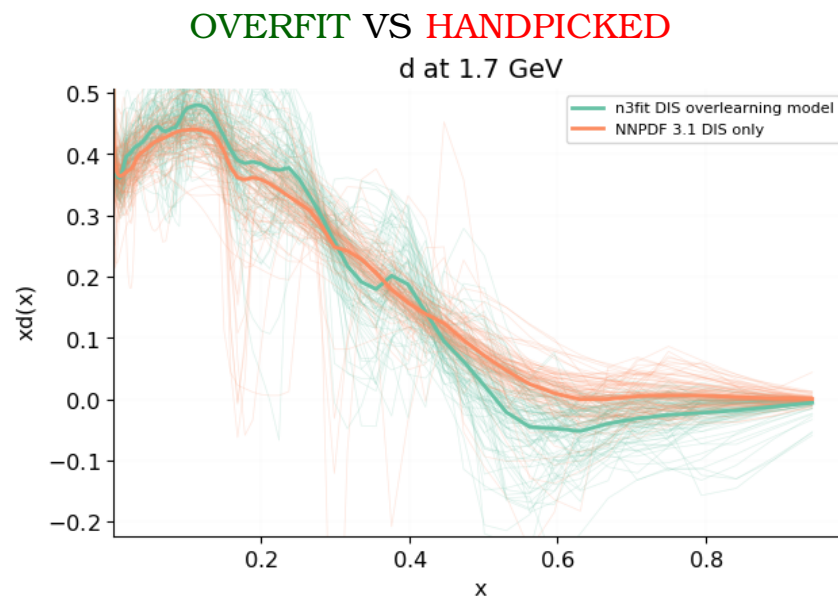


COMPARE TO A **A TEST SET** (NEW SET OF DATA PREVIOUSLY NOT USED AT ALL)
TESTS **GENERALIZATION POWER**

THE TEST SET METHOD

- COMPLETELY UNCORRELATED TEST SET
- OPTIMIZE ON WEIGHTED AVERAGE OF VALIDATION AND TEST
⇒ NO OVERLEARNING

HYPEROPTIMIZED PDFs DOWN QUARK



- NO OVERFITTING
- COMPARED TO HANDPICKED
 - MUCH GREATER STABILITY ⇒ FEWER REPLICAS FOR EQUAL ACCURACY
 - UNCERTAINTIES SOMEWHAT REDUCED

K-FOLDING

THE BASIC IDEA:

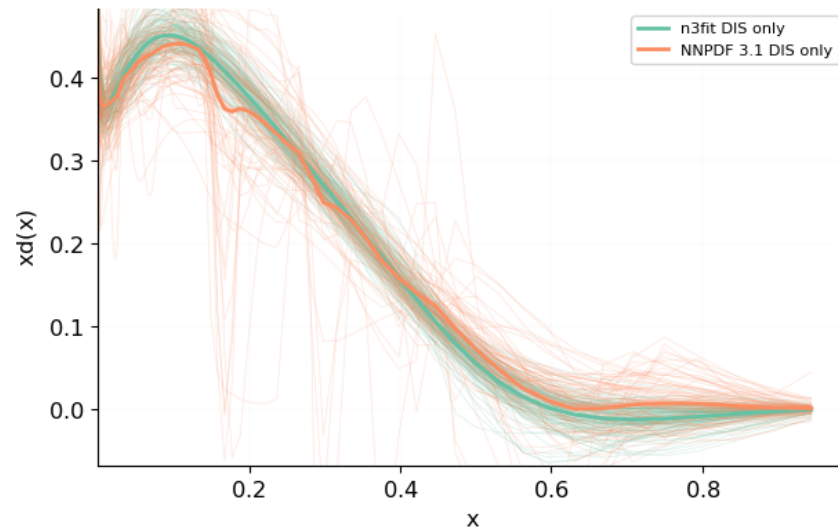
- DIVIDE THE DATA INTO n REPRESENTATIVE SUBSETS
EACH CONTAINING PROCESS TYPES, KINEMATIC RANGE OF FULL SET
- FIT $n - 1$ SETS AND USE n -TH SET AS TEST
 $\Rightarrow n$ VALUES OF $\chi^2_{\text{test}, i}$
- HYPEROPTIMIZE ON NON FITTED $\chi^2_{\text{test}, i}$
 \rightarrow GOOD & STABLE GENERALIZATION

FOLDED PDFs

DOWN QUARK

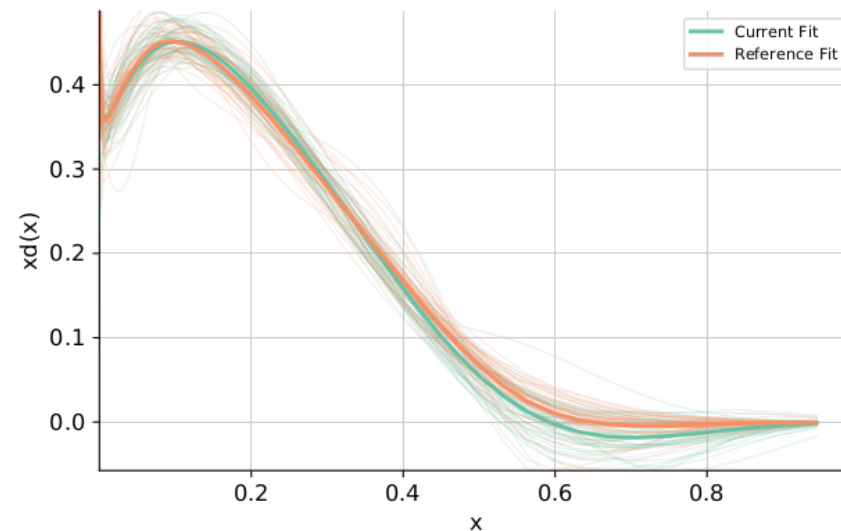
TEST-SET HYPER VS HANDPICKED

d at 1.7 GeV

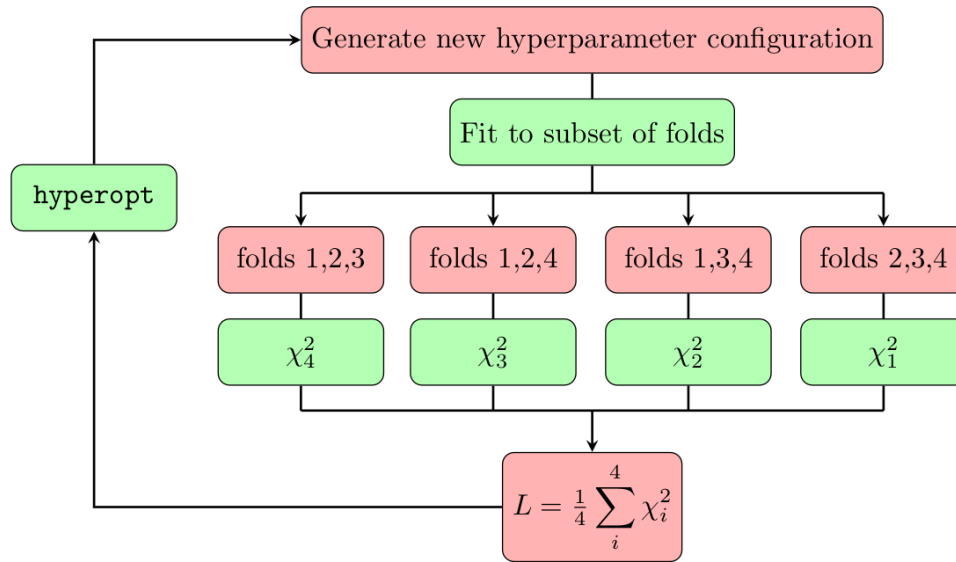


K-FOLD HYPER VS. TEST-SET HYPER

d at 1.7 GeV



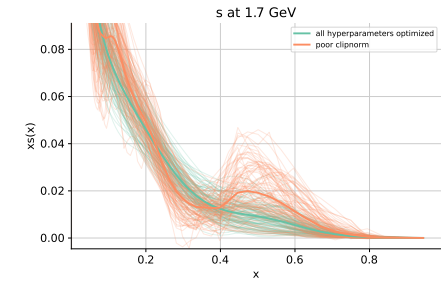
K-FOLDING IMPLEMENTATION



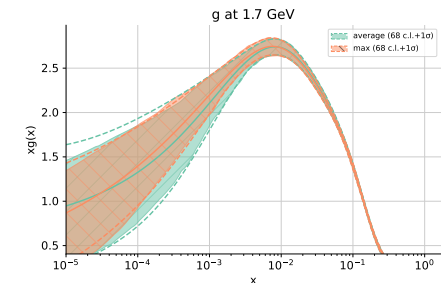
- EACH FOLD REPRODUCES FEATURES OF FULL DATASET
- DIFFERENT CHOICES POSSIBLE FOR LOSS (NON-FITTED)
 - BEST WORST
 - BEST AVERAGE
- RESULTS STABLE

Fold 1		
CHORUS σ_{CC}^e	HERA I+II inc NC e^+p 920 GeV	BCDMS p
LHCb Z 940 pb	ATLAS W, Z 7 TeV 2010	CMS Z pp 8 TeV (p_T^Z, y_{int})
DY E605 σ_{DY}^e	CMS Drell-Yan 2D 7 TeV 2011	CMS 3D dijets 8 TeV
ATLAS single- t y (normalised)	ATLAS single top R_t 7 TeV	CMS $t\bar{t}$ rapidity $y_{t\bar{t}}$
CMS single top R_t 8 TeV		
Fold 2		
HERA I+II inc CC e^-p	HERA I+II inc NC e^+p 460 GeV	HERA comb. σ_{bb}^{ind}
NMC p	NuTeV σ_e^p	LHCb $Z \rightarrow ee$ 2 fb
CMS W asymmetry 840 pb	ATLAS Z pp 8 TeV (p_T^Z, M_{ll})	D0 $W \rightarrow \mu\nu$ asymmetry
DY E886 σ_{DY}^e	ATLAS direct photon 13 TeV	ATLAS dijets 7 TeV, $R=0.6$
ATLAS single antitop y (normalised)	CMS σ_{tt}^{int}	CMS single top $\sigma_t + \sigma_{\bar{t}}$ 7 TeV
Fold 3		
HERA I+II inc CC e^+p	HERA I+II inc NC e^+p 575 GeV	NMC d/p
NuTeV σ_e^p	LHCb $W, Z \rightarrow \mu\tau$ 7 TeV	LHCb $Z \rightarrow ee$
ATLAS W, Z 7 TeV 2011 Central selection	ATLAS W^+ +jet 8 TeV	ATLAS HM DY 7 TeV
CMS W asymmetry 4.7 fb	DYE 866 $\sigma_{DY}^d/\sigma_{DY}^p$	CDF Z rapidity (new)
ATLAS σ_{tt}^{int}	ATLAS single top y_t (normalised)	CMS σ_{tt}^{int} 5 TeV
CMS $t\bar{t}$ double diff. ($m_{t\bar{t}}, y_t$)		
Fold 4		
CHORUS σ_{CC}^e	HERA I+II inc NC e^+p 820 GeV	LHCb $W, Z \rightarrow \mu$ 8 TeV
LHCb $Z \rightarrow \mu\mu$	ATLAS W, Z 7 TeV 2011 Fwd	ATLAS W^- +jet 8 TeV
ATLAS low-mass DY 2011	ATLAS Z pp 8 TeV (p_T^Z, y_{int})	CMS W rapidity 8 TeV
D0 Z rapidity	CMS dijets 7 TeV	ATLAS single top y_t (normalised)
ATLAS single top R_t 13 TeV	CMS single top R_t 13 TeV	

NO K-FOLDING



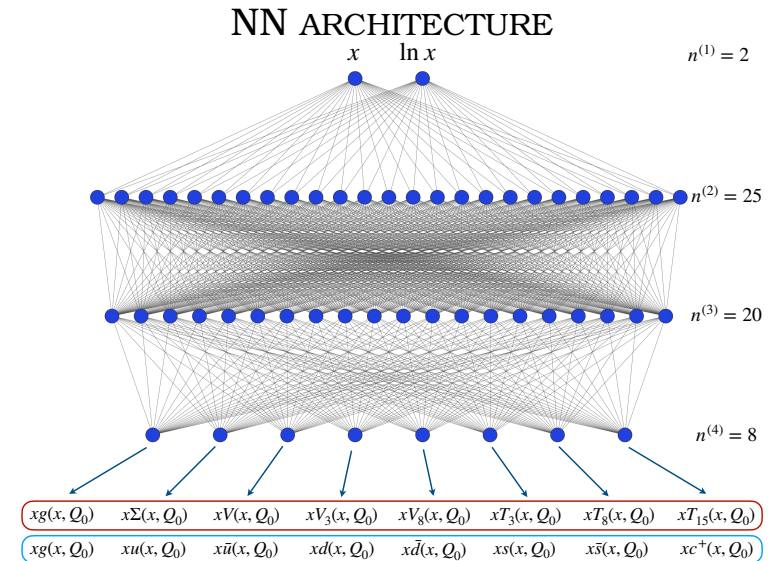
K-FOLDING VARIATION



THE ML METHODOLOGY

HYPEROPTIMIZED PARAMETERS

Parameter	NNPDF4.0	L as in Eq. (3.21)	Flavour basis Eq. (3.2)
Architecture	25-20-8	70-50-8	7-26-27-8
Activation function	hyperbolic tangent	hyperbolic tangent	sigmoid
Initializer	glorot_normal	glorot_uniform	glorot_normal
Optimizer	Nadam	Adadelta	Nadam
Clipnorm	6.0×10^{-6}	5.2×10^{-2}	2.3×10^{-5}
Learning rate	2.6×10^{-3}	2.5×10^{-1}	2.6×10^{-3}
Maximum # epochs	17×10^3	45×10^3	45×10^3
Stopping patience	10% of max epochs	12% of max epochs	16% of max epochs
Initial positivity $\Lambda^{(\text{pos})}$	185	106	2
Initial integrability $\Lambda^{(\text{int})}$	10	10	10



- HYPEROPT ADAPTS TO EXTERNAL CHOICES (E.G. PARAMETRIZATION BASIS)
- SIMILAR RESULTS CAN BE OBTAINED WITH RATHER DIFFERENT SETTINGS
- ~ 800 FREE PARAMETERS

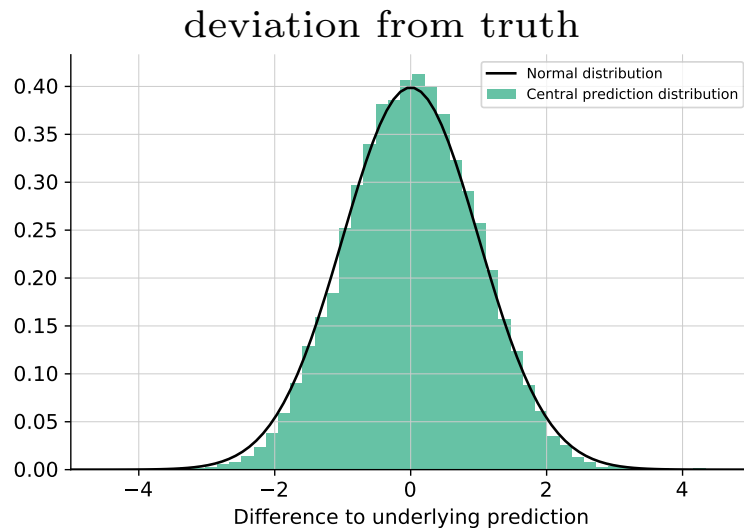
VALIDATION

CLOSURE TESTS

FAITHFUL UNCERTAINTIES IN DATA REGION?

- ASSUME “TRUE” UNDERLYING PDF \Rightarrow E.G. SOME RANDOM PDF REPLICA
- GENERATE DATA DISTRIBUTED ACCORDING TO EXPERIMENTAL COVARIANCE MATRIX
- RUN WHOLE METHDOLOGY ON THESE DATA
- DO STATISTICS ON “RUNS OF THE UNIVERSE”, POSSIBLE THANKS TO EFFICIENT METHDOLOGY: COMPARE TO TRUE PDFS, OR TO TRUE VALUES OF OBSERVABLES (NOT FITTED)
 - BIAS/VARIANCE: MEAN SQUARE DEVIATION WR TO TRUTH VS UNCERTAINTY
 - IS TRUTH WITHIN ONE SIGMA 68% OF TIMES?

RESULTS



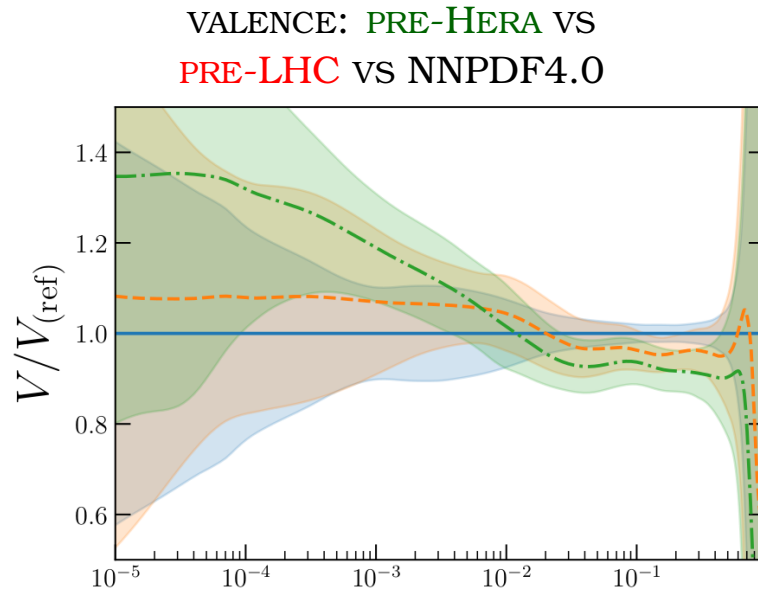
Dataset	$\sqrt{\text{bias/variance}}$	$\xi_{1\sigma}^{(\text{data})}$
DY	0.99 ± 0.08	0.69 ± 0.02
Top-pair	0.75 ± 0.06	0.75 ± 0.03
Jets	1.14 ± 0.05	0.63 ± 0.03
Dijets	0.99 ± 0.07	0.70 ± 0.03
Direct photon	0.71 ± 0.06	0.81 ± 0.03
Single top	0.87 ± 0.07	0.69 ± 0.04
Total	1.03 ± 0.05	0.68 ± 0.02

FUTURE TESTS

FAITHFUL UNCERTAINTIES IN EXTRAPOLATION?

- DETERMINE PDFs FROM A SUBSET OF CURRENT DATA: “PRE-HERA”, “PRE-LHC”,...
- COMPUTE χ^2 TO THE FULL CURRENT DATASET:
 - WITHOUT PDF UNCERTAINTIES \Rightarrow IF $\gg 1$, MISSING INFORMATION
 - WITH PDF UNCERTAINTY \Rightarrow IF ~ 1 , MISSING INFO REPRODUCED BY UNCERTAINTY

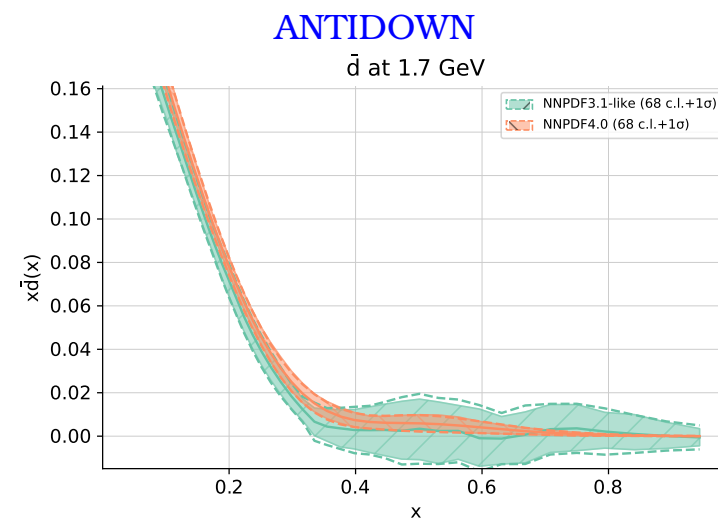
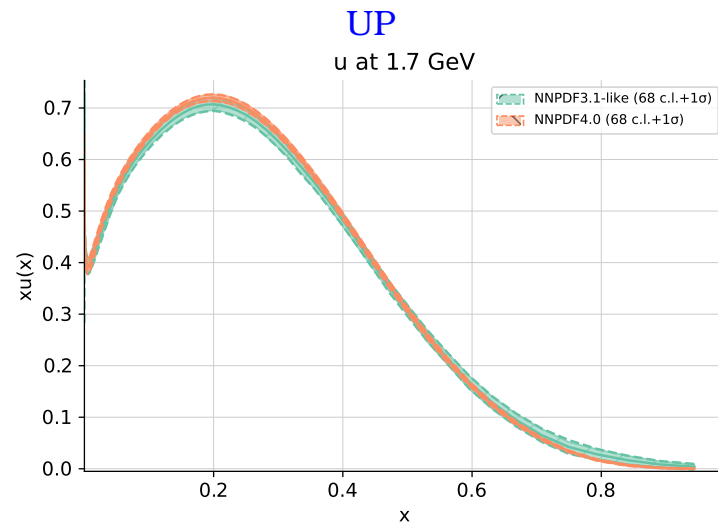
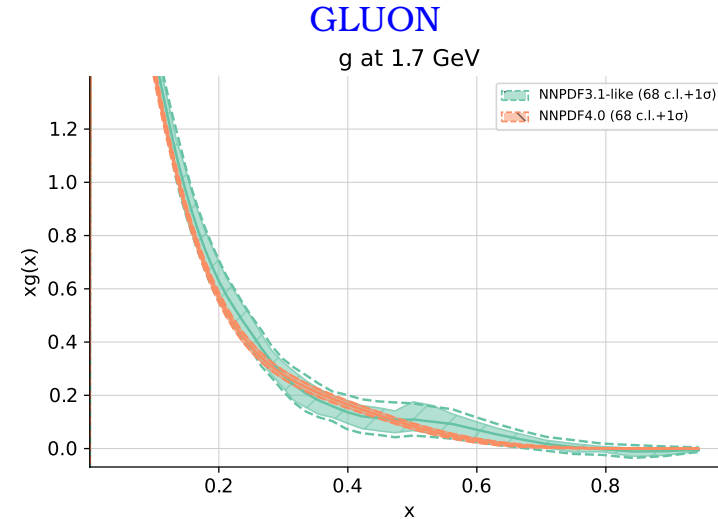
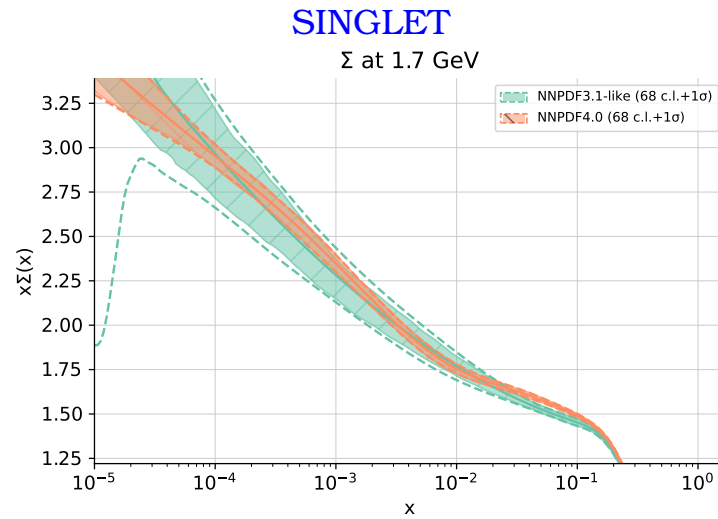
χ^2 WITHOUT/WITH PDF UNC.



PROCESS	PRE-HERA	PRE-LHC	3.1-LIKE	4.0-GLOB
FT DIS (NC)	1.04	1.17	1.17	1.26
FT DIS (CC)	0.80	0.86	0.88	0.90
FT DY	0.93	1.27	1.43	1.59
HERA	24.01/ 1.12	1.22	1.21	1.21
COLL. DY (TeV.)	5.31/ 1.08	0.96	0.95	1.13
COLL. DY (LHC)	15.50/ 1.37	2.64/ 1.54	1.39	1.54
TOP QUARK	23.35/ 1.08	1.29/ 0.86	0.82	0.98
JETS	6.18/ 1.21	3.66/ 1.29	2.07/ 1.37	1.26
TOTAL	9.70	1.44	1.22	1.17

NNPDF4.0 vs. NNPDF3.1

- FULL BACKWARD COMPATIBILITY
- SUBSTANTIAL REDUCTION IN UNCERTAINTY

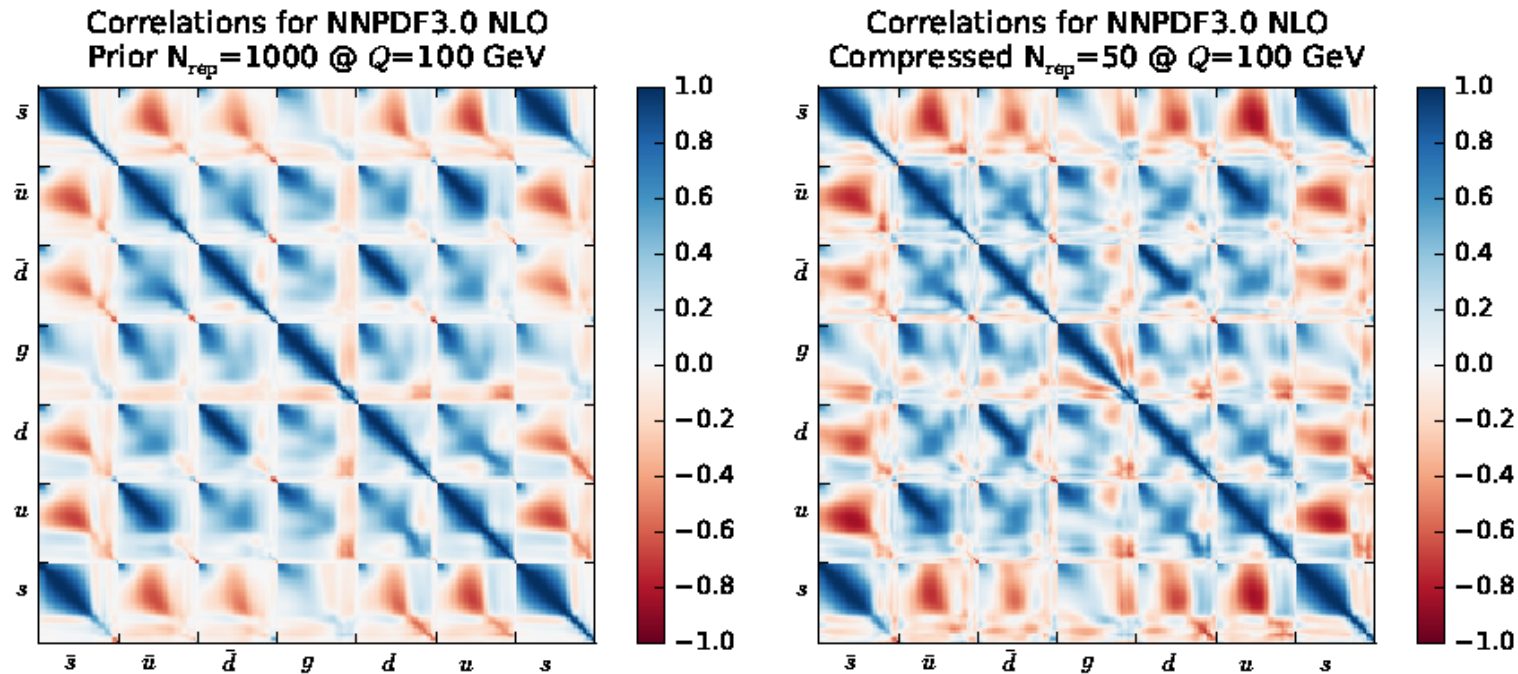


DELIVERY

MONTECARLO COMPRESSION

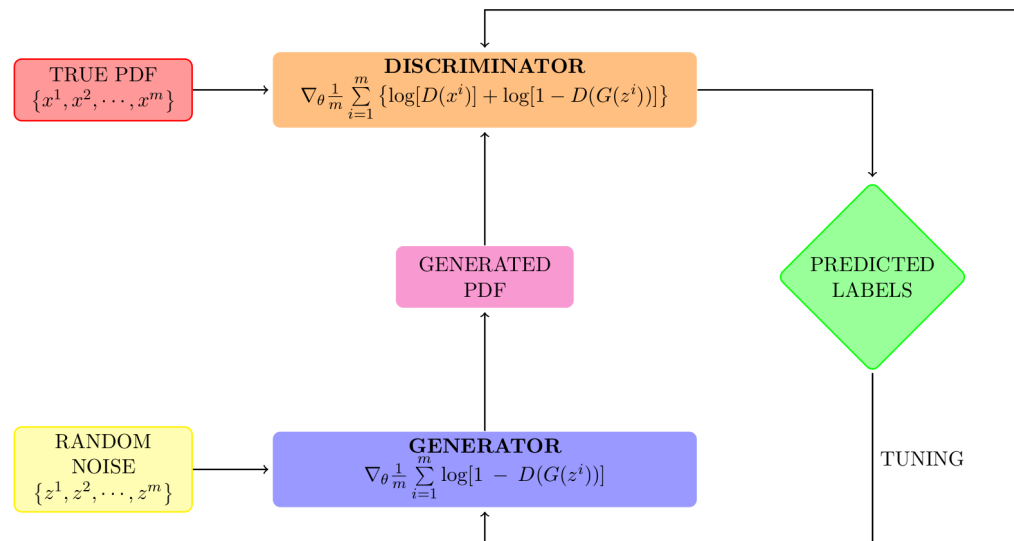
CAN WE REDUCE THE NUMBER OF REPLICAS?

- START WITH LARGE REPLICAS SAMPLE
- SELECT BY GENETIC ALGORITHM SUBSET OF REPLICAS \Rightarrow STATISTICAL FEATURES OPTIMIZED TO PRIOR
- MINIMIZE LOSS: DIFFERENCE OF MOMENTS, KL DIVERGENCE, ...
- 50 COMPRESSED REPLICAS REPRODUCE 1000 REPLICAS SET TO PRESENT ACCURACY



GAN ENHANCEMENT

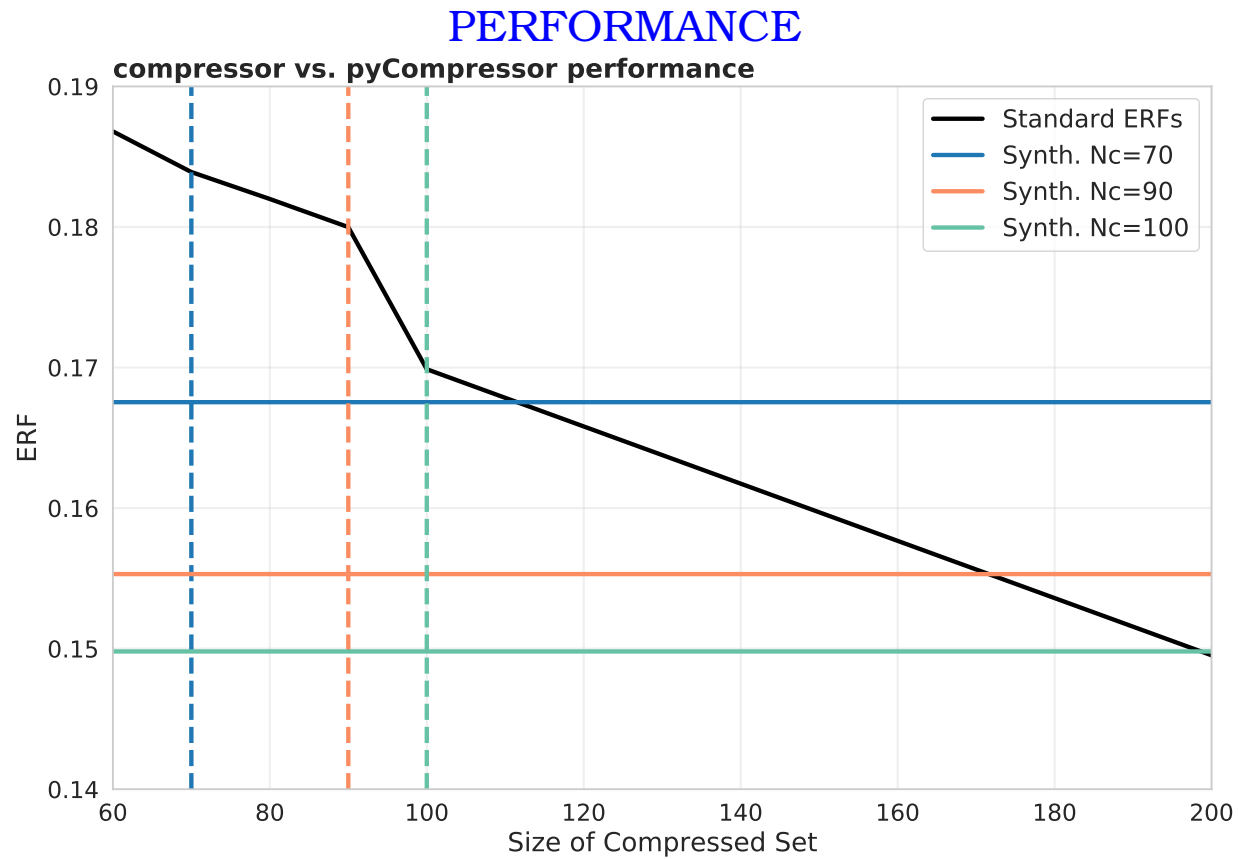
CAN WE FURTHER REDUCE THE NUMBER OF COMPRESSED REPLICAS WITHOUT LOSS OF INFORMATION? GENERATIVE ADVERSARIAL NETWORKS



- TRAIN A NETWORK TO **SIMULATE** THE TRUE DISTRIBUTION (**GENERATOR**)
- TRAIN A NETWORK TO **DISCRIMINATE** TRUTH FROM SIMULATION (**DISCRIMINATOR**)
- TRAIN THE **GENERATOR** TO **TRICK** THE **DISCRIMINATOR**

GAN ENHANCEMENT

- **ENHANCE** THE STARTING PDF SET BY ADDING GAN-PDFs TO IT
- **PERFORM COMPRESSION** OF THE ENHANCED SET

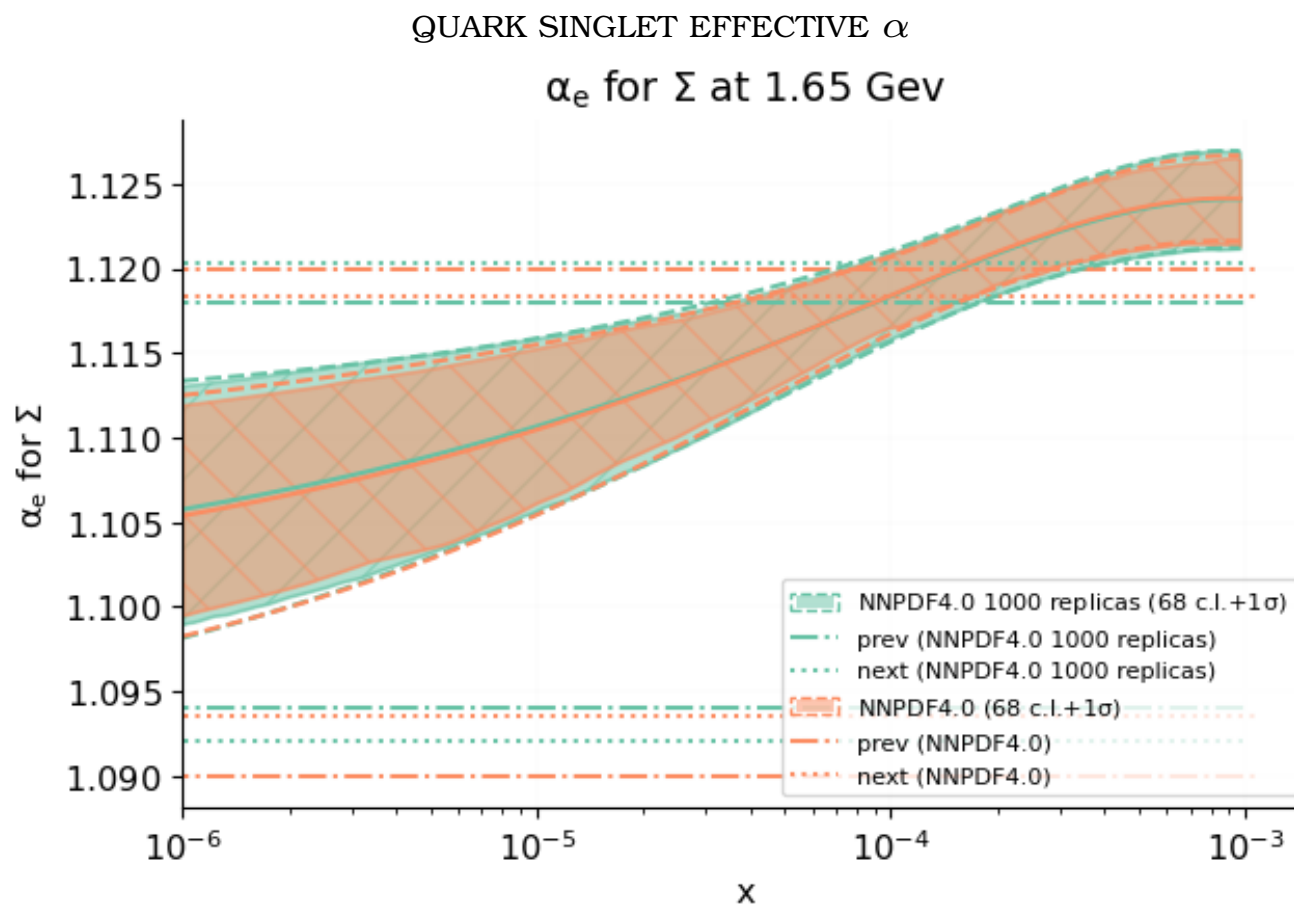


ENHANCED: NUMBER OF REPLICAS **CUT IN HALF** FOR SAME TARGET ACCURACY

NEW IDEAS

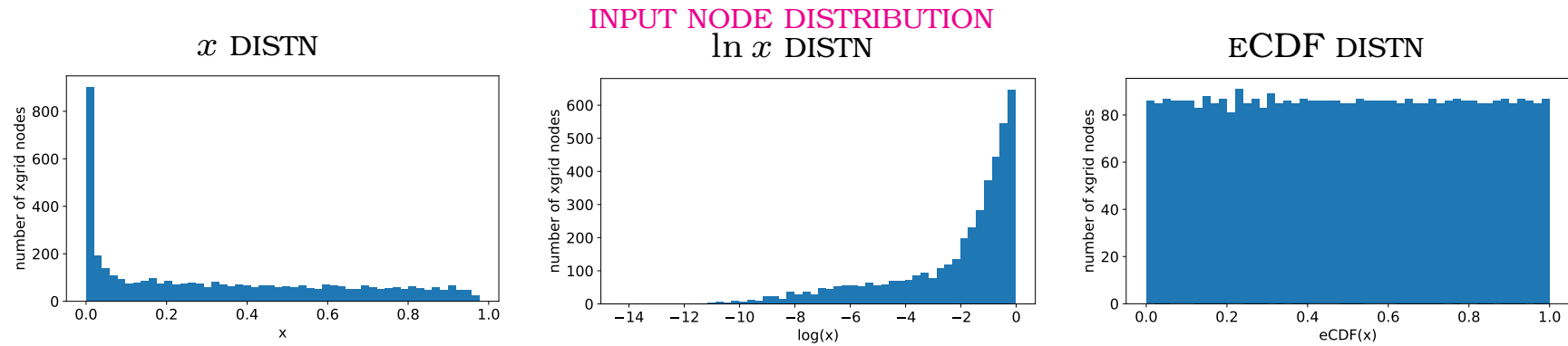
PREPROCESSING

- PDF EQUAL TO PREPROCESSED NN: $f_i = x^{\alpha_i} (1 - x)^{\beta_i} NN(i, x, \ln x)$
- PREPROCESSING EXPONENTS α_i, β_i VARIED RANDOMLY REPLICA BY REPLICA
- RANGE OF VARIATION DETERMINED SELF-CONSISTENTLY
- PDF TAKES $x, \ln x$ AS INPUTS

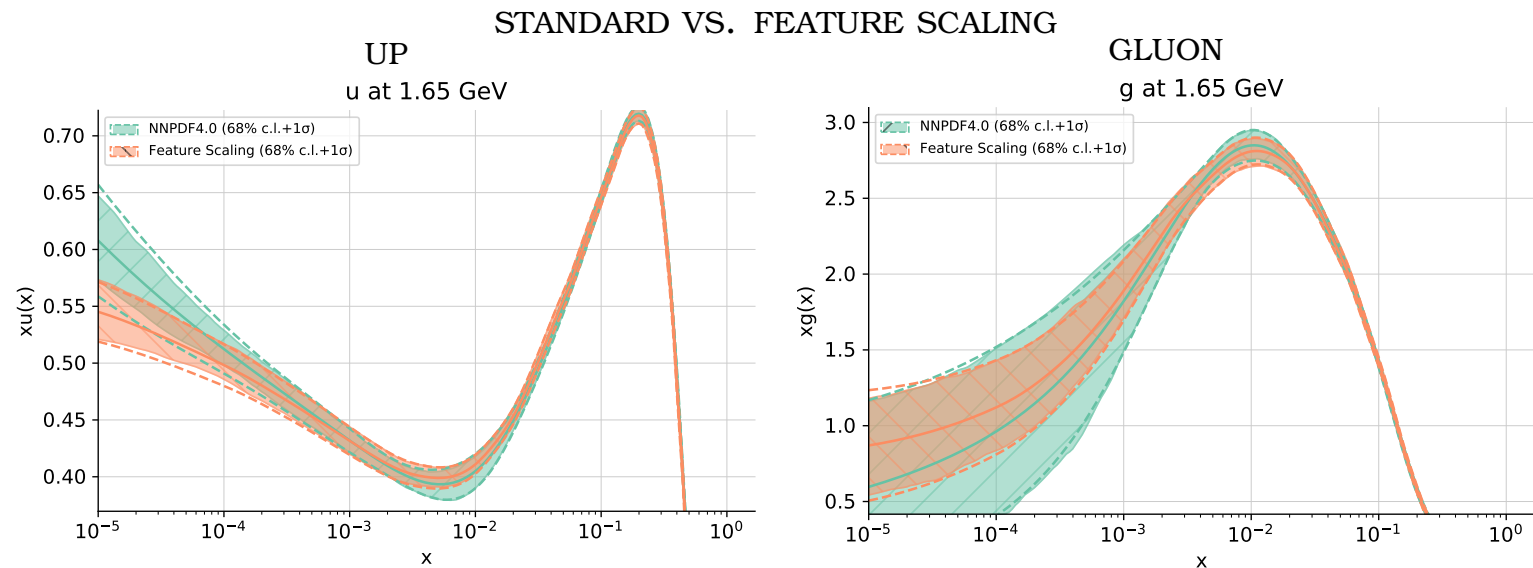


- NEED TO ITERATE FITS
- POSSIBLE SOURCE OF BIAS?

FEATURE SCALING



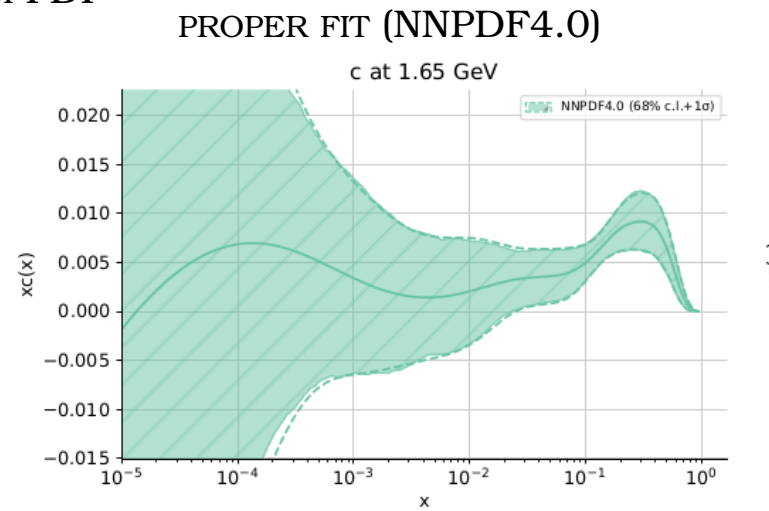
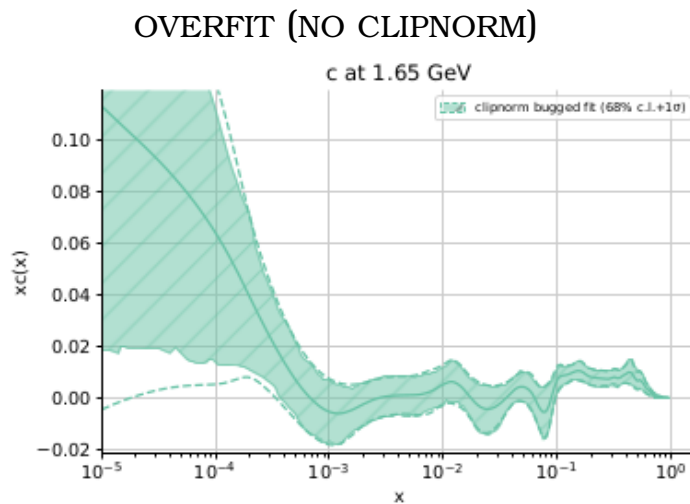
- **RESCALE** \Rightarrow **UNIFORMLY** DISTRIBUTED INPUT (ECDF+INTERPOLATION)
- RERUN **HYPEROPT**
- **ONLY ONE INPUT NEEDED**



OVERFITTING IN HYPEROPT

- HYPEROPT \Rightarrow OVERFITTING?
- WHAT IS A “NATURAL” PDF?

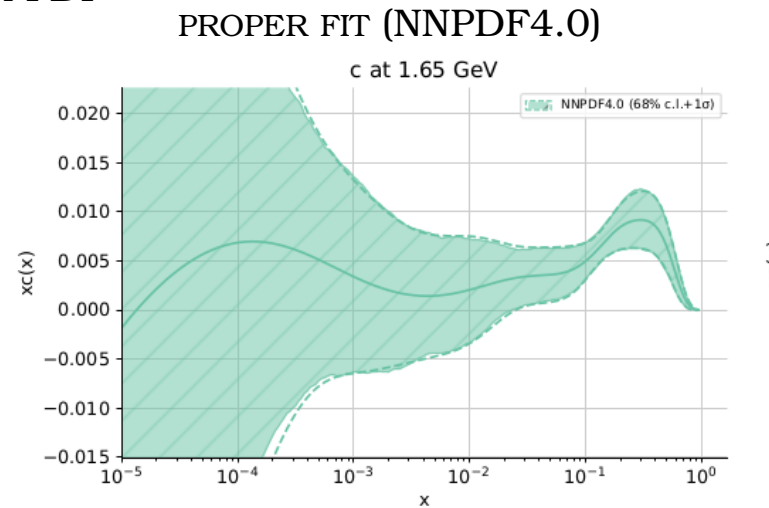
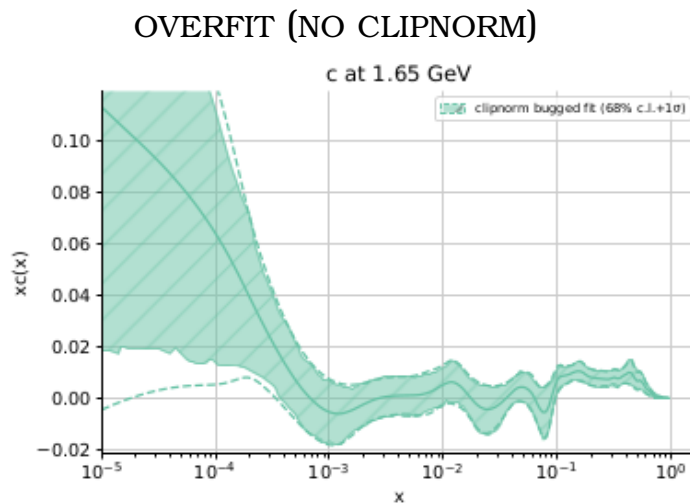
CHARM PDF



OVERFITTING METRIC

- RECOMPUTE VALIDATION χ^2
 - SAME TRAINING-VALIDATION SPLIT
 - DIFFERENT FLUCTUATED VALIDATION DATA
- COMPUTE AVERAGE χ^2 & DETERMINE DIFFERENCE TO VALIDATION $\mathcal{R}_O = \langle \chi_{\text{val}}^2 - \chi_{\text{val}'}^2 \rangle$
OVERFITNESS
- **NEGATIVE** OVERFITNESS $\mathcal{R}_O \Rightarrow$ OVERFIT

CHARM PDF



FOOD FOR THOUGHT

- OPTIMIZED FOLDS
- OVERFITTING AND UNDERFITTING METRICS IN HYPEROPT
- HYPEROPT ON FUTURE TESTS
- BEYOND NEURAL NETS

AN OPEN SOURCE CODE!

- THE **FULL** NNPDF CODE IS **PUBLIC!**
- INCLUDING HYPEROPTIMIZATION, EVOLUTION, THEORY, FITTING, VISUALIZATION
- **FULLY DOCUMENTED** CODE
- LINKS TO CODE (GITHUB), DOCUMENTATION, INSTALLATION BINARY PACKAGES AVAILABLE FROM
<http://nnpdf.mi.infn.it/nnpdf-open-source-code/>

<https://arxiv.org/abs/2109.02671>

An open-source machine learning framework for global analyses of parton distributions

The NNPDF Collaboration: Richard D. Ball · Stefano Carrazza · Juan Cruz-Martinez · Luigi Del Debbio · Stefano Forte · Tommaso Giani · Shayan Iranipour · Zahari Kassabov · Jose I. Latorre · Emanuele R. Nocera · Rosalyn L. Pearson · Juan Rojo · Roy Stegeman · Christopher Schwan · Maria Ubiali · Cameron Voisey · Michael Wilson

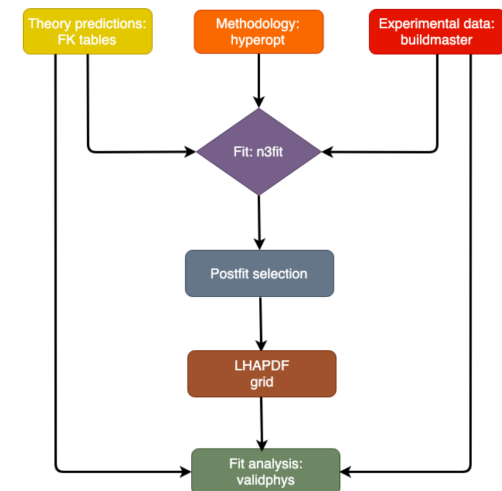


Fig. 2.1. Workflow for an NNPDF fit