

QCD THEORY

STEFANO FORTE
UNIVERSITÀ DI MILANO & INFN



UNIVERSITÀ DEGLI STUDI DI MILANO
DIPARTIMENTO DI FISICA



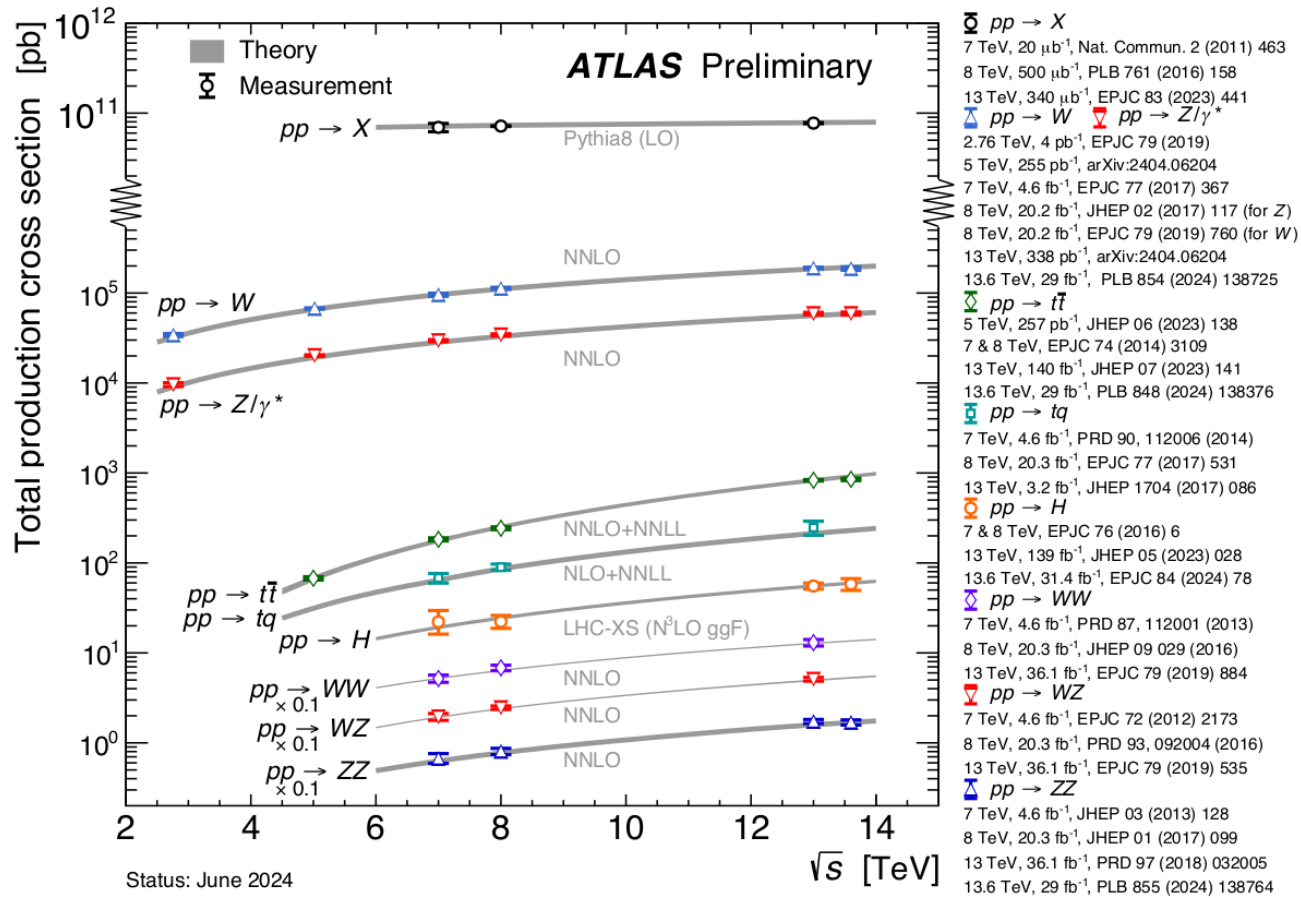
Istituto Nazionale di Fisica Nucleare

XXXI Cracow Epiphany Conference

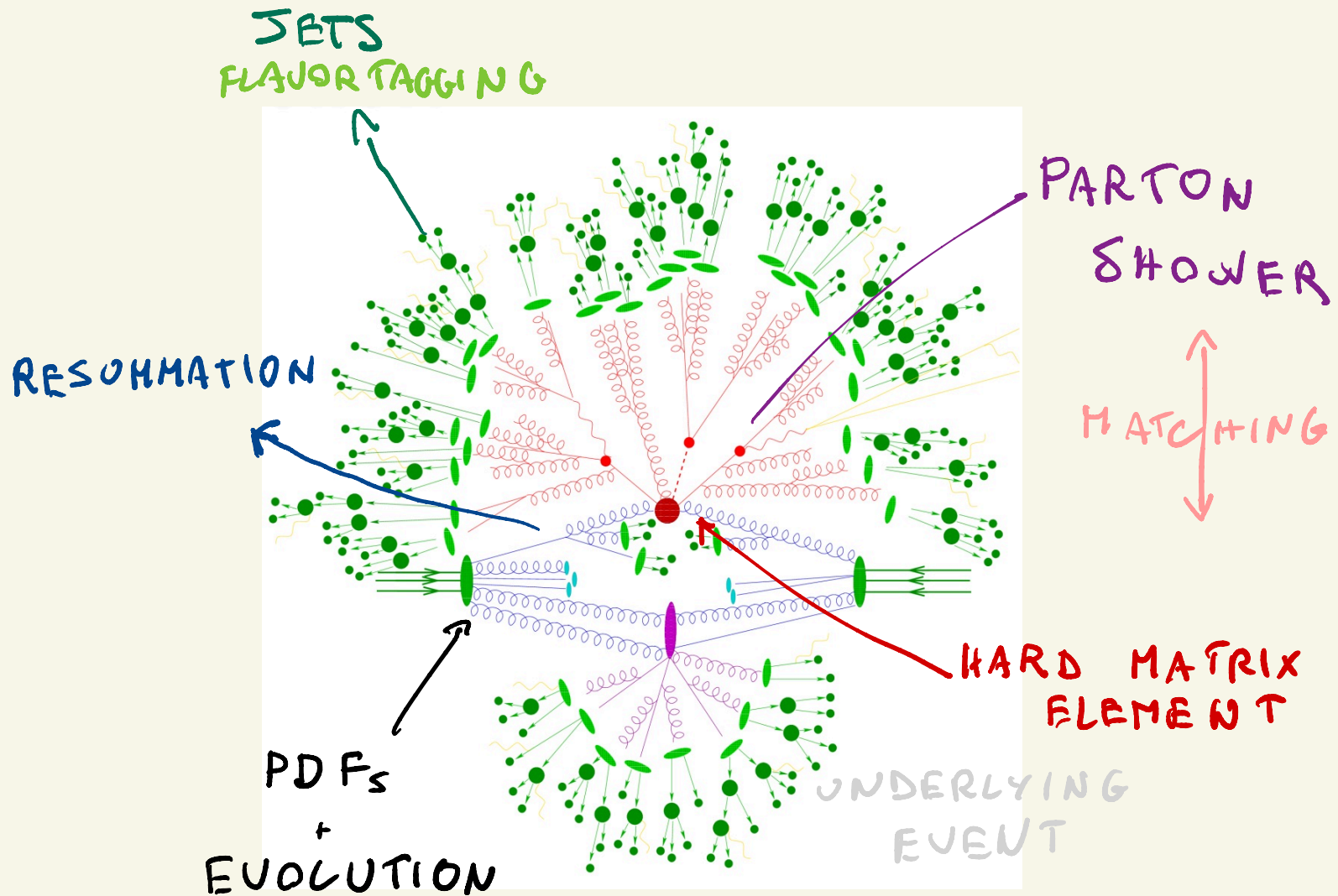
Krakow, 15 January 2025

LHC: THE FIRST PRECISION HADRON COLLIDER!

ATL-PHYS-PUB-2024-011



PRECISION FROM QCD!



MORE PRECISION THE HL-LHC... AND THE EIC



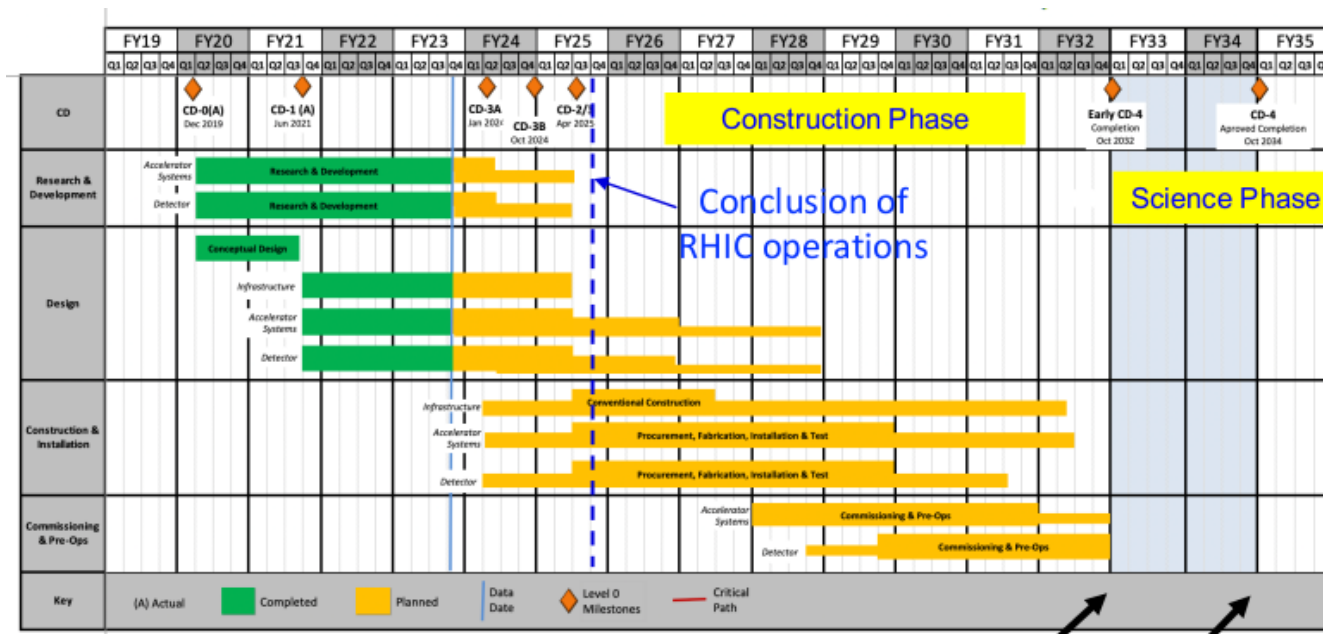
LHC / HL-LHC Plan



HL-LHC TECHNICAL EQUIPMENT:



HL-LHC CIVIL ENGINEERING:



QCD

- A TOOL FOR PRECISION PHYSICS
- A PATH TO THEORETICAL DISCOVERY

MOVING AHEAD THE FRONTIER

- BEYOND CURRENT PRECISION AND ACCURACY
- THE LHC CONFRONTS THE EIC: DIS REDUX
- STRETCHING THE CURRENT THEORY
- THE ERA OF MACHINE LEARNING

DISCLAIMER

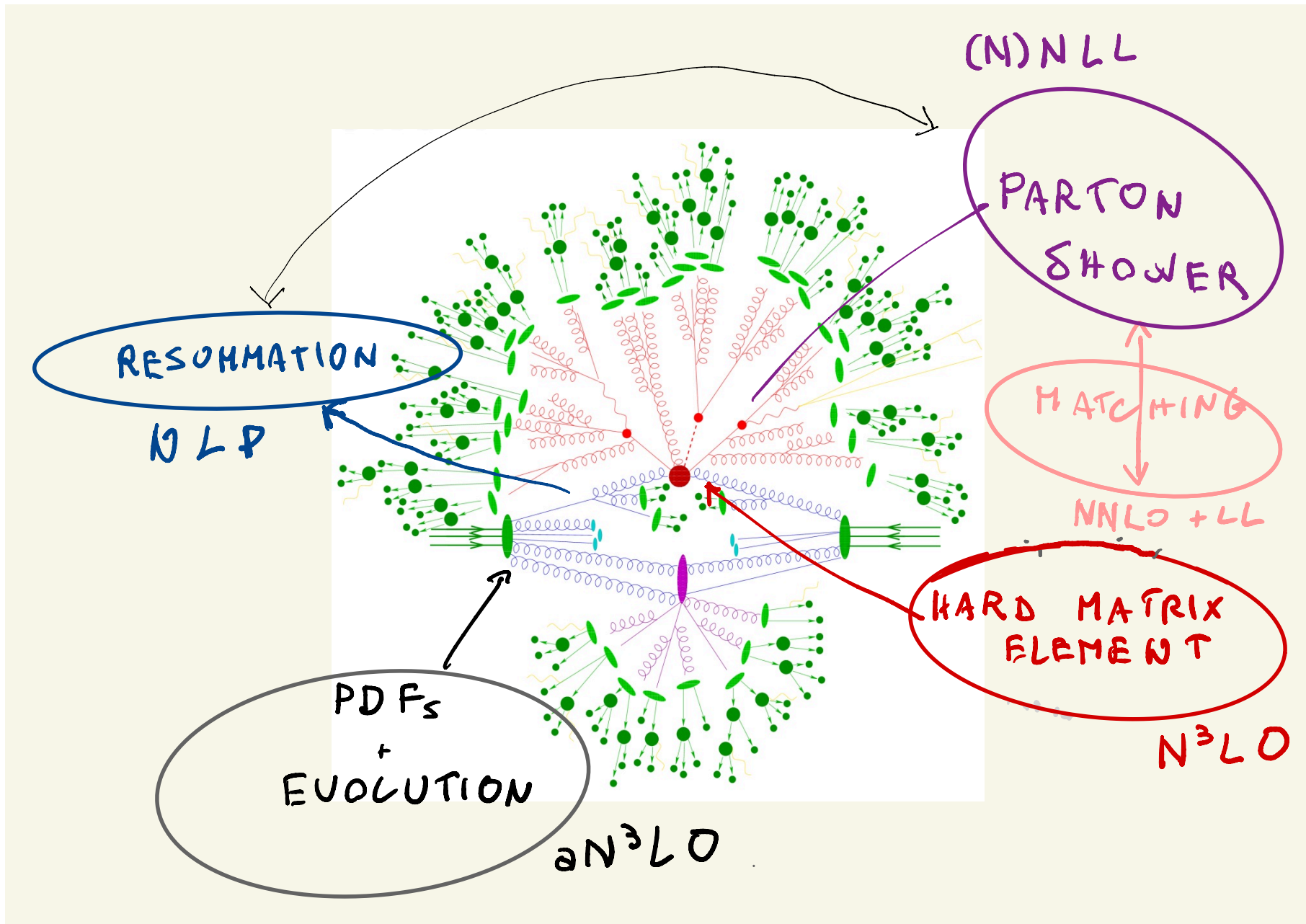
- A PERSONAL SELECTION OF RESULTS
- ONLY RECENT DEVELOPMENTS SINCE EARLY 2023 COVERED

STEFANO CATANI (1958-2024)

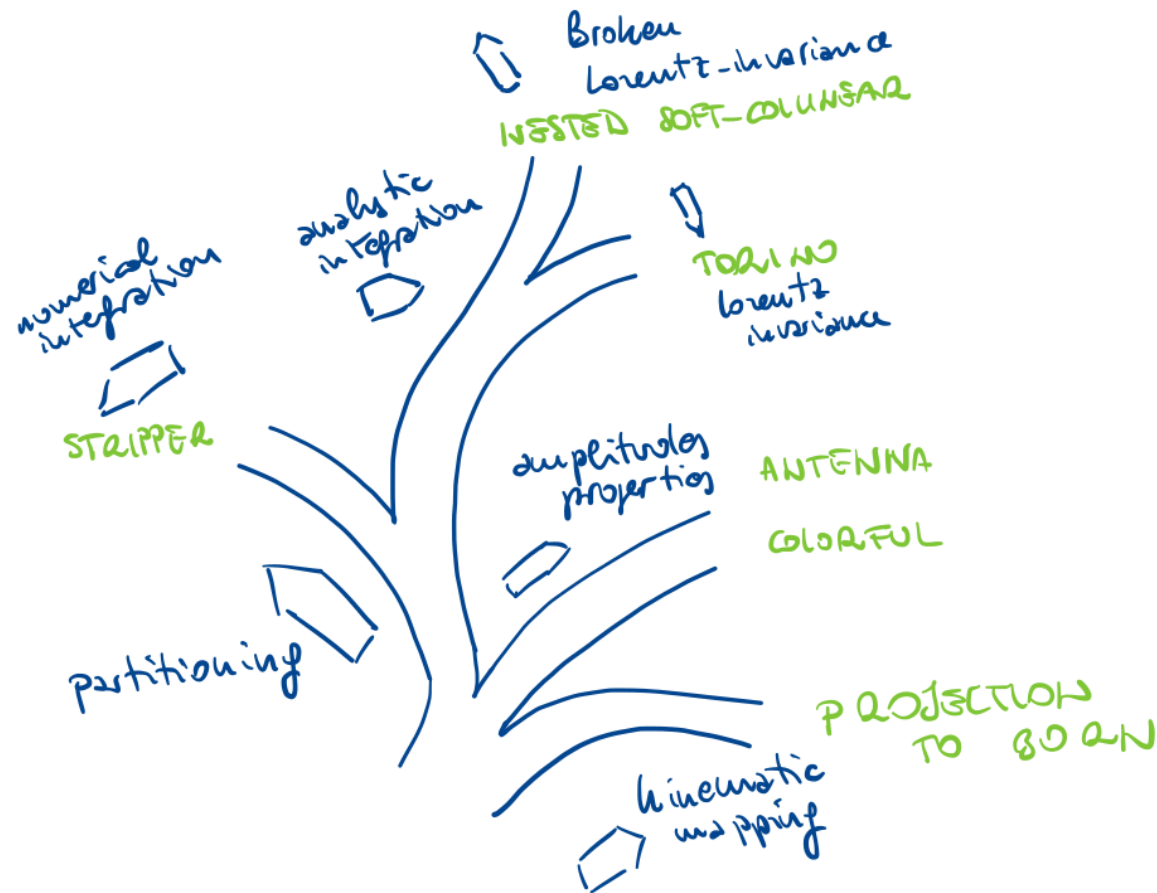


HIGHER PRECISION AND ACCURACY

THE PRECISION FRONTIER



THE AMPLITUDE REVOLUTION NNLO SUBTRACTION METHODS

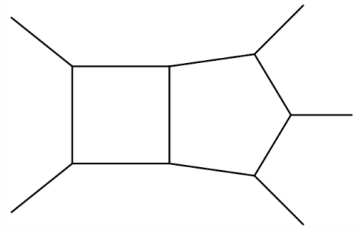


C. Signorile-Signorile

- SUBTRACTION TECHNIQUES \Leftrightarrow NNLO UNDER CONTROL

THE AMPLITUDE REVOLUTION MORE LEGS AND MORE LOOPS

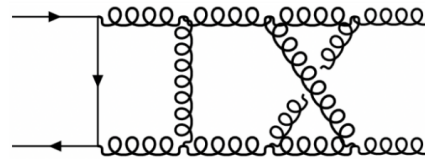
A



2 loop 5 point



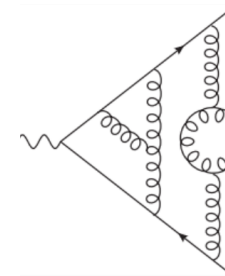
Abreu, Agarwal, Badger, Buccioni, Chawdhry, Chicherin, Czakon, de Laurentis, Febres-Cordero, Gambuti, Gehrmann, Henn, Ita, Lo Presti, Manteuffel, Ma, Mitov, Page, Peraro, Pochelet, Schabinger, Sotnikov, Tancredi, Zhang, ...



3 loop 4 point



Bargiela, Bobadilla, Canko, Caola, Jakubcik, Gambuti, Gehrmann, Henn, Lim, Mella, Mistlberger, Wasser, Manteuffel, Syrrakos, Smirnov, Tancredi, ...



4 loop 3 point



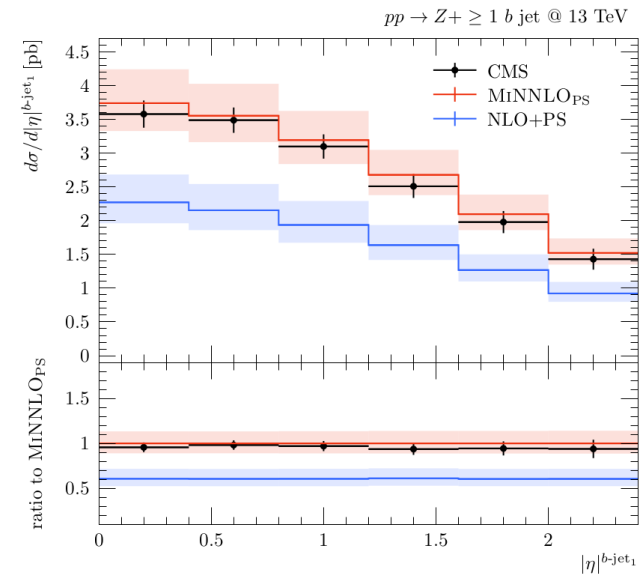
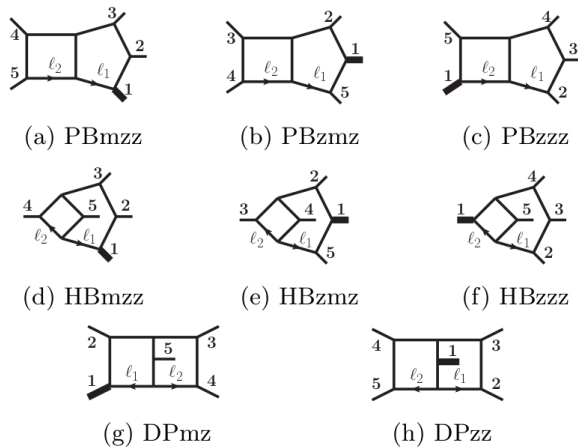
Henn, Lee, Manteuffel, Schabinger, Smirnov, Smirnov, Stainhauser, ...

**All processes computed in Full Color
Including Planar and Non-Planar diagrams**

THE AMPLITUDE REVOLUTION THE COMPLEXITY FRONTIER

$$pp \rightarrow \{V_{jj}, H_{jj}, V\gamma\gamma, \dots\}$$

Complete results obtained for **2 loops integrals**



[Abreu, Chicherin, Ita, Page, Sotnikov, Tschernow, Zoia '23]

NNLO corrections to $pp \rightarrow Zb\bar{b}$ + PS matching

[Mazzitelli, Sotnikov, Wieseman '24]

L. Tancredi

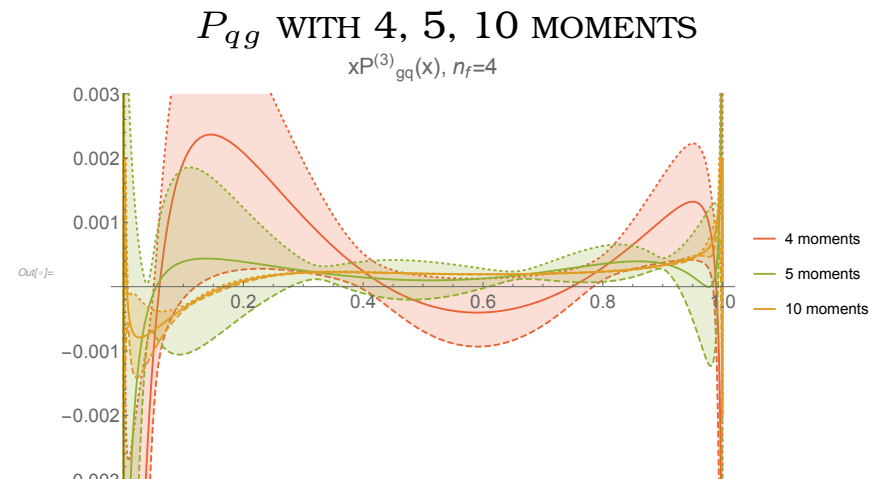
- **2 MASSLESS 1 MASSIVE AT TWO LOOPS:** $pp \rightarrow H_{jj}, V\gamma\gamma \dots$
- MANY RESULTS AT **LEADING COLOR (PLANAR), FIRST AT NLC!**
- **FIRST PHENO STUDIES!**

THE AMPLITUDE REVOLUTION THE N³LO FRONTIER MATRIX ELEMENTS

- TOTAL XSECT: $gg \rightarrow H$ (2015), $gg \rightarrow HH$ (2020), CC& NC DY (2020-2021)
- FULLY DIFFERENTIAL ggH (2021)
- MORE N³LO MATRIX ELEMENTS:
HIGGS DECAY TO $b\bar{b}$ OR gg , INDIVIDUAL PARTON CHANNELS UP TO N³LO
Chen, Jakubčík, Marcoli, Stagnitto, 2024

SPLITTING FUNCTIONS

- LO: 1973 Gross, Wilckzek; NLO: 1979 Floratos, Ross, Sachrajda; Gonzalez-Arroyo, López, Ynduráin; NNLO: 2004 Moch, Vermaseren, Vogt
- N³LO: SUBLEADING LARGE AND SMALL x BEHAVIOUR, INCREASINGLY LARGE NUMBER OF MELLIN MOMENTS (SINCE 2017): FIVE MOMENTS FOR P_{ij} KNOWN (2022)
- FIVE MORE MOMENTS FOR ALL P_{ij} SINCE EARLY 2023
Falcioni, Herzog, Moch, Vogt; + Pelloni, Ruijl, Ueda, Vermaseren
EXACT N_f^2 TERMS Gehrmann, von Manteuffel, Sotnikov, Yang
- HEAVY QUARK MATCHING FULLY KNOWN (Ablinger, Behring, Blümlein, De Freitas, von Manteuffel, Schneider, Schönwald, 2024)



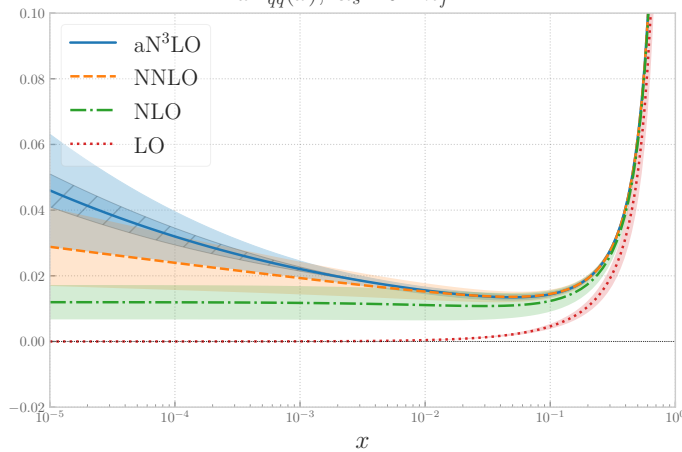
N³LO SPLITTING FUNCTIONS

- UNCERTAINTY APPROX (IHOU) \ll MISSING N⁴LO UNCERTAINTY (MHOU) \Rightarrow KNOWN EXACTLY FAPP
- FIXED-ORDER N³LO EVOLUTION KNOWN FAPP

P_{qq}

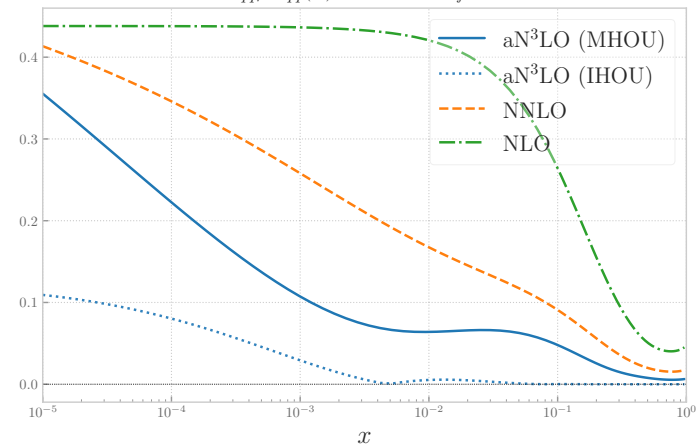
SPLITTING FCTN

$xP_{qq}(x), \alpha_s = 0.2, n_f = 4$



UNCERTAINTY

$\sigma_{qq}/P_{qq}(x), \alpha_s = 0.2, n_f = 4$

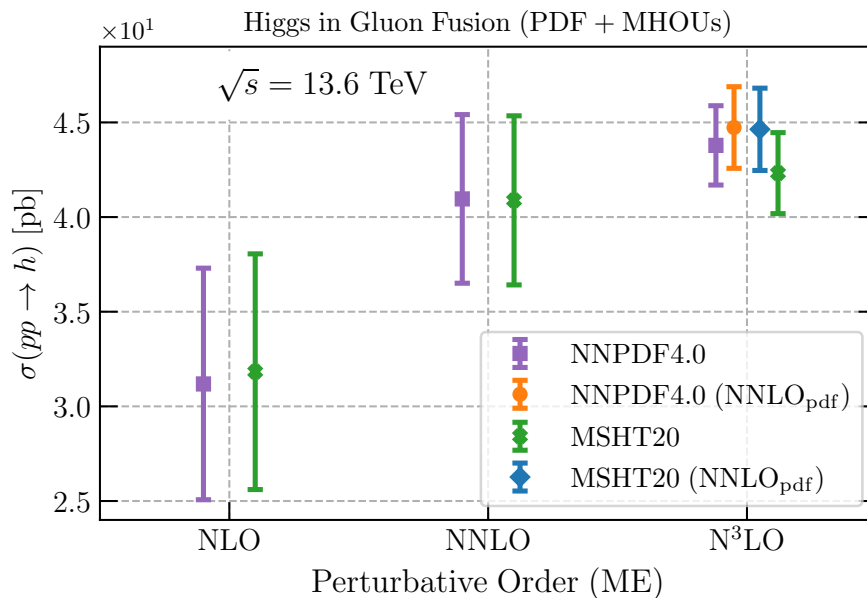


PDFs: N³LO, MHOUs, QED

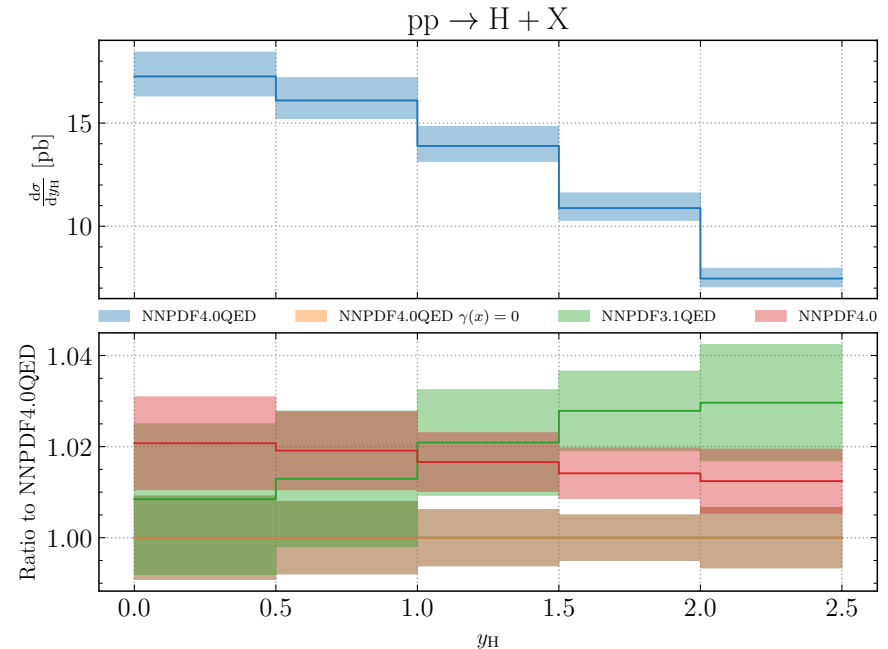
- AN³LO PDF SETS NOW AVAILABLE: MSHT20 (2023), NNPDF4.0 (2024), COMBINATION (2024)
 - NNPDF IHOU ESTIMATED FROM THEORY COVARIANCE MATRIX
 - MSHT IHOU ESTIMATED FITTING NUISANCE PARMS TO DATA
- MHOU ON PDF FIT AVAILABLE:
 - NNPDF4.0 AT ANY ORDER, FROM SCALE VARIATION
 - MSHT20 AT AN³LO FROM NUISANCE PARMS, AT NNLO FROM N³LO-NNLO DIFFERENCE
- COMBINED QED-QCD EVOLUTION AND PHOTON PDF AVAILABLE FOR BOTH

Higgs in gluon fusion

NNPDF vs MSHT



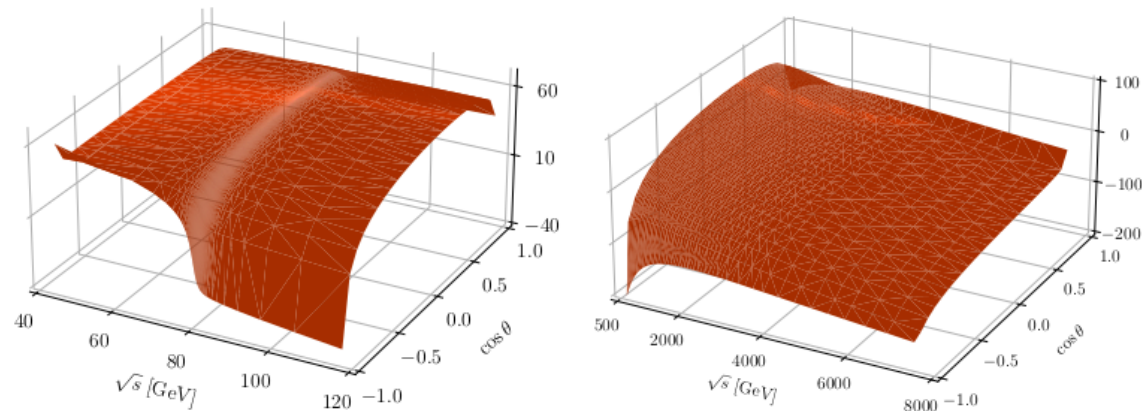
NNPDF: IMPACT OF QED



MIXED QCD×EW CORRECTIONS

- $\alpha \sim (\alpha_s(M_Z))^2$ SO $\alpha\alpha_s \sim \alpha_s^3$; NONTRIVIAL INTERFERENCE
- FULL TWO LOOP QCD×EW CORRECTIONS TO NC DRELL-YAN INCLUDING DECAY RECENTLY COMPLETED, RESONANT AND HIGH-MASS Bonciani et al., Buccioni et al. (2022)
- CC DRELL-YAN AVAILABLE WITH TWO LOOP VIRTUAL CORRECTIONS IN POLE APPROX (2021)
- EXACT TWO-LOOP VIRTUAL CORRECTIONS TO CC NOW AVAILABLE (Armadillo, Bonciani, Devoto, Rana, Vicini, 2024)
- DETAILED PHENO: CORRECTIONS UP TO PERCENT AT HIGH RAPIDITY (Armadillo, et al., 2025)

VIRTUAL TWO-LOOP RATIO TO BORN IN UNITS OF $\alpha\alpha_s$



- PERCENT-LEVEL INTERFERENCE (NEGATIVE)

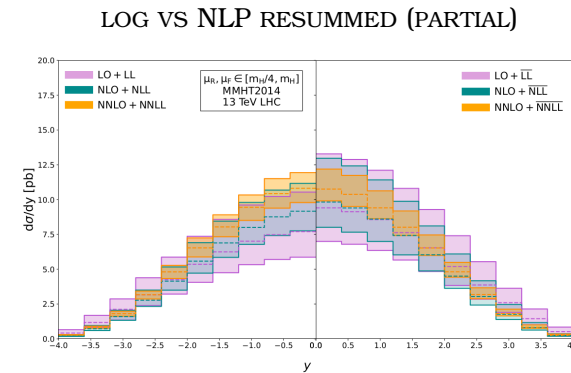
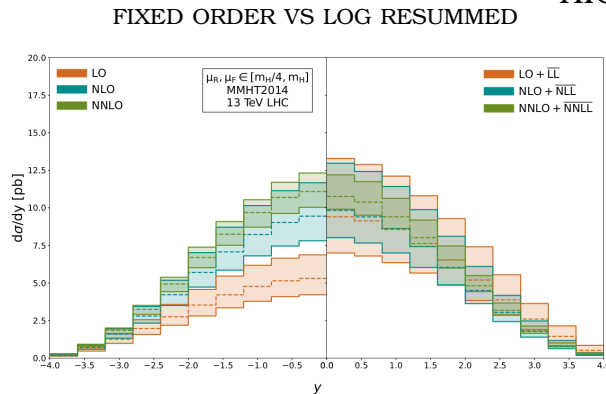
RESUMMATION: THE NLP FRONTIER

DRELL-YAN, HIGGS CROSS-SECTION: $\sigma(\tau) = \sigma^{\text{LO}} C(\alpha_s, \tau)$, $C(\alpha_s, \tau) = 1 + \alpha_s (M^2) C^{\text{NLO}} + \dots$, $\tau = \frac{M^2}{s}$;
 $C(\alpha_s, N) = \int_0^1 d\tau \tau^{N-1} C(\alpha_s, \tau)$

LEADING, NEXT TO LEADING... LOG VS. LEADING, NEXT TO LEADING... POWER: $\lim_{N \rightarrow \infty} C^{\text{N}^k \text{LO}}(\alpha_s, N) \sim \alpha^k \left[C^{k,LL} \ln^{2k} N + C^{k,NLL} \ln^{2k-1} N + \dots + g^k + \frac{1}{N} C^{k,NLP} (\ln N) + \dots \right]$

- N³LO DETERMINES N³LL
- NLP PHENOMENOLOGICALLY RELEVANT FOR M² BETWEEN THE GeV AND THE TeV SCALE

HIGGS PRODUCTION LHC



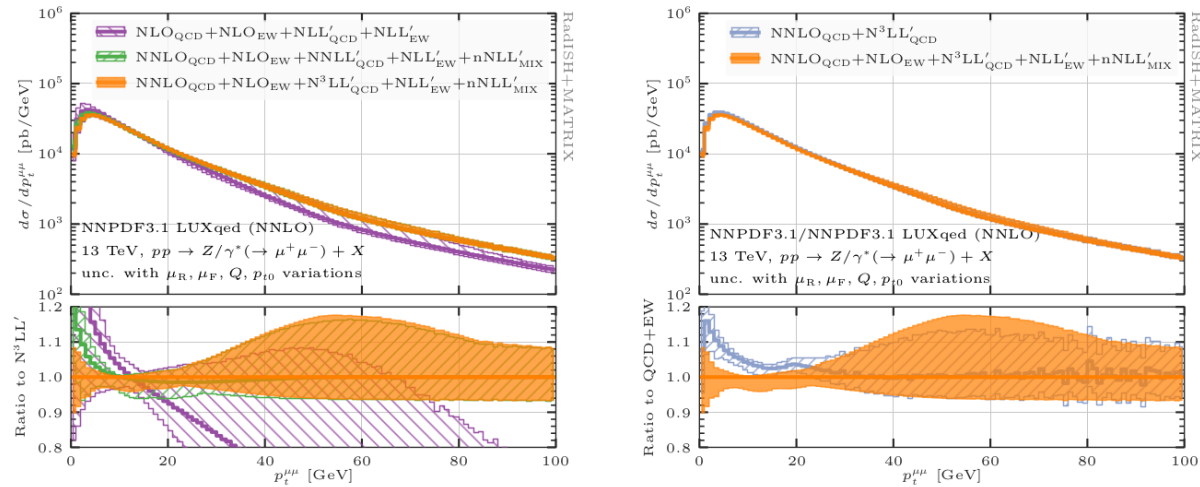
(Ravindran, Sankar, Tiwari, 2022)

- FULL LL, NLP RESUMMATION FOR DY (Bileveld, Laenen, Vernazza, Wang, 2023)
- SOFT QUARK EMISSION GENERALLY RESUMMED (van Beekveld, Vernazza, White, 2023)
- NLP PARTLY RESUMMED FOR JET THRUST AND C-PARM (Agarwal, van Beekveld, Laenen, Mishra, Mukhopadhyay, Tripathi, 2024)

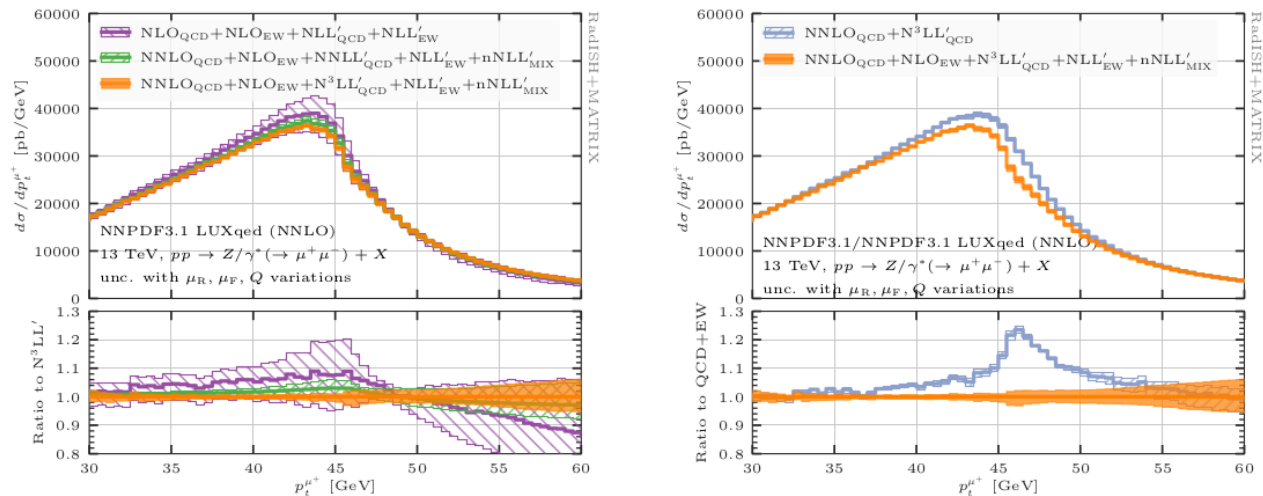
COMBINED QCD-EW RESUMMATION

- DRELL-YAN **FIXED ORDER MIXED QCD+EW** COMPUTATION IMPROVED WITH TRANSVERSE MOMENTUM RESUMMATION THROUGH PARTON SHOWERING LONG AGO
- **ANALYTIC NLL (EW) x NNLL(QCD) x NLL (MIXED) NOW AVAILABLE**
(Buonocore, Rottoli, Torrielli, 2024)

NEUTRAL CURRENT DIMUON p_T



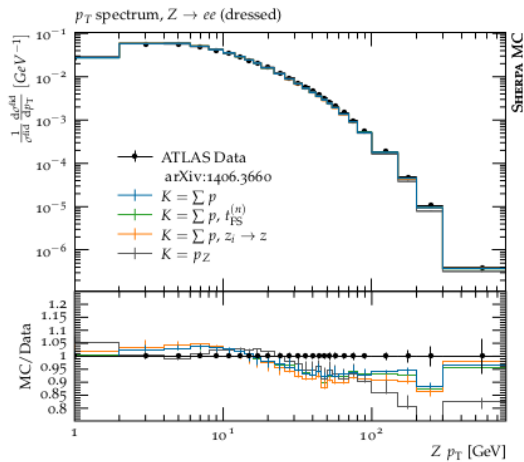
MUON p_T



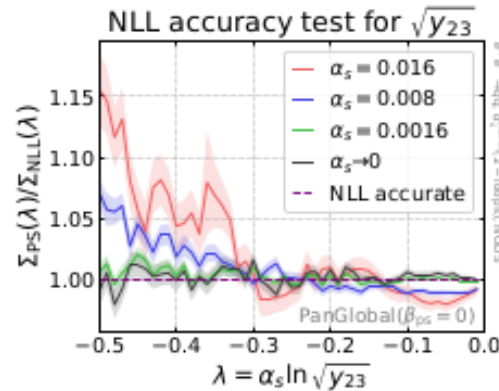
PARTON SHOWER MONTECARLOS: THE PATH TO NN LOGARITHMIC ACCURACY

- CLOSE TO ACHIEVING FULL AGREEMENT WITH NLL ANALYTIC RESUMMATION \Rightarrow COLOR DIPOLE
 - Alaric \Rightarrow NLL FOR GLOBAL LHC OBSERVABLES (Höche, Krauss, Reichelt, 2024)
 - PanScales \Rightarrow EXACT NLL FOR e^+e^- (van Beekveld et al., 2023)
- INITIAL-STATE MASSIVE QUARK EFFECTS INCLUDED IN Alaric (Assi, Höche, 2024)
- FULL NNLL ACCURACY FOR JET EVENT SHAPES! (van Beekveld, Dasgupta, El-Menoufi, Ferrario-Ravasio, Helliwell, Hamilton, Karlberg, Monni, Salam, Soto-Ontoso, Sczyboz, Soyez, 2024)

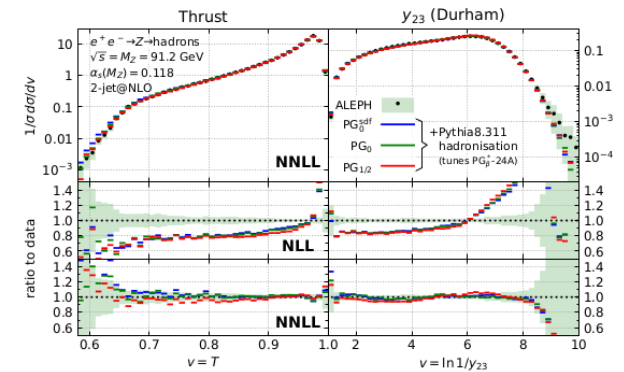
Alaric: RECOIL UNCERTAINTY IN DY



PanScales: NLL ACCURACY TEST



PanScales: NNLL EVENT SHAPES



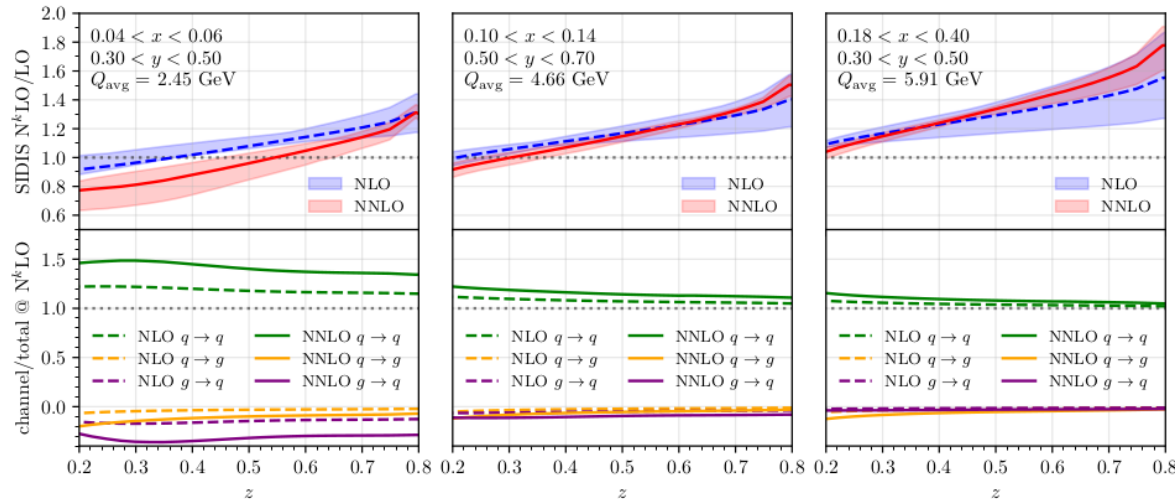
TOWARDS THE EIC: THE RESURRECTION OF DIS

SIDIS AT NNLO

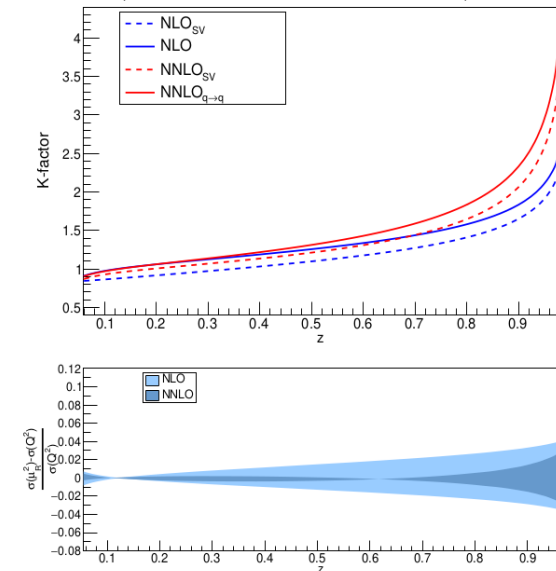
- SEMI-INCLUSIVE DIS: $ep \rightarrow h + X$ (TAGGED HADRON IN FINAL STATE)
- WILL BE MEASURED ACCURATELY AT EIC
- SIMULTANEOUS DETERMINATION OF PDF AND FRAGMENTATION FUNCTIONS DEPENDS ON TWO MOMENTUM FRACTIONS x & z
- STRINGENT CONSTRAINTS ON PDF FLAVOR SEPARATION \Rightarrow NEW PHYSICS SEARCHES AT HL-LHC
- NNLO CORRECTIONS COMPUTED (Bonino, Gehrmann, Stagnitto, 2024; Goyal, Moch, Pathak, Rana, Ravindran, 2024), ALSO IN POLARIZED CASE (Bonino, Gehrmann, Stagnitto, 2024)
- SIMILAR IN SIZE TO INCLUSIVE, NONTRIVIAL z DEPENDENCE

NNLO/LO & NLO/LO K -FACTORS VS z

COMPASS x BINS (Bonino et al., 2024)

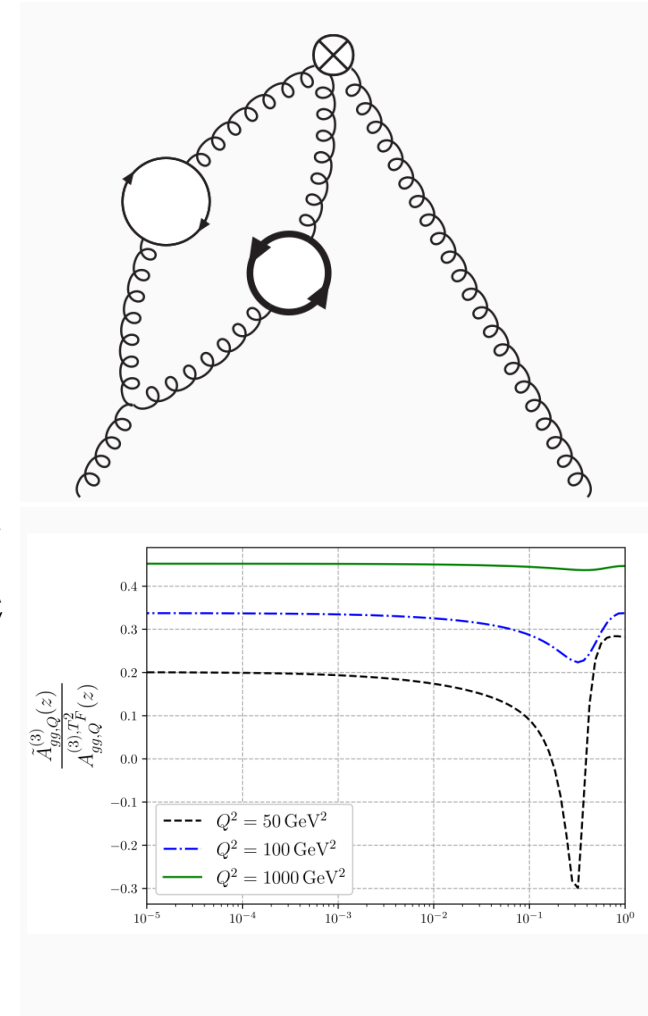


INTEGRATED OVER x FOR EIC (Moch et al., 2024)



HQ MASSES, RESUMMATION

- $m_b \gtrsim m_c \Rightarrow$ **MUST INCLUDE BOTH AT ONCE IN VARIABLE-FLAVOR NUMBER SCHEME**
- **NEW TWO-MASS CONTRIBUTIONS** Ablinger, Behring, Blümlein, De Freitas, Manteuffel, Schneider, Schönwald 2024
- **SIZABLE WILSON COEFFICIENT AT LOW SCALE, VALENCE PEAK**

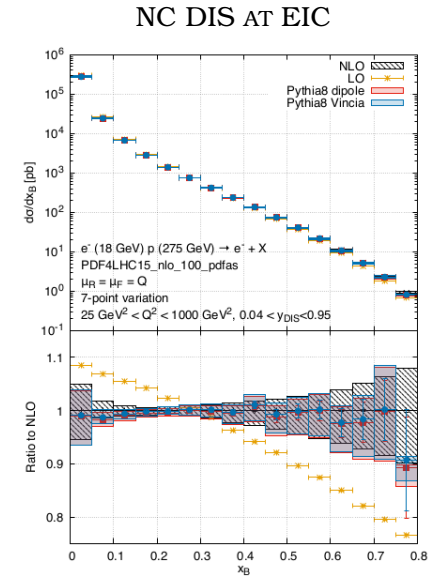


- **THRESHOLD RESUMMATION GENERALISED TO EIC PROCESSES: SIDIS** Abele, de Florian, Vogelsang 2022, **DVCS** Schoenleber, 2024

PARTON SHOWER MCs FOR DIS

NLO+PS

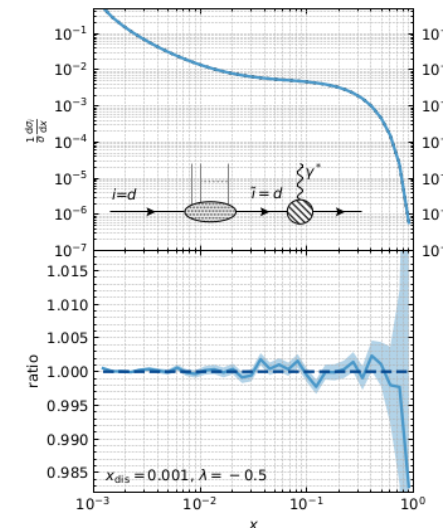
- **NLO+PS** EVENT GENERATOR IMPLEMENTED IN **POWHEG BOX** FOR DIS
(Banfi, Ferrario Ravasio, Jäger, Karlberg, Reichenbach, Zanderighi, 2023)
- **FSR DOES NOT PRESERVE** x_B, y, Q^2
⇒ **MOMENTUM MAPPINGS ADAPTED**
⇒ **PRESERVE INCOMING & OUTGOING LEPTON MOMENTA**
- **NLO** CORRECTIONS **SIGNIFICANT** IN EIC KINEMATICS
- RECENTLY **EXTENDED** TO FINAL-STATE **MASSIVE QUARKS**
(Buonocore, Limatola, Nason, Tramontano, 2024)



NLL SHOWER

- PanScales **FULLY IMPLEMENTED** FOR DIS AND VBF
(van Beekveld, Ferrario Ravasio, 2023)
- **FIXED-ORDER** ⇒ **WIDELY SEPARATED EMISSIONS INDEPENDENT**
- **FIXED-ORDER** ⇒ **EXACT SUBLEADING COLOR**
- **ALL-ORDER** ⇒ **TESTED VS. EXACT NLO EVOLUTION**

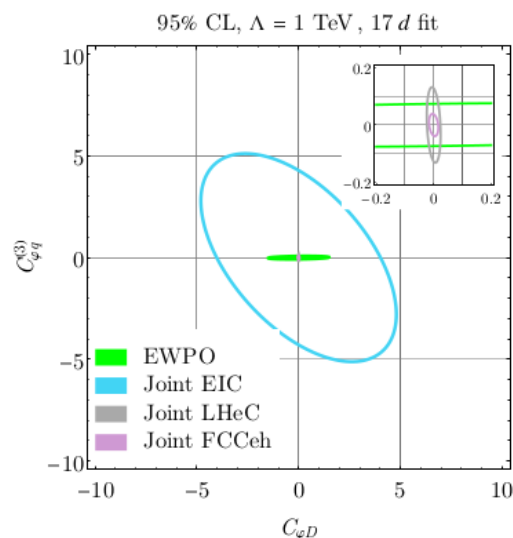
Panscales VS HOPPET
PROBABILITY OF PARTON x FOR FIXED x_B



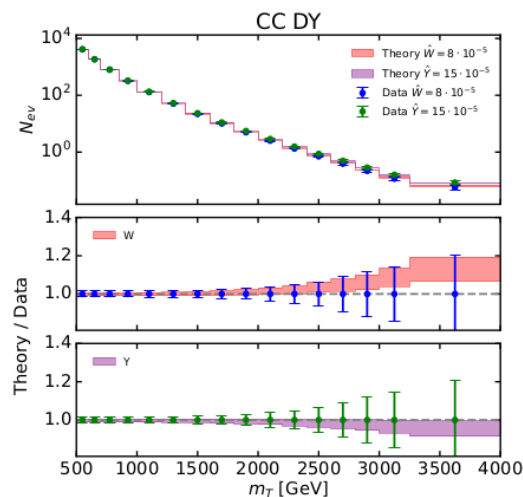
SMEFT, DIS, AND PDFs

- KNOWLEDGE OF QCD SECTOR \Rightarrow SEARCHES FOR NEW PHYSICS
- DIS CAN RESOLVE DEGENERACIES IN SMEFT FITS, BUT EIC $\Rightarrow \sim 3$ TeV (LHEC ~ 13 TeV; FCC-EH ~ 18 TeV) (Bissolotti, Boughezal, Simsek, 2023)
- PDFs CAN BE CONTAMINATED BY NP \Rightarrow DIFFICULT TO SEE IN CC DY, VISIBLE IN DIBOSON (Hammou, Kassabov, Madigan, Mangano, Mantani, Moore, Morales, Ubiali, 2023)
- MUST PERFORM GLOBAL FIT \Rightarrow OPEN-SOURCE TOOL SIMUnet (Costantini, Hammou, Kassabov, Madigan, Mantani, Moore, Morales, Ubiali, 2024)

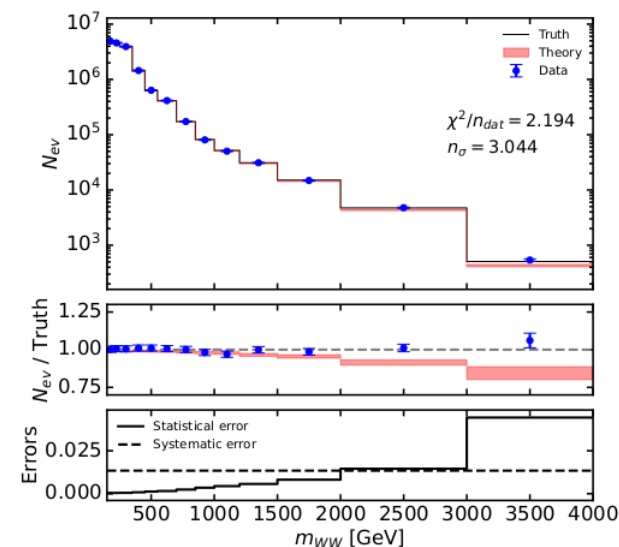
SMEFT FITS: IMPACT OF FUTURE DATA



CONTAMINATED PDFs: CC DY



CONTAMINATED PDFs WW



STRETCHING THE THEORY

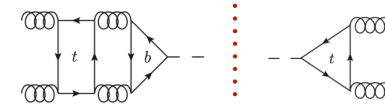
HIGGS IN GLUON FUSION: TOP-BOTTOM INTERFERENCE

new: top-bottom interference effects at NNLO

Pietrulewicz, Stahlhofen 2302.06623

Niggetiedt, Usowitsch 2312.05297 (3-loop form factor with 3 mass scales)

Czakon, Eschment, Niggetiedt, Poncelet, Schellenberger 2312.09896 (t-b interference), 2407.12413 (OS vs MSbar, 4FS/5FS)



Order	σ_{HEFT} [pb]	$(\sigma_t - \sigma_{\text{HEFT}})$ [pb]	$\sigma_{t \times b}$ [pb]	$\sigma_{t \times b} / \sigma_{\text{HEFT}}$ [%]
$\sqrt{s} = 13 \text{ TeV}$				
$\mathcal{O}(\alpha_s^2)$	+16.30	–	–1.975	
LO	$16.30^{+4.36}_{-3.10}$	–	$-1.98^{+0.38}_{-0.53}$	–12
$\mathcal{O}(\alpha_s^3)$	+21.14	–0.303	–0.446(1)	
NLO	$37.44^{+8.42}_{-6.29}$	$-0.303^{+0.10}_{-0.17}$	$-2.42^{+0.19}_{-0.12}$	$-6.5^{+0.9}_{-0.8}$
$\mathcal{O}(\alpha_s^4)$	+9.72	+0.147(1)	+0.434(8)	
NNLO	$47.16^{+4.21}_{-4.77}$	$-0.156(1)^{+0.13}_{-0.03}$	$-1.99(1)^{+0.30}_{-0.15}$	$-4.2^{+0.9}_{-0.8}$

M. Niggetiedt, HP2 2024

t-b interference effect larger than pure top mass effect, also larger than NLO scale uncertainties

...**REMEMBER**
YR4

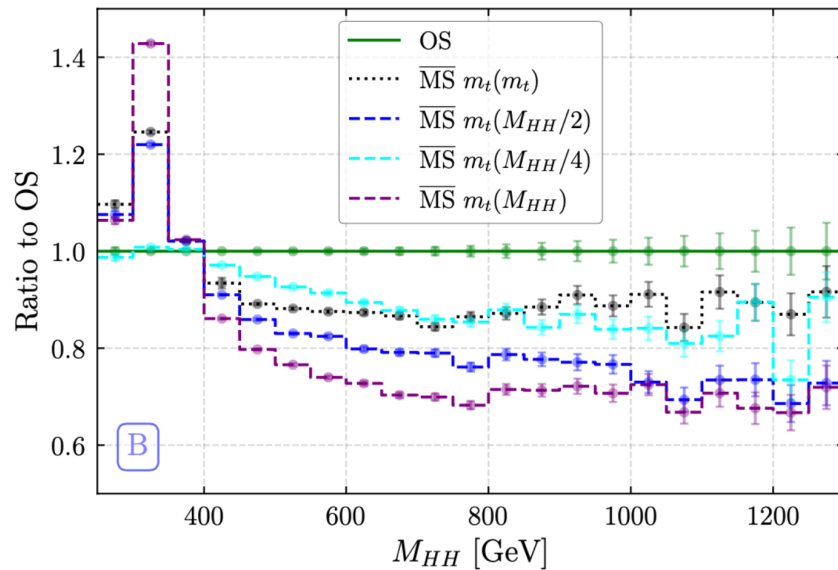
bottom and charm interference correction changes by 0.7 pb if $\overline{\text{MS}}$ or pole heavy quark masses are used.

The **F-uncertainty** is estimated as $\Delta_{t,bc} = \pm 0.4 \text{ pb}$, i.e. a relative uncertainty of $\pm 0.8\%$, following Sect. [I.4.1.a.iii](#) and Ref. [93].

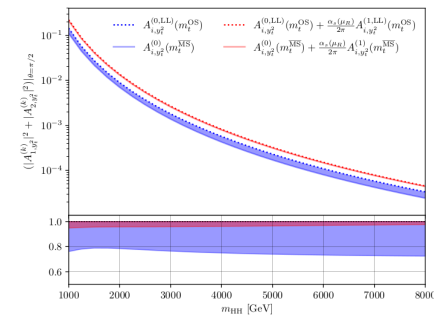
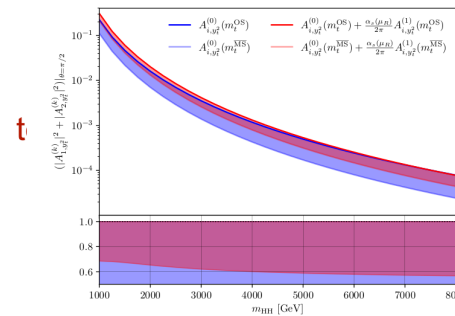
The **G-uncertainty** is estimated taking the scheme dependence of the NLO interference as a reasonably conservative estimate. This leads to $\Delta_{t,bc} = \pm 0.7 \text{ pb}$, i.e. a relative uncertainty of $\pm 1.5\%$.

DOUBLE HIGGS PRODUCTION: TOP MASS DEPENDENCE

- **LARGE DIFFERENCE** BETWEEN OS AND $\overline{\text{MS}}$ SCHEME RESULTS \Rightarrow **LARGEST** UNCERTAINTY, UP TO 20% (Bagnaschi, Degrassi, Gröber, 2023)
- REDUCED **?** TO PERCENT LEVEL BY **HIGH-ENERGY LL RESUMMATION** $\ln \frac{m_t^2}{s}$ (Jaskiewicz, Jones, Szafron, Ulrich, 2025)



Bagnaschi et al, 2023

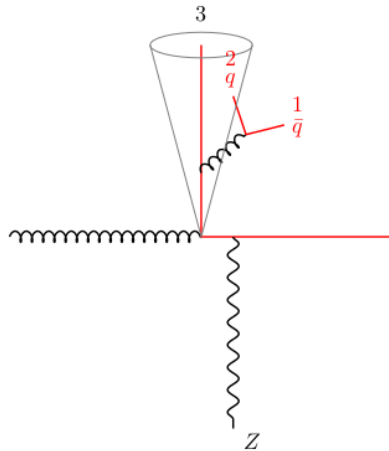


Jaskiewicz et al., 2025

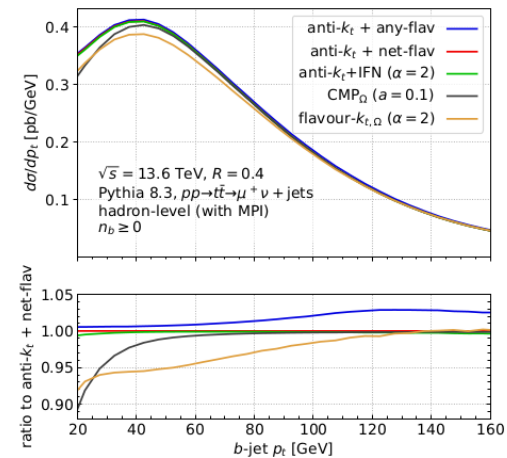
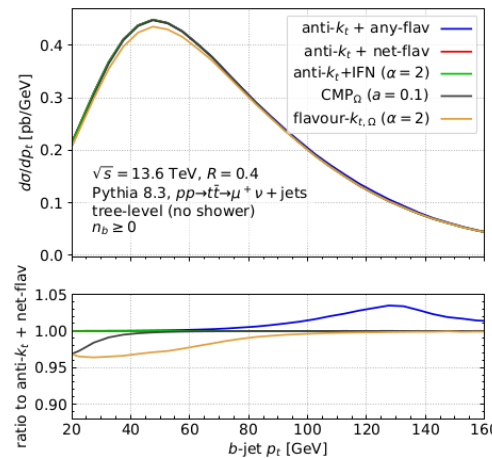
HEAVY FLAVORED JETS

- DEFINITION OF **HEAVY FLAVORED JET NONTRIVIAL** \Rightarrow “EXPERIMENTAL” DEFINITION NOT IRC SAFE
- LONG-STANDING **OPEN PROBLEM**: SOLUTIONS
 - LIMITED (IRC ONLY AT LOW ORDER)
 - IMPRACTICAL (DIFFICULT TO MERGE WITH ANTI- k_t .)
- **FULL SOLUTION (IFN SCHEME)**, CONSISTENT WITH ANTI- k_t , **ALL-ORDER IRC-SAFETY TEST** (Caola, Grabarczyk, Hitt, Salam, Sczyboz, Thaler, 2024)
- ENABLES **HEAVY FLAVORED JET SUBSTRUCTURE** STUDIES (Dhani, Fedkevych, Ghira, Marzani, Soyez, 2024)

JET FLAVOR POLLUTION



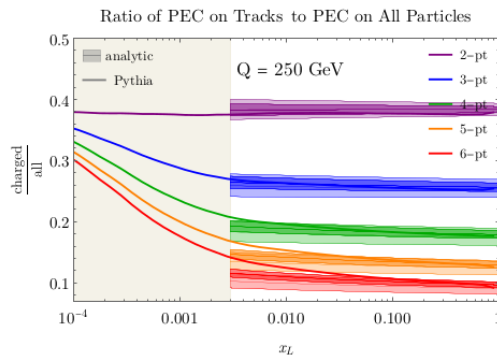
B JET FROM TOP PRODUCTION



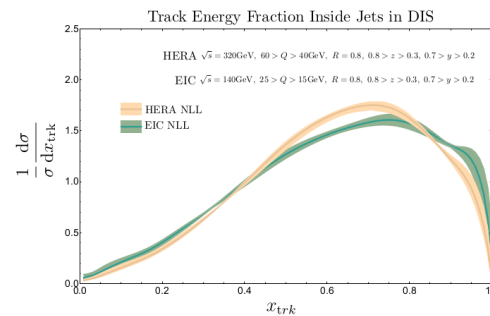
JET SUBSTRUCTURE AND ENERGY CORRELATORS

- **PARISI'S IDEA (1978): ENERGY CORRELATORS** \Rightarrow **PARTON TO HADRON TRANSITION**
- **COMPUTABLE** \Rightarrow **FACTORIZED TRACK FUNCTIONS; NONPERTURBATIVE, PERTURBATIVE RGE** (Jaarsma, Li, Moutl, Waalewijn, Zhu, 2023)
- **TRACK FUNCTIONS** (PROPERTY OF FINAL STATE) MATCHED TO **TRACK JET FUNCTION** (PROPERTIES OF IDENTIFIED JETS) \Rightarrow **JET SUBSTRUCTURE FROM DATA** (Lee, Moutl, Ringer, Waalewijn 2023)
- **CORRELATIONS BETWEEN DIFFERENT HADRONS** \Rightarrow **DECONFINEMENT** (Lee, Moutl, 2023)
- **SPECTRAL FUNCTIONS** \Rightarrow **METRIC IN JET SPACE (& IN THEORY SPACE?)** (Larkoski, Thaler, 2023)

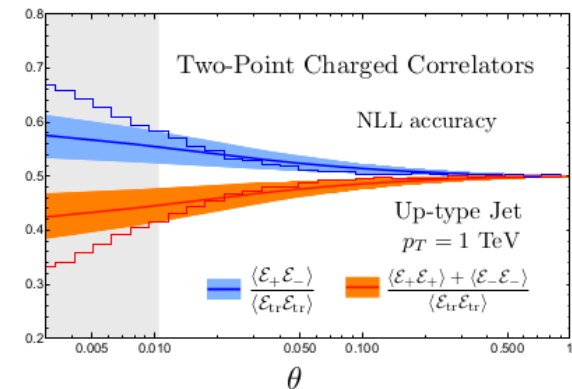
ENERGY CORRELATORS VS ANGULAR SIZE: TRACK TO ALL RATIO
PERTURBATIVE VS. pythia



EXTRACTION OF TRACK FUNCTION FROM EIC DIS DATA



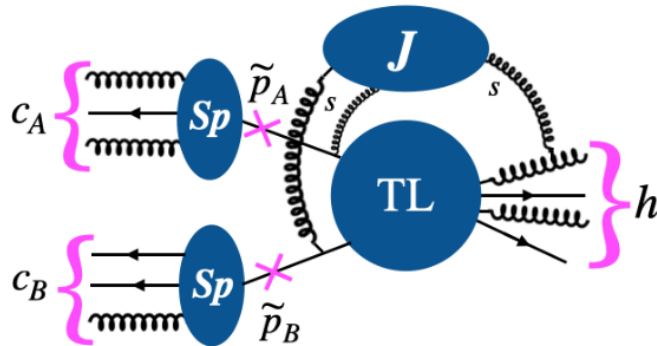
HADRON ENERGY CORRELATORS: SAME VS. DIFFERENT CHARGE



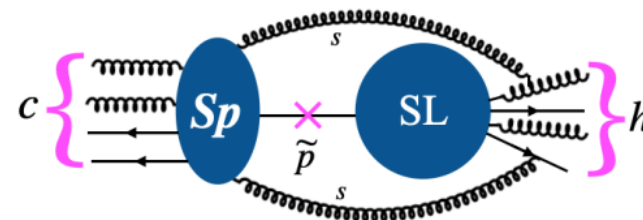
STRETCHING THE LIMITS OF FACTORIZATION

- ALL-ORDER EXTENSION OF SOFT-GLUON EFFECTIVE COUPLING
 \Rightarrow ALL-ORDER EXACT RESULTS IN LARGE n_f LIMIT \Rightarrow CUSP ANOMALOUS DIMENSION
 (Catani, de Florian, Devoto, Grazzini, Mazzitelli, 2023)
- UNIVERSALITY OF FACTORIZATION VIOLATED BY INITIAL-STATE COLLINEAR CONFIGURATIONS \Rightarrow
 COLLINEAR FACTORIZATION ENDANGERED AT N³LO AND BEYOND
- SOFT-PHOTON THEOREM MODIFIED IN QCD (Ma, Sterman, Venkata, 2024)
- Catani's GENERALIZED FACTORIZATION FOR SPACELIKE COLLINEAR EMISSION
 (Cieri, Dhani, Rodrigo, 2024)

TIMELIKE COLLINEAR (FINAL STATE)



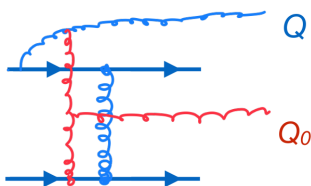
SPACELIKE COLLINEAR (INITIAL STATE)



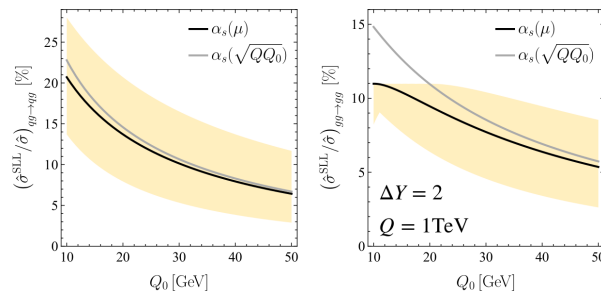
SUPERLEADING LOGS & PDF FACTORIZATION

- **NON-GLOBAL** OBSERVABLES: **GAP** BETWEEN **JETS**, **VETO** SCALE Q_0
- **COLLINEAR LOGS** HIGHER ORDER THAN ALTARELLI PARISI \Rightarrow **FACTORIZATION VIOLATION**
- **RESUMMATION** (Becher, Neubert, Shao, Stillger, 2023)
- **CANCELLED** BY GLAUBER GLUONS \Rightarrow **PDF FACTORIZATION RESTORATION** VERIFIED AT FIXED ORDER (Becher, Hager, Jaskiewicz, Neubert, Schwienbacher, 2024)

SUPERLEADING LOGS



DIJET SLL RESUMMATION



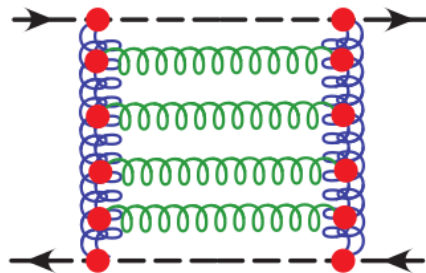
Collinear factorization breaking at $\mu = Q$ **X** soft-collinear factorization breaking by Glauber modes at $\mu = Q_0$

= PDF factorization for $\mu < Q_0$

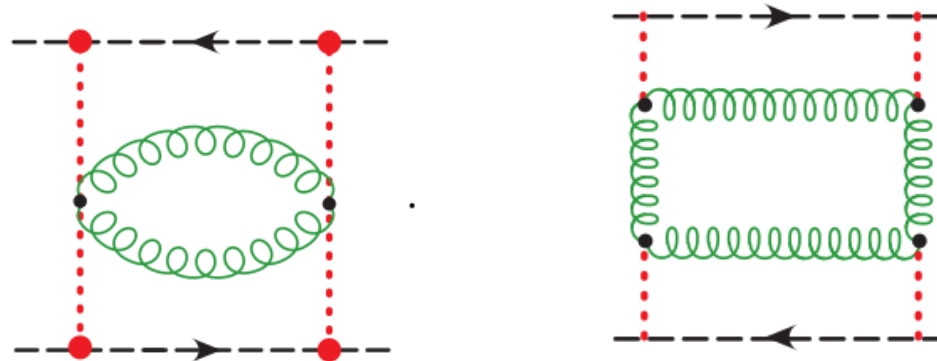
HIGH-ENERGY RESUMMATION

- HIGH ENERGY (BFKL, SMALL x) LOGS $\propto \ln 1/x$, $x = \frac{M^2}{s}$
 \Rightarrow PARTONIC CROSS-SECTIONS AND ANOMALOUS DIMENSIONS
- SMALL x EVOLUTION DUAL TO LARGE Q^2 EVOLUTION
- SMALL x SPLITTING FUNCTIONS \Leftrightarrow HIGH ENERGY RESUMMATION OF COLLINEAR SPLITTING FUNCTIONS
- SCET APPROACH \Rightarrow RESUMMATION FROM RGE OF SOFT GLUON OPERATORS
- CONSISTENCY BETWEEN COLLINEAR & SOFT ANOMALOUS DIMENSIONS
 (Gao, Moulton, Raman, Ridgway, Stewart 2024)

LIPATOV VERTEX DIAGRAMS IN QCD



GLAUBER GLUON DIAGRAMS IN SCET

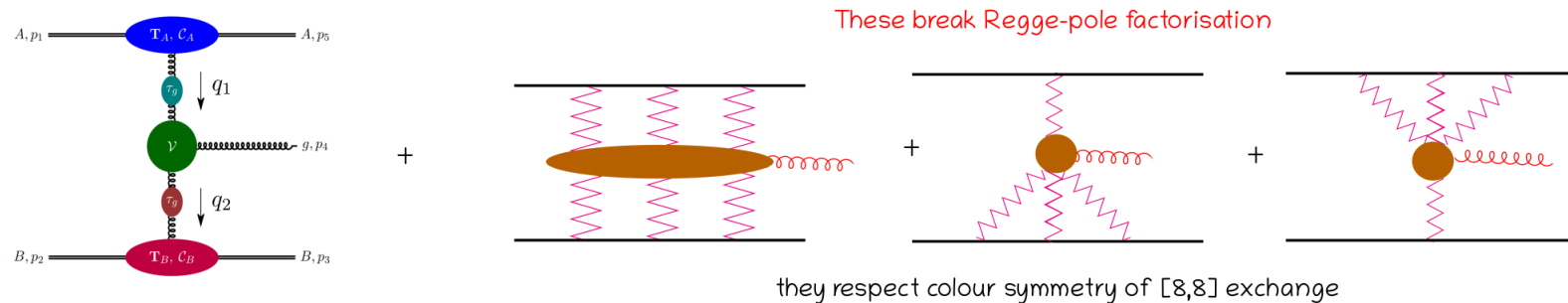


TOWARDS NNLO BFKL

- **ONLY LL FULLY RESUMMED** → **DOMINANT UNCERTAINTY** AT N³LO
- **HIGH ENERGY (BFKL, SMALL x) LOGS** ↔ HIGH-ENERGY BEHAVIOR OF FACTORIZED 2 → n AMPLITUDES
- **BFKL FACTORIZATION BROKEN** AT NNLO
- 2 → 3 AMPLITUDE COMPUTED TO TWO LOOPS (Buccioni, Caola, Devoto, Gambuti, 2024; Abreu, De Laurentis, Falcioni, Gardi, Milloy, Vernazza, 2025)
- **RESTORED** IN COLLINEAR LIMIT BY **MULTIGLUON EXCHANGES?**

Regge-pole factorisation broken at NNLL for $A(-,-)$:

$$\mathcal{A}_\lambda^{AB}(s) = s_{12} [\mathbf{T}_A^a \mathcal{C}_{A,\lambda_A}(s_{51})] \frac{\mathcal{R}(s_{45}, s_{51})}{s_{51}} [f^{aba_4} \mathcal{V}_{\lambda_g}(k_\perp, \mathbf{q}_1, \mathbf{q}_2)] \frac{\mathcal{R}(s_{34}, s_{23})}{s_{23}} [\mathbf{T}_B^b \mathcal{C}_{B,\lambda_B}(s_{51})] + \text{Multi-Reggeon exchanges}$$



Our goal: recover/show Regge-pole factorisation at NNLL + extract 2-loop CEV

Our strategy:

1. Expand 2-loop five-pt QCD amplitudes in MRK [Agarwal, FB, Devoto, Gambuti, von Manteuffel, Tancredi 2311.09870]
2. Use an effective theory that allows for the calculation/prediction of MR exchanges [Caron-Huot 1309.6521]

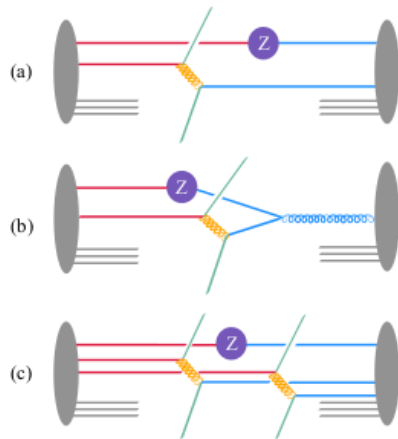
✓ 3-loop Regge-Trajectory
[Caola et al 2112.11097, Falcioni et al 2112.11098]

✓ 2-loop impact factors
[taken from Caola et al 2112.11097]

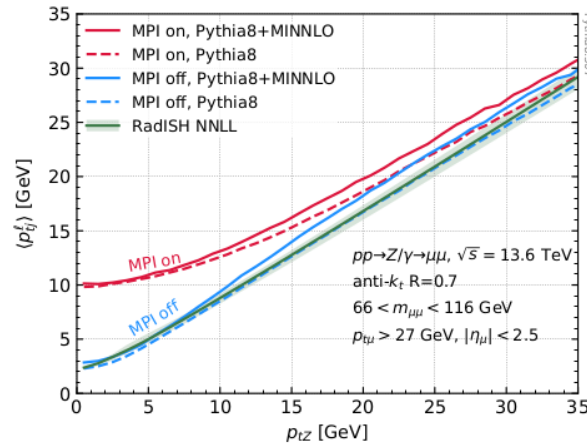
MULTIPARTON INTERACTIONS

- **SIZABLE** CONTRIBUTION, **FACTORIZABLE** IN HARD SCATTERING
- **DISENTANGLE** THROUGH p_t CUTS (Andersen, Monni, Rottoli, Salam, Soto-Ontoso 2023)
- **DOMINANT** CONTRIBUTION TO DY AT SMALL p_T
- **ENHANCED** IN CUMULATIVE INTEGRATED JET SPECTRUM $p_t > p_t^{\min}$

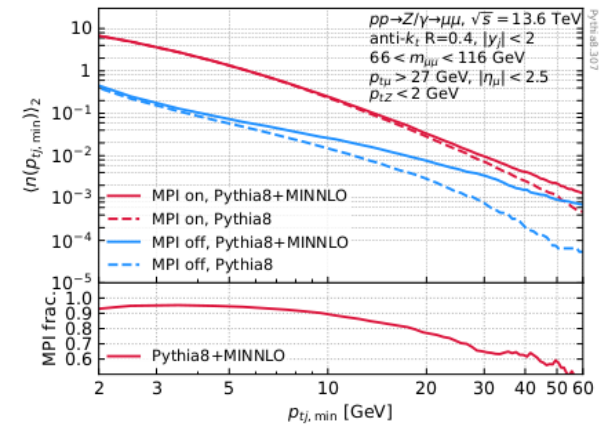
DOUBLE (A,B) AND TRIPLE (C) PARTON HARD SCATTERING



MPI VS NO MPI VS p_t

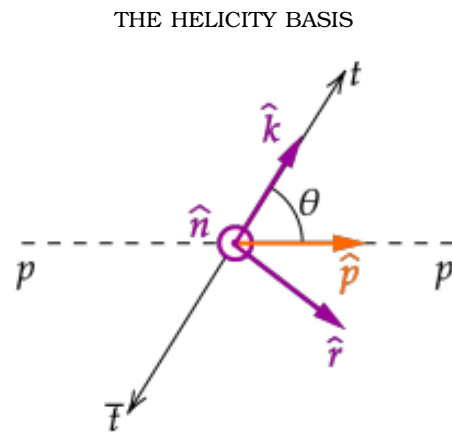


MPI VS NO MPI CUT CUMULATIVE JET SPECTRUM

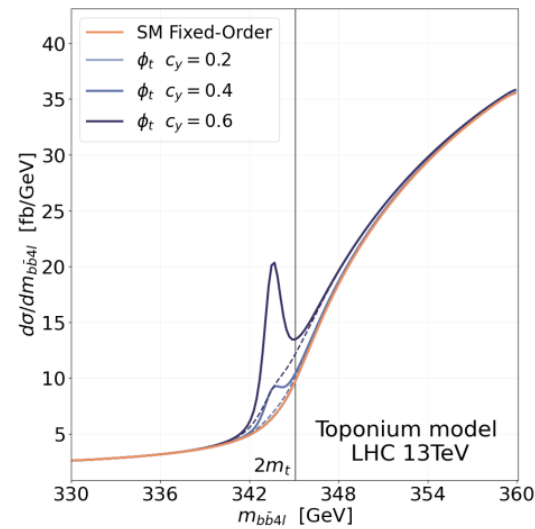


ENTANGLED TOP PAIRS

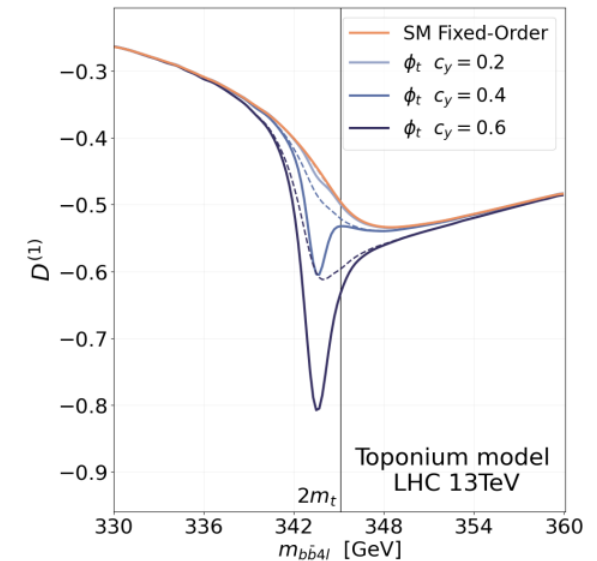
- TOP PAIRS ENTANGLED \Rightarrow PATTERN CHANGES BSM
- DEFINE $D^1 = -\text{tr } C_{ij}$ ENTANGLEMENT MARKER \Rightarrow TRACE OF $t\bar{t}$ SPIN CORRELATION MATRIX IN HELICITY BASIS
- ENTANGLEMENT SENSITIVE TO BSM PSEUDOSCALAR RESONANCE ϕ (Maltoni, Severi, Tentori, Vryonidou 2024)
- ALSO EW DIBOSON PRODUCTION (Aoude, Madge, Maltoni, Mantani 2024)



CROSS-SECTION VS FINAL STATE MASS



ENTANGLEMENT MARKER VS FINAL STATE MASS



DEEP LEARNING QCD

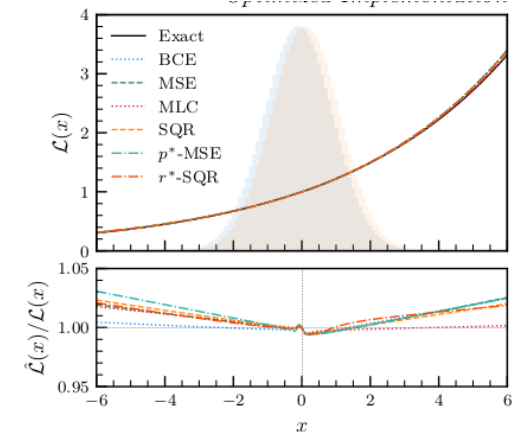
CLASSIC METHODS

REGRESSION

- HYPOTHESIS TESTING \Rightarrow LIKELIHOOD RATIO:

$$\mathcal{L}(x) = \frac{p(x|\theta_0)}{p(x|\theta_1)},$$
 θ_i PARMS OF PROBABILITY
- NEURAL NET FIT
- OPTIMAL NN CLASSIFIER (Rizvu, Pettee, Nachman, 2023)
- MATRIX ELEMENT METHOD: RECONSTRUCTED PROBABILITY FROM UNDERLYING PARTON EVENT (Heimel, Huetsch, Winterhalder, Plehn, Butter 2023)

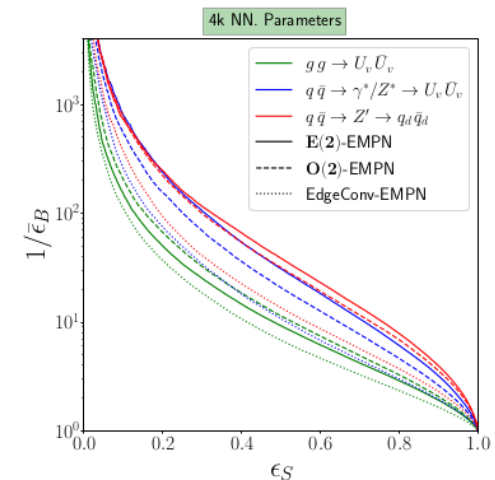
LIKELIHOOD RATIO: DISPLACED GAUSSIAN
FITTED VS TRUE



TAGGING

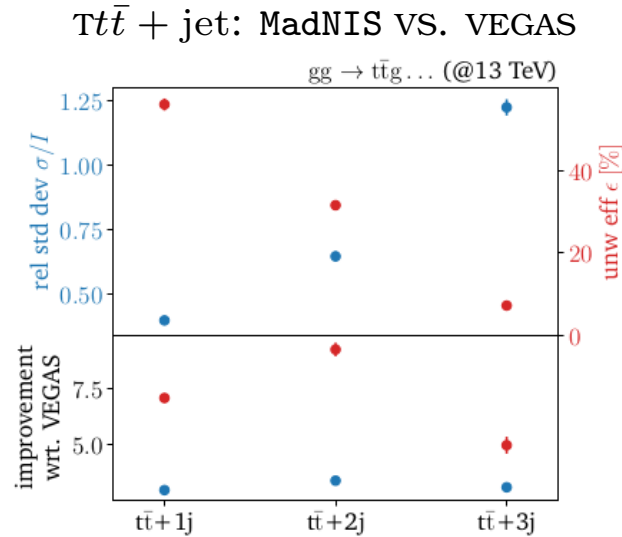
- TRAIN NEURAL NET \Rightarrow TAG SIGNAL FROM BACKGROUND
- STANDARD IN TOP TAGGING, EXTENDED TO JETS
- GRAPH & CONVOLUTIONAL NN \Rightarrow EQUIVARIANCE
- JET TAGGING FOR NP SIGNALS (Bhardwaj, Englert, Naskar, Ngairangbam, Spannowsky, 2024)

1/(FALSE POSITIVE) VS TRUE POSITIVE
NEW PHYSICS SIGNALS

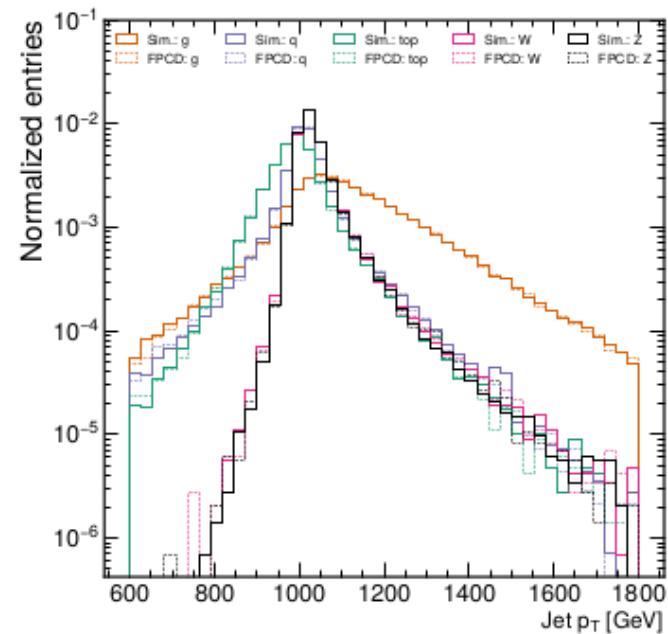


CONTEMPORARY METHODS GENERATIVE METHODS

- GENERATIVE METHODS \Rightarrow ARTIFICIAL IMAGES
- IMPORTANCE SAMPLING \Rightarrow MadNIS NEURAL IMPORTANCE SAMPLING IN Madgraph (Heimel, Huetsch, Maltoni, Mattelaer, Plehn, Winterhalder, 2023)
- HEP EVENTS \Rightarrow CONTINUOUS VARIABLES (NOT PIXELS), SYMMETRIES
- DIFFUSION MODELS \Rightarrow GENERATE PROBABILITY USED FOR SAMPLING: FPCD (FAST POINT CLOUD DIFFUSION) FOR JETS (Mikuni, Nachman, Pettee, 2023)



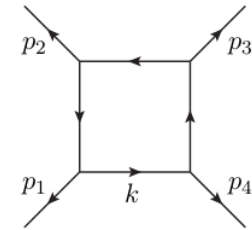
JET p_T : GENERATED VS SIMULATED



TOWARDS THE FUTURE LEARNING FEYNMAN INTEGRALS

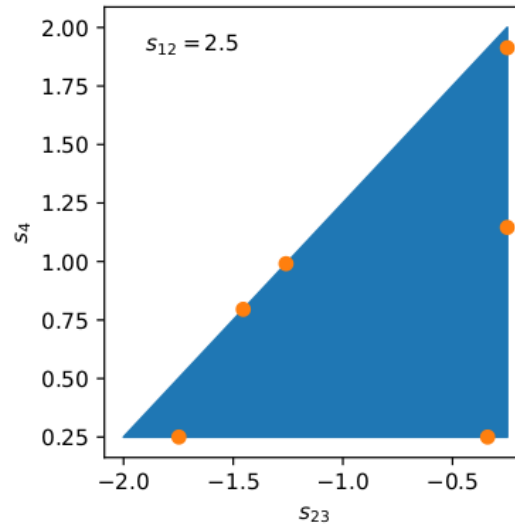
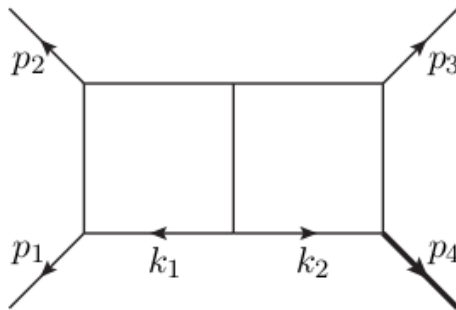
- MASSLESS BOX INTEGRAL FAMILY: $I_{\vec{a}} = \int \frac{d^d k}{i\pi^{d/2}} \frac{\mu^{4-d}}{D_1^{a_1} D_2^{a_2} D_3^{a_3} D_4^{a_4}}$
- FINITE NUMBER LIN. INDEP. \Rightarrow MASTER INTEGRALS $\vec{F}(s, t, \epsilon)$
- DIFFERENTIAL EQUATIONS $\frac{\partial}{\partial s} F^i(s, t, \epsilon) = \epsilon A_s^{ij}(s, t) F^j(s, t, \epsilon) \Rightarrow$
DETERMINE \vec{F} SOLVING EQN., B.C. FROM NUMERICAL EVALUATION
- PHYSICS-INSPIRED DEEP LEARNING: TRAIN NN
LOSS: DIFFERENCE BETWEEN TWO SIDE OF EQN + BOUNDARY VALUES
(Calisto, Moodie, Zoia, 2023)

THE BOX DIAGRAM

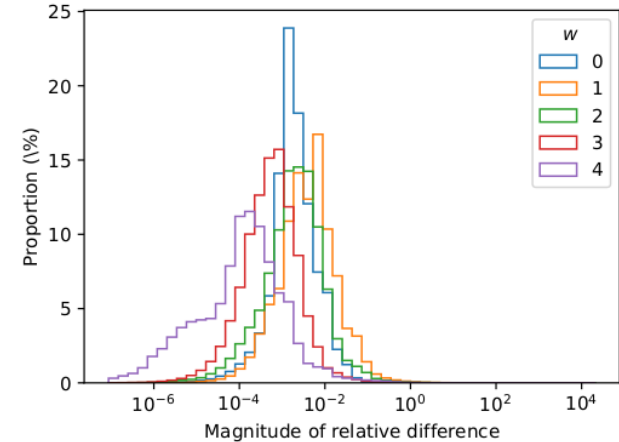


SIMILAR PROBLEM: DETERMINE PHASE OF AMPLITUDE FROM XSECT FROM OPTICAL THM \Rightarrow INTEGRAL EQN (Dersy, Schwartz, Zhiboedov, 2023)
BOUNDARY POINTS

THE DOUBLE BOX

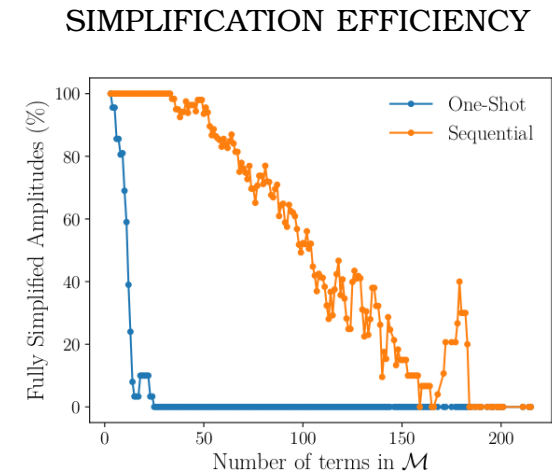
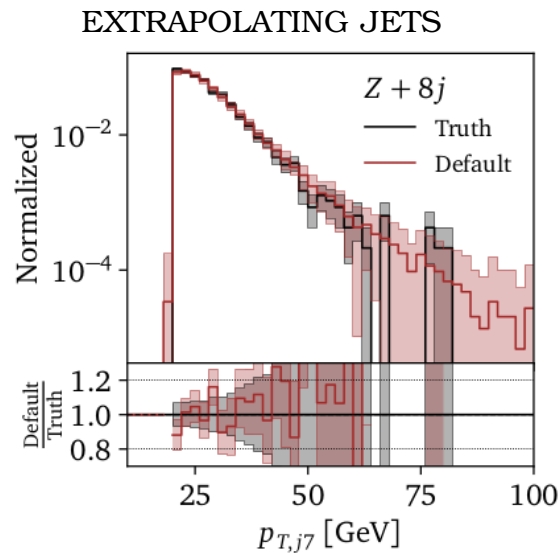
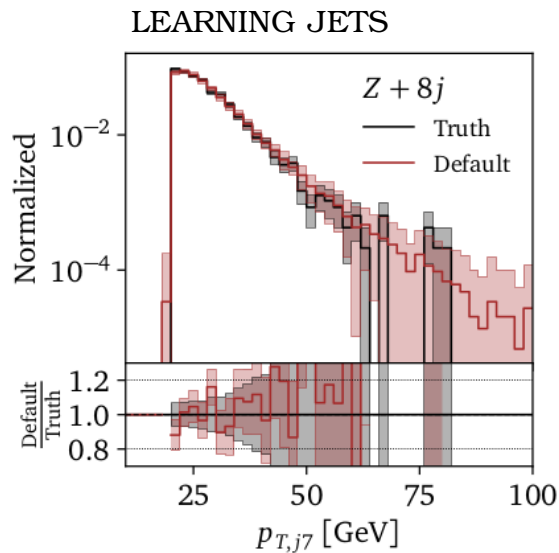


APPROX ERROR FOR DIFFERENT POWERS OF ϵ



THE FUTURE? TRANSFORMERS: LEARNING AMPLITUDES

- TRANSFORMERS \Rightarrow LARGE LANGUAGE MODELS \Leftrightarrow ATTENTION (TOKENS)
- PREDICT ANSWER TO QUESTION \Rightarrow PREDICT ITEM IN SEQUENCE



- PREDICT $n + k$ -JET RADIATION FEATURES FROM n -JET RADIATION (Butter, Charton, Villadamigo, Plehn, Spinner, 2024)
- SIMPLIFY AMPLITUDES WITH ~ 100 TERMS (Cheung, Dersy, Schwartz, 2024)
- PREDICT COEFFICIENTS OF SPECIFIC HIGHER-ORDER TERMS IN AMPLITUDES (Cai, Merz, Charton, Nolte, Wilhelm, K. Cranmer, Dixon, 2024)

SUMMARY

THE TWO HORIZONS



- 2030s: **SUB-PERCENT** ACCURACY AND PRECISION
 - $N^3\text{LO} + N(N)\text{LO}$ EW **STANDARD CANDLES**;
NLP RESUMMATION, NNLO PARTON SHOWER
 - LEVERAGING THE HL-LHC EIC **SYNERGY**
- 2040: **THE TRIUMPH** OF QCD
 - FULL UNDERSTANDING OF **QCD** FACTORIZATION
 - **MACHINE LEARNING** FOR INFERENCE