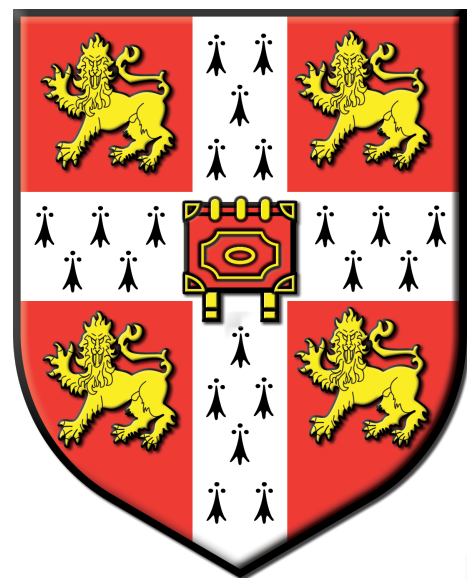




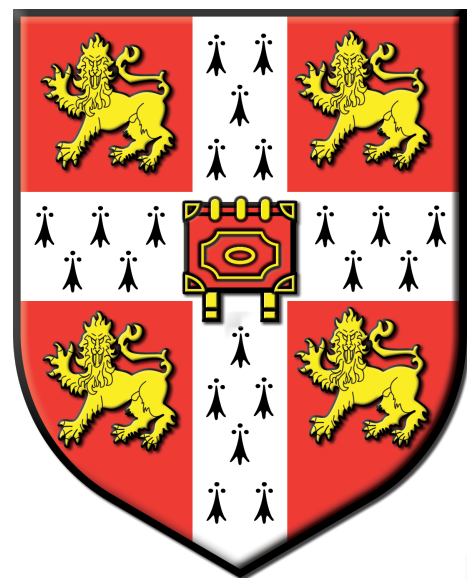
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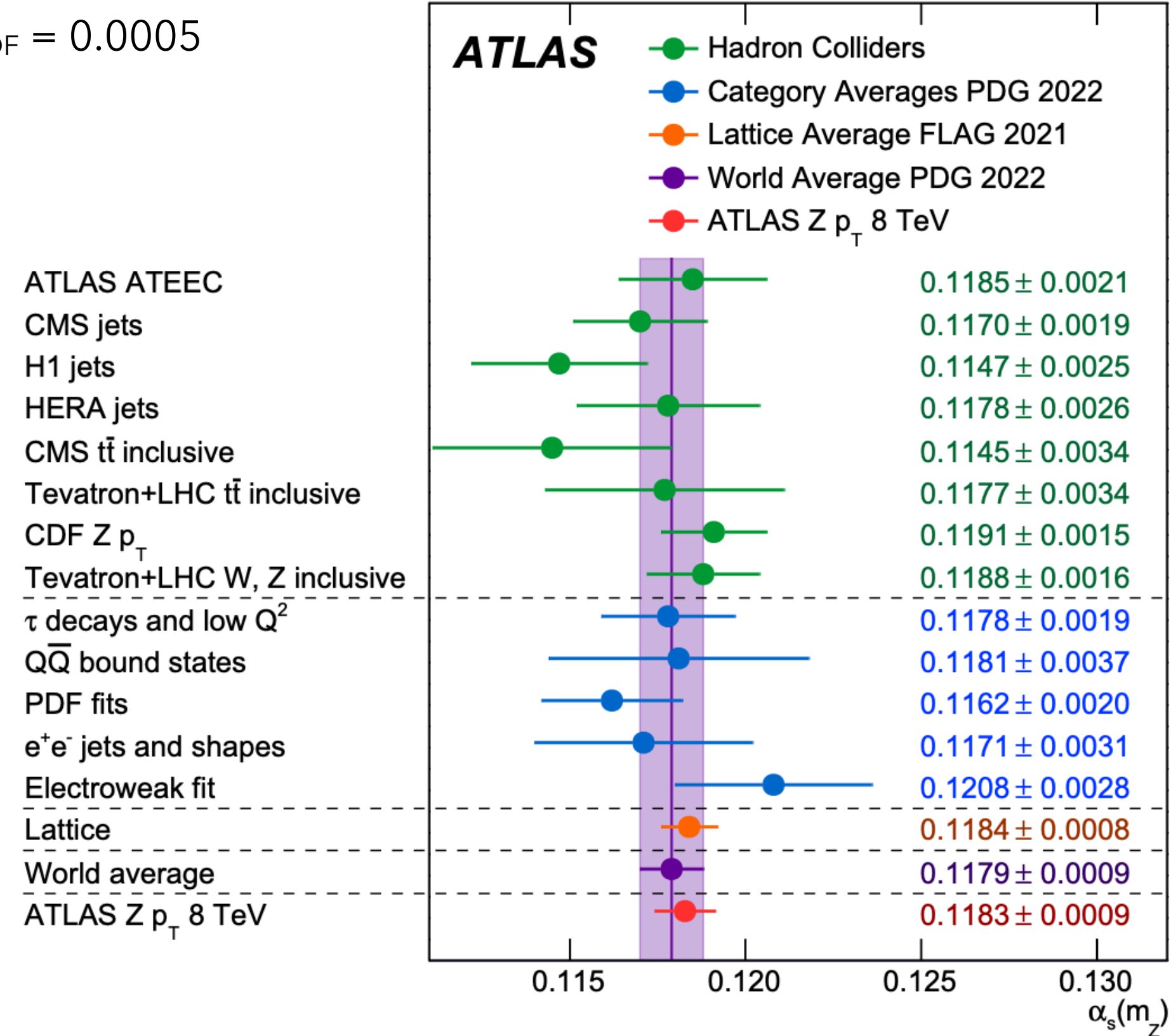
– A PERSONAL OVERVIEW

PDFS CRUCIAL INPUT FOR PRECISION PHYSICS

$$d\sigma^{pp\rightarrow ab} = \sum_{i,j} f_i \otimes f_j \otimes d\hat{\sigma}^{ij\rightarrow ab} + \dots$$

ATLAS α_s determination

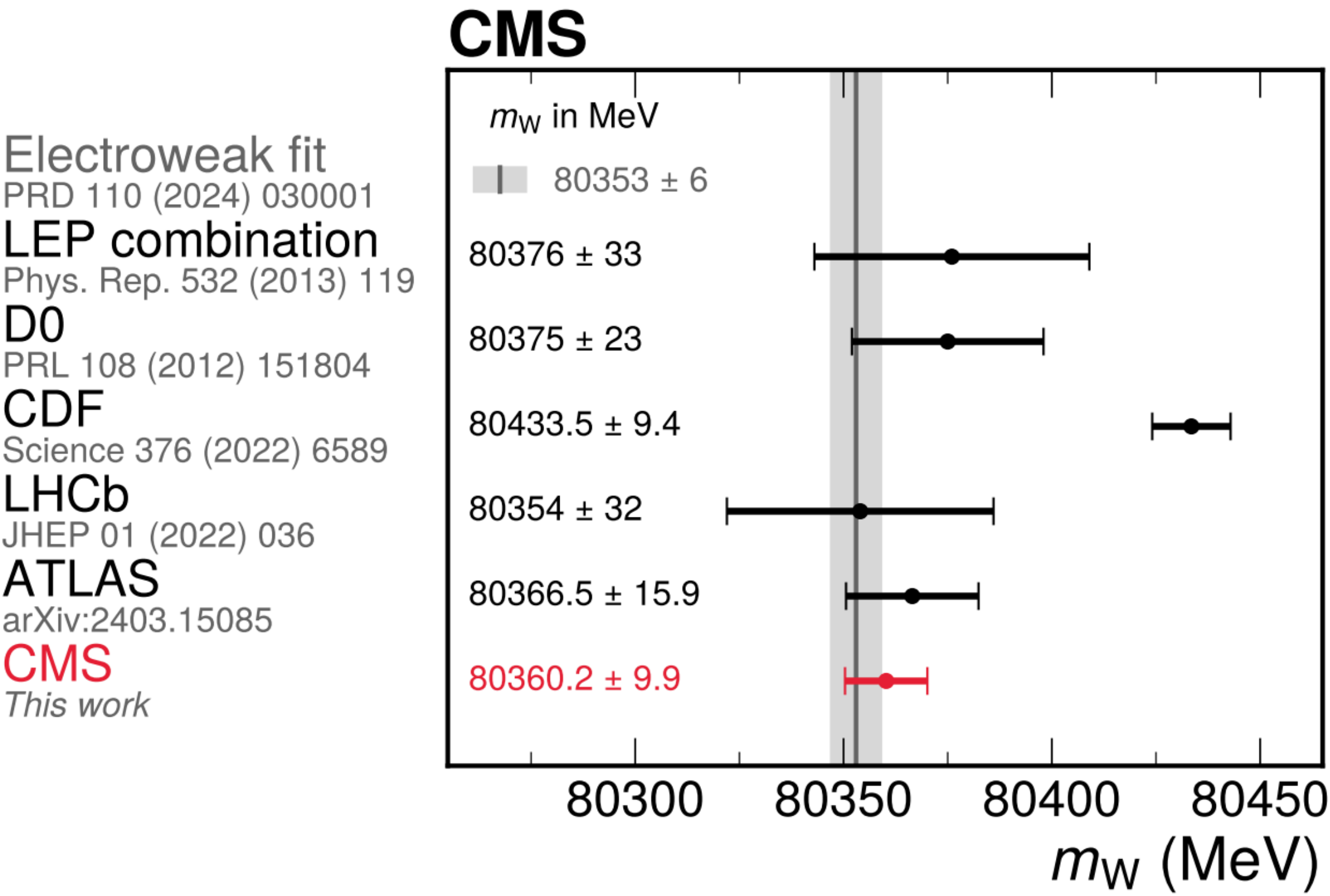
$\Delta_{\text{TOT}} = 0.0009$
 $\Delta_{\text{PDF}} = 0.0005$



ATLAS collaboration, arXiv: 2309.12986

CMS M_W determination

$\Delta_{\text{TOT}} = 9.9 \text{ MeV}$
 $\Delta_{\text{PDF}} = 4.4 \text{ MeV}$



Electroweak fit
PRD 110 (2024) 030001
LEP combination
Phys. Rep. 532 (2013) 119
D0
PRL 108 (2012) 151804
CDF
Science 376 (2022) 6589
LHCb
JHEP 01 (2022) 036
ATLAS
arXiv:2403.15085
CMS
This work

CMS collaboration, arXiv: 2412.13872

OUTLINE

➡ **Part I:** progress and highlights on recent developments in PDF determination

➡ **Part II:** precision vs accuracy: new challenges and frontiers

PDF DETERMINATION

- Huge progress from first PDF determinations to where we stand now
 - ➔ **Experimental data**: many more precise measurements constraining PDFs
 - ➔ **Theory**: heavy quark schemes, aN3LO PDFs, inclusion of MHOUs in PDF error bands, EW and QED corrections, initial photon...
 - ➔ **Methodology**: uncertainty propagation, parametrisation bias, closure tests,...

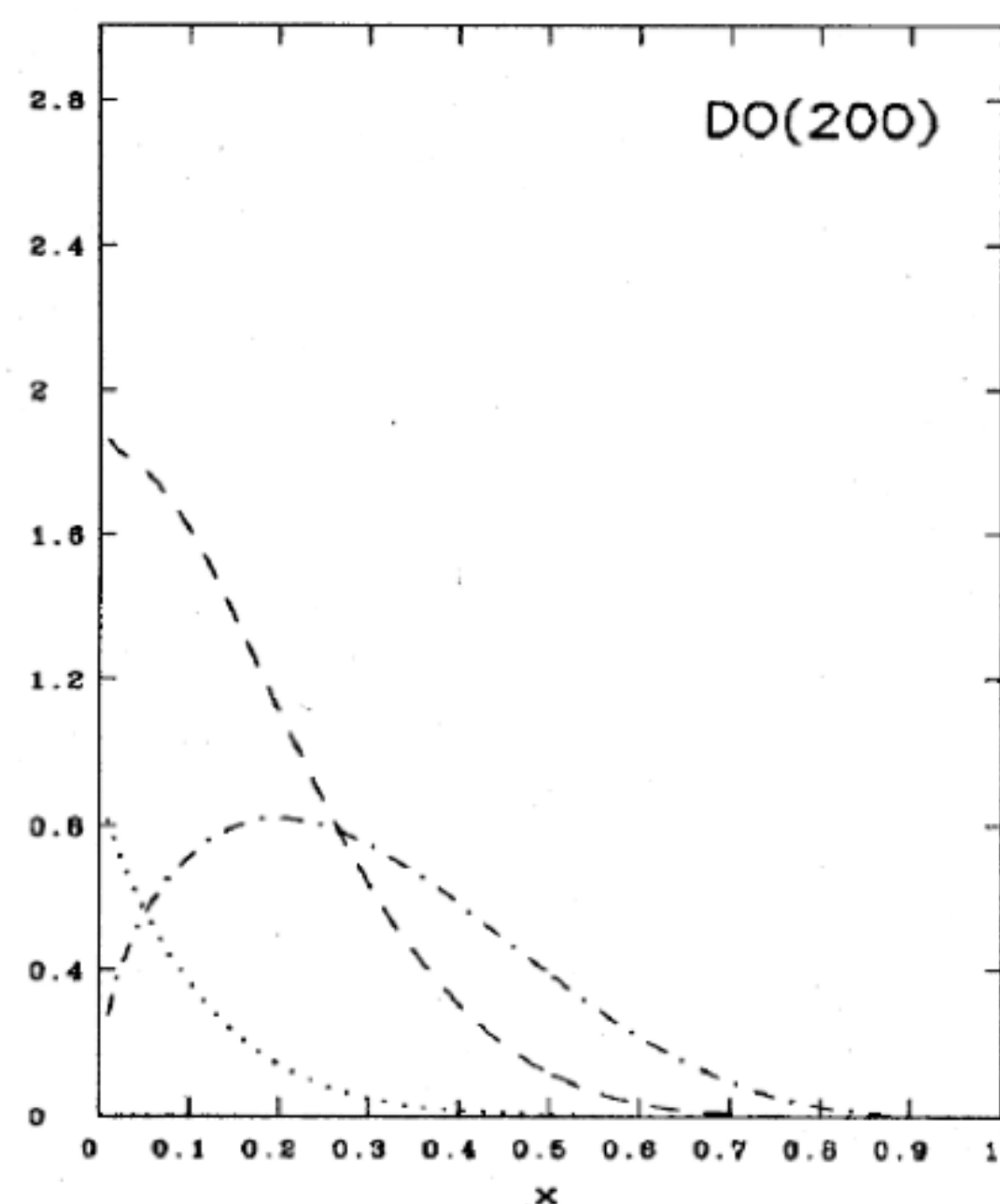
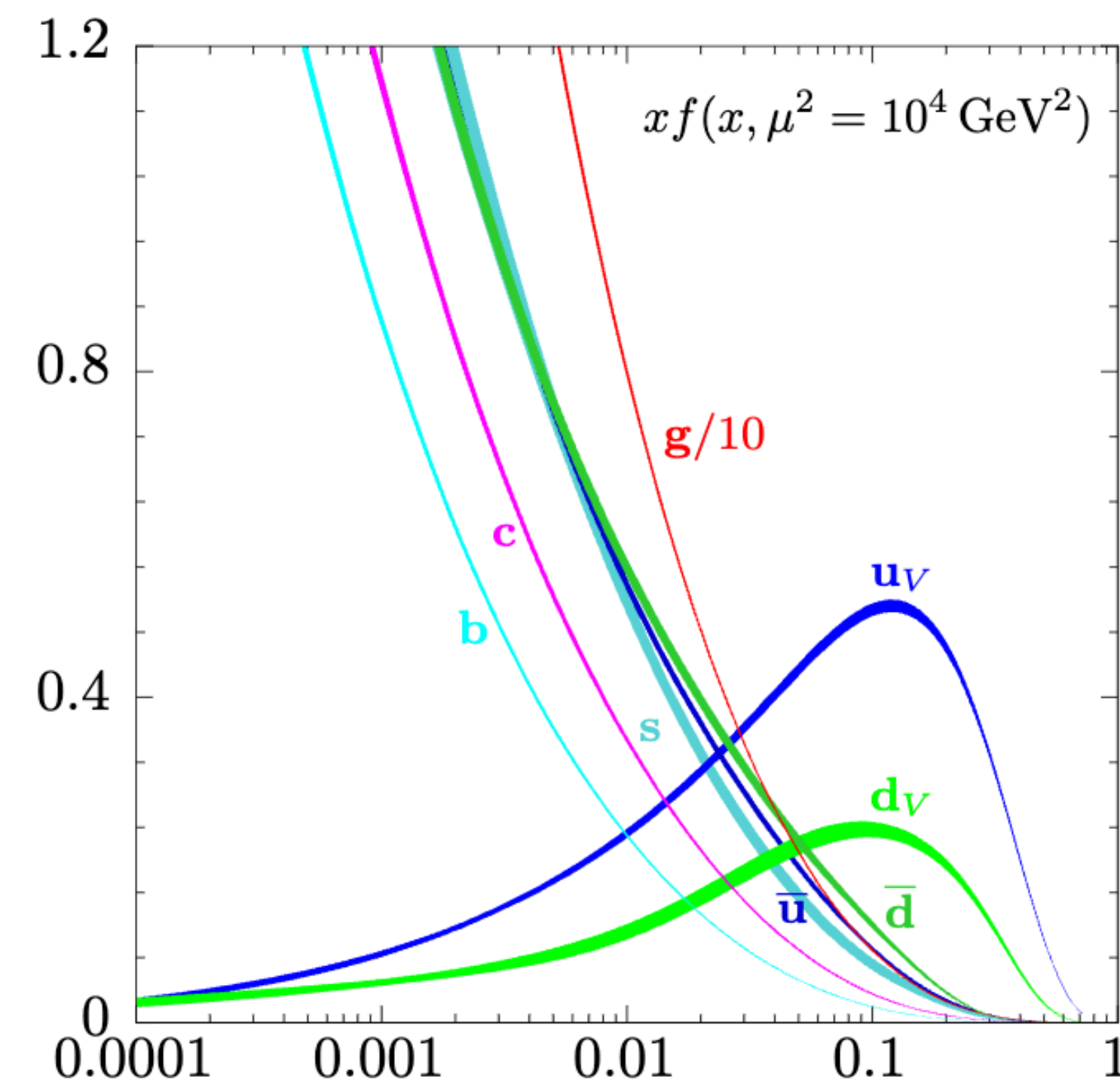
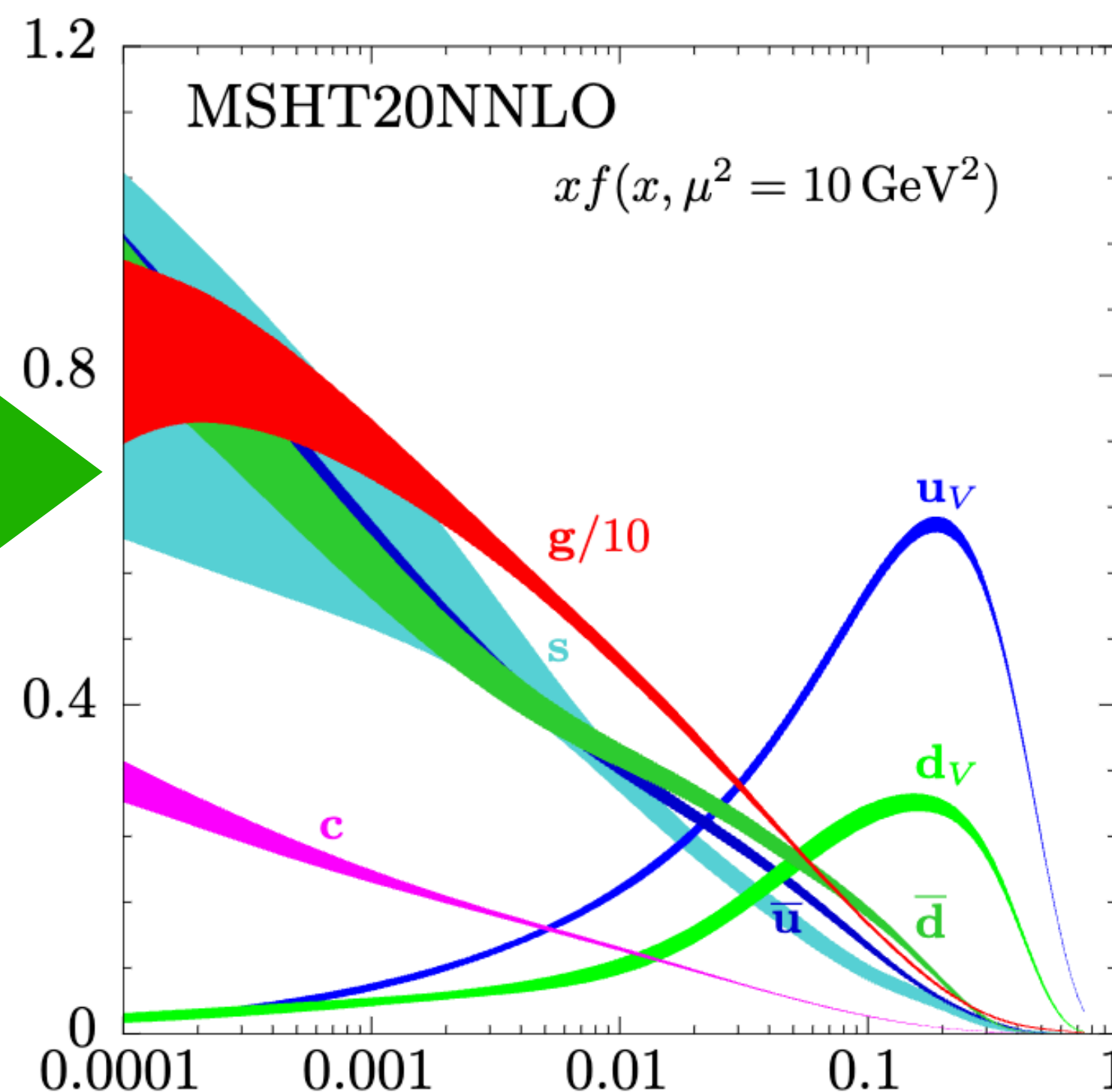
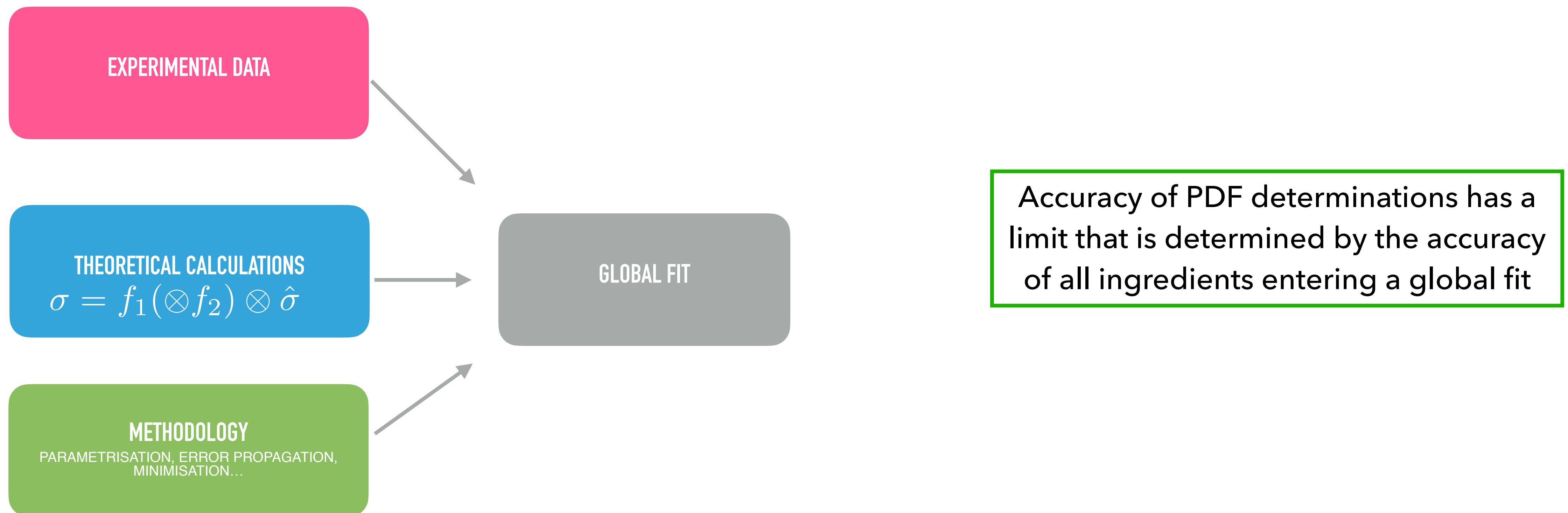


FIG. 27. “Soft-gluon” ($\Lambda=200$ MeV) parton distributions of Duke and Owens (1984) at $Q^2=5$ GeV²: valence quark distribution $x[u_v(x)+d_v(x)]$ (dotted-dashed line), $xG(x)$ (dashed line), and $q_v(x)$ (dotted line).



PDF DETERMINATION

- Huge progress from first PDF determinations to where we stand now
 - ➔ **Experimental data**: many more precise measurements constraining PDFs
 - ➔ **Theory**: heavy quark schemes, aN3LO PDFs, inclusion of MHOUs in PDF error bands, EW and QED corrections, initial photon...
 - ➔ **Methodology**: uncertainty propagation, parametrisation bias, closure tests,...



PROGRESS: DATA

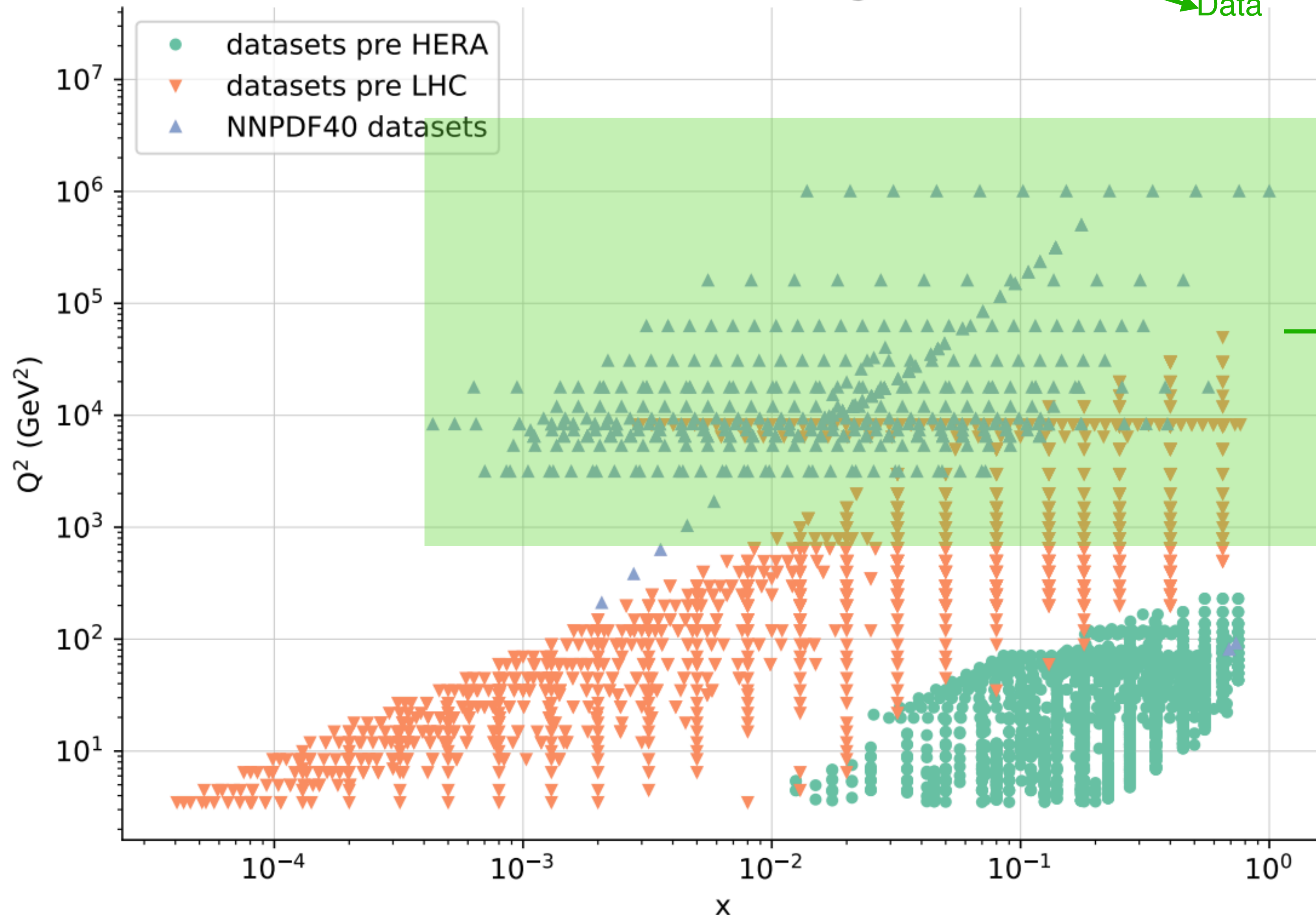
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$$f_i(x, \mu)$$

Perturbative QCD

Data

Kinematic coverage



Splitting functions P_{ab} known up to approximate N3LO

[Blumlein, Moch, Gehrmann, von Manteuffel, Sotnikov, Yang, Davies, Vogt, Bonvini, Marzani,...]

NNPDF4.0:

O(5000) datapoints,
about 30% from LHC

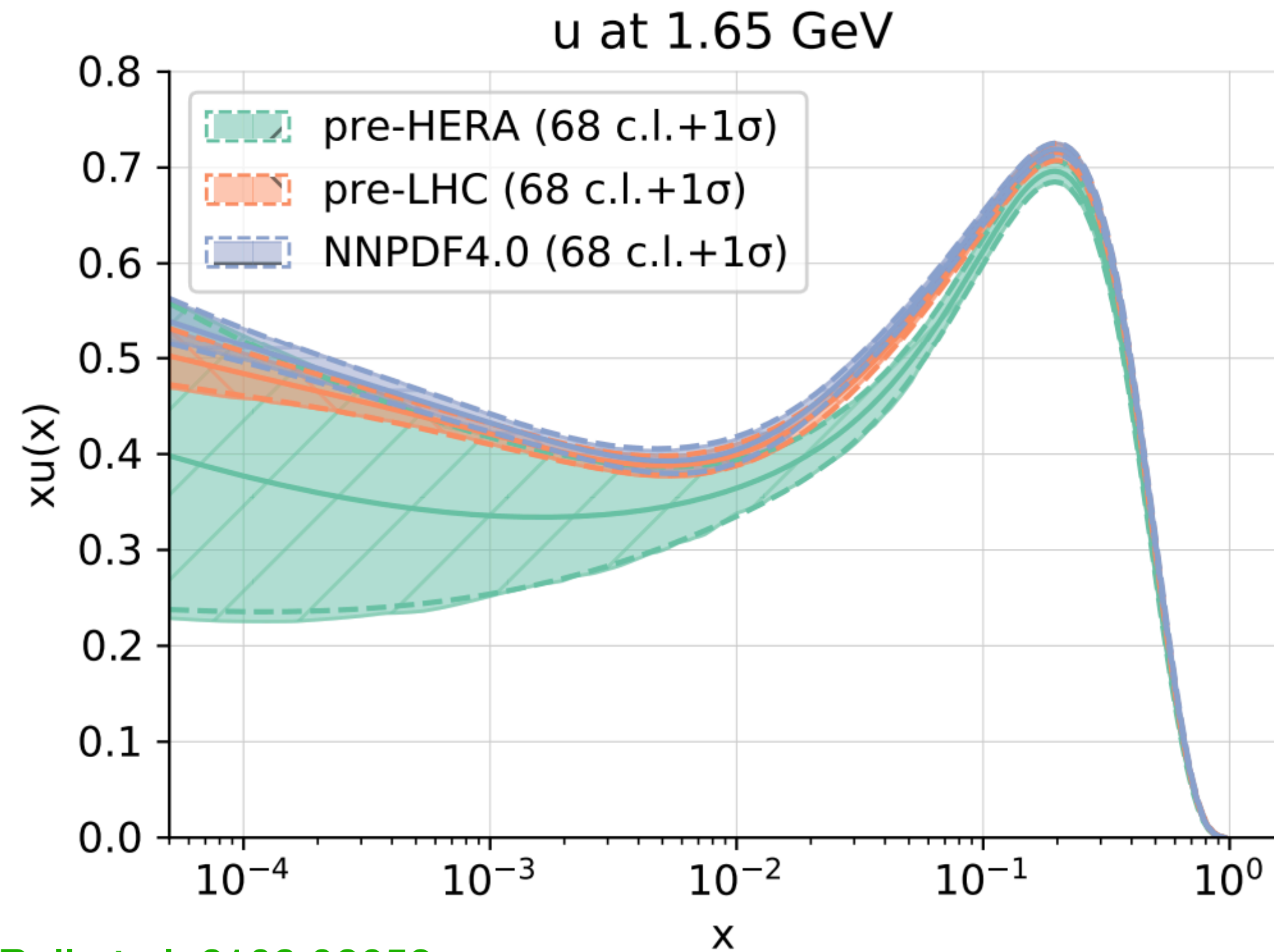
- Modern data show increasingly small statistical uncertainty and dominating correlated systematic uncertainties make global PDF fits challenging

Kassabov, Nocera, Wilson 2207.00690

Bailey, Harland-Lang 1909.10541

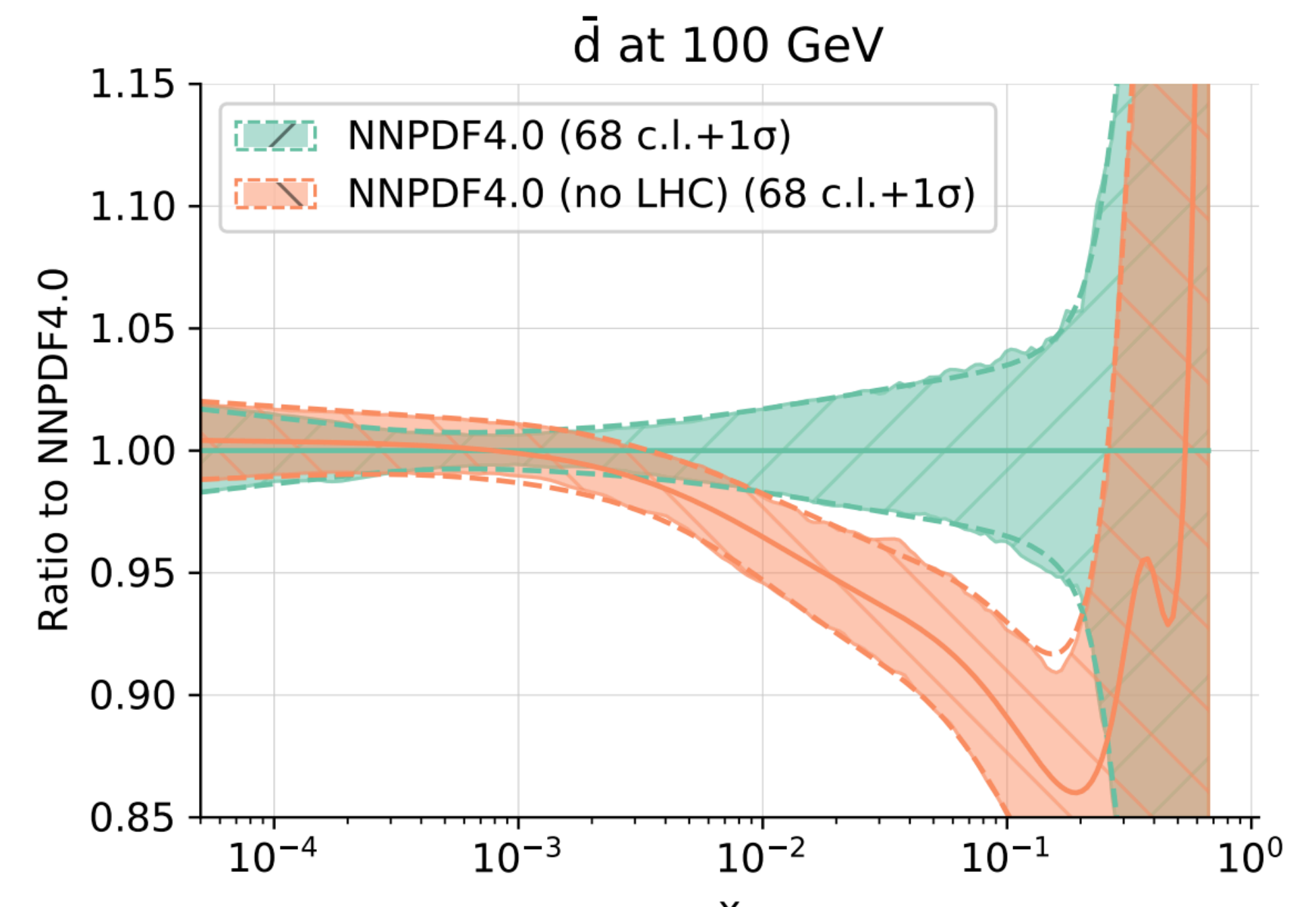
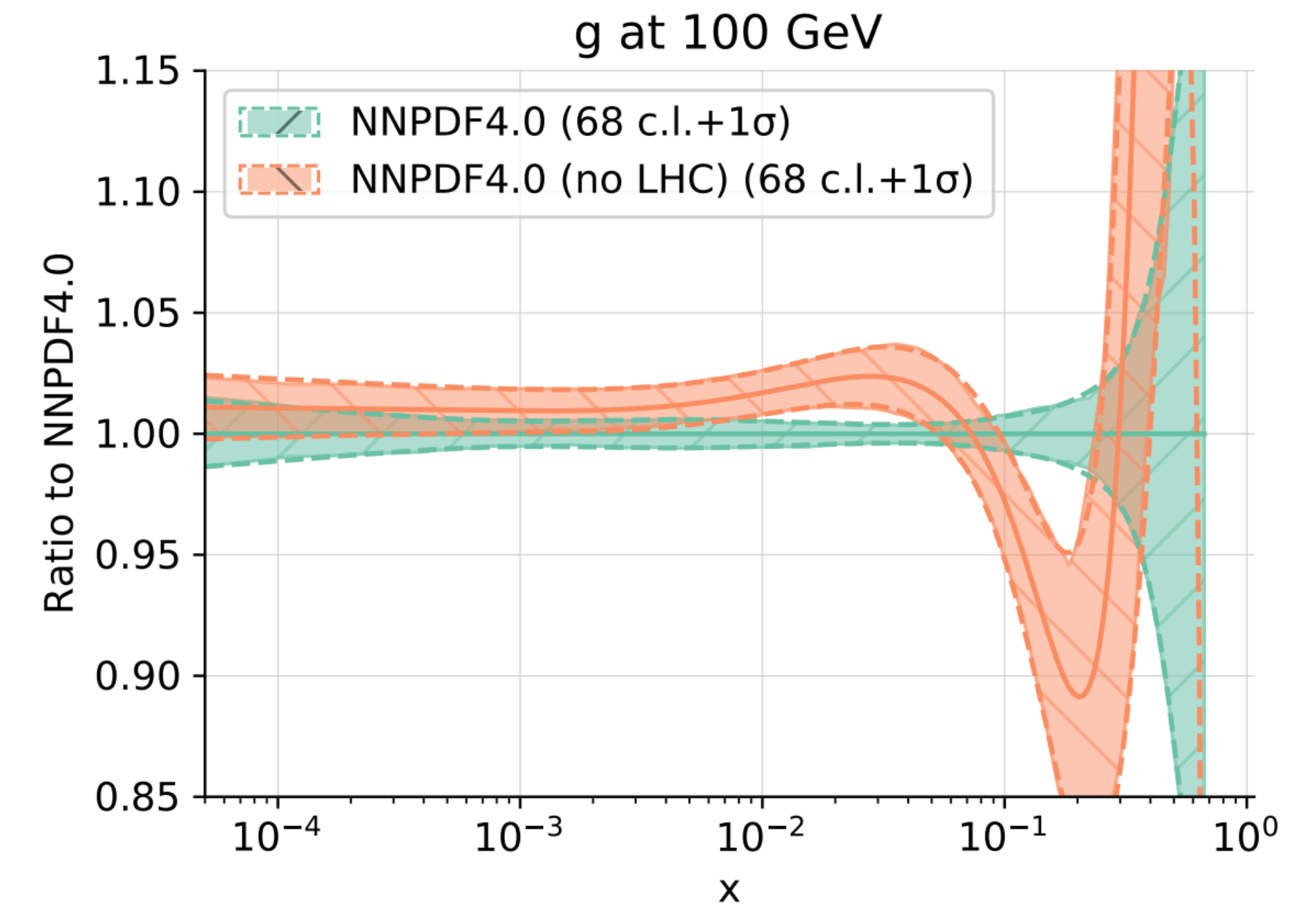
PROGRESS: DATA

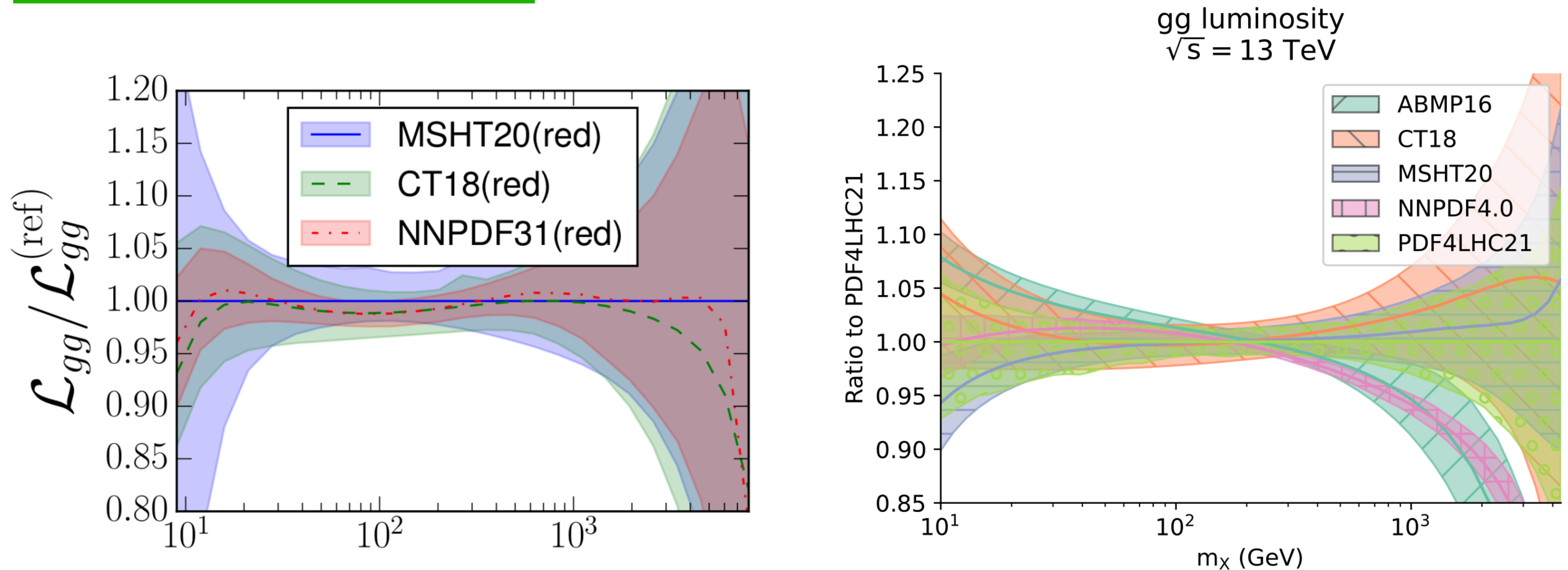
5/19



Ball et al, 2109.02653

- **HERA** data crucial to constrain quark valence (up and to less extent down valence) across intermediate to small x and gluon at small x
- **LHC** high energy data crucial to provide additional constraints to PDFs, in particular in medium- to large- x gluon and quarks.
- Some **tension** with older fixed-target Drell-Yan and DIS data visible in the large- x region (especially gluon and anti-quarks)





- In recent updates from global PDF fitting collaborations **effect of LHC data driving PDF uncertainties down**
 → PDF4LHC21 combination of NNPDF31', CT18' and MSHT20' smaller uncertainties than PDF4LHC15
- Benchmark among NNPDF3.1, MSHT20 and CT18: overall agreement, which improves once common dataset is used, **differences in uncertainties** associated with methodologies with $\Delta\text{CT18} \gtrsim \Delta\text{MSHT20} \gtrsim \Delta\text{NNPDF31}$
- Increased precision of the data and their strong correlation demands methodological improvements (e. g. **more flexible parametrisation** that shifts PDFs outside nominal error band) and **>1 PDF fits** to accomodate some tension (CT18 vs CT18Z)

PROGRESS: TESTING THE METHODOLOGY

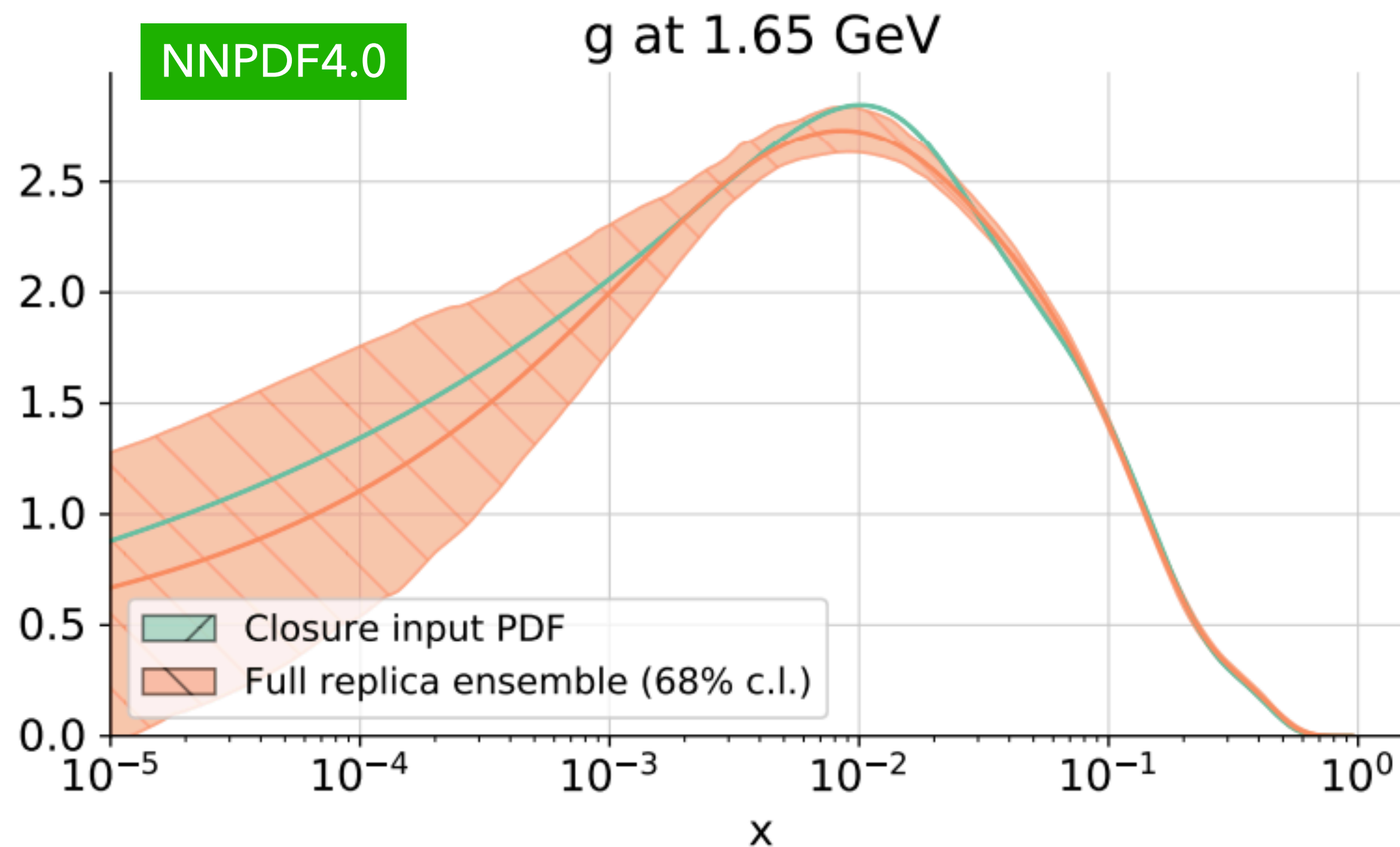
7/19

- Closure tests: key study to **statistically validate** various PDF fitting methodologies and **assess faithfulness of PDF uncertainties**
- Imagine we knew the law of Nature $G(w^0)$ and the true PDFs w^0 is fitting methodology able to reproduce it? Is the uncertainty faithful?
- Can also be used to check the effect of inconsistencies in the data
[Harland-Lang et al, arXiv:2407.07944, Costantini et al: arXiv:2503.17447]

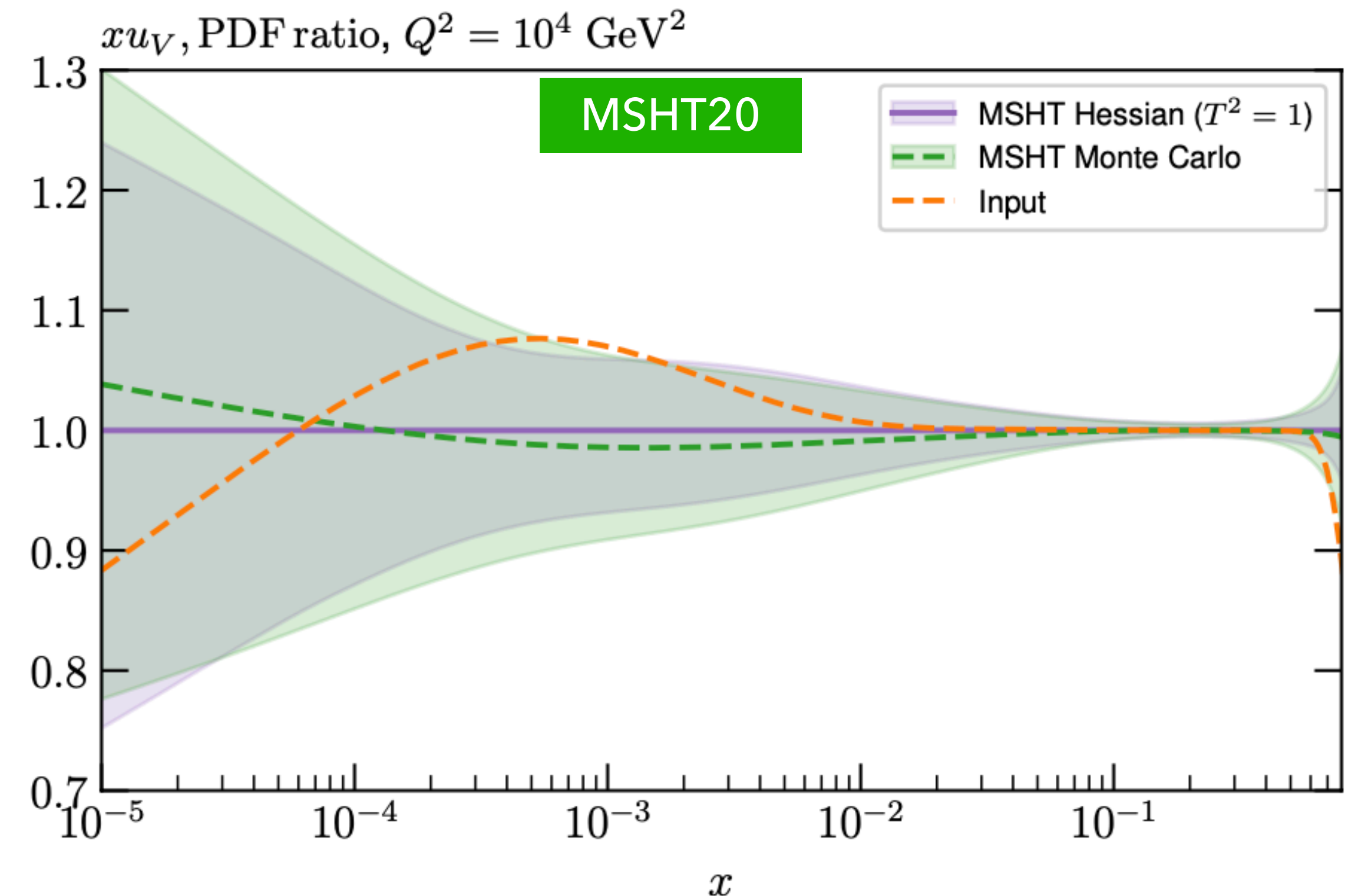
$$y_0 = \mathcal{G}(w^0) + \eta$$

Experimental noise

Law of Nature
 $\hat{\sigma}_{\text{NNLO}} \otimes (f \otimes f)$ "true" PDF



Del Debbio et al, [arXiv: 2111.05787]



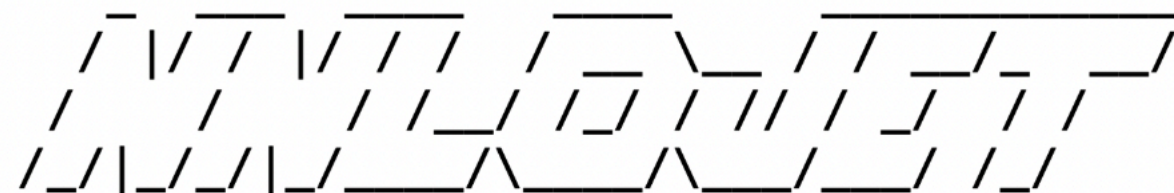
Harland-Lang et al, arXiv:2407.07944

PROGRESS: TESTING PDF PERFORMANCE ON NEW DATA

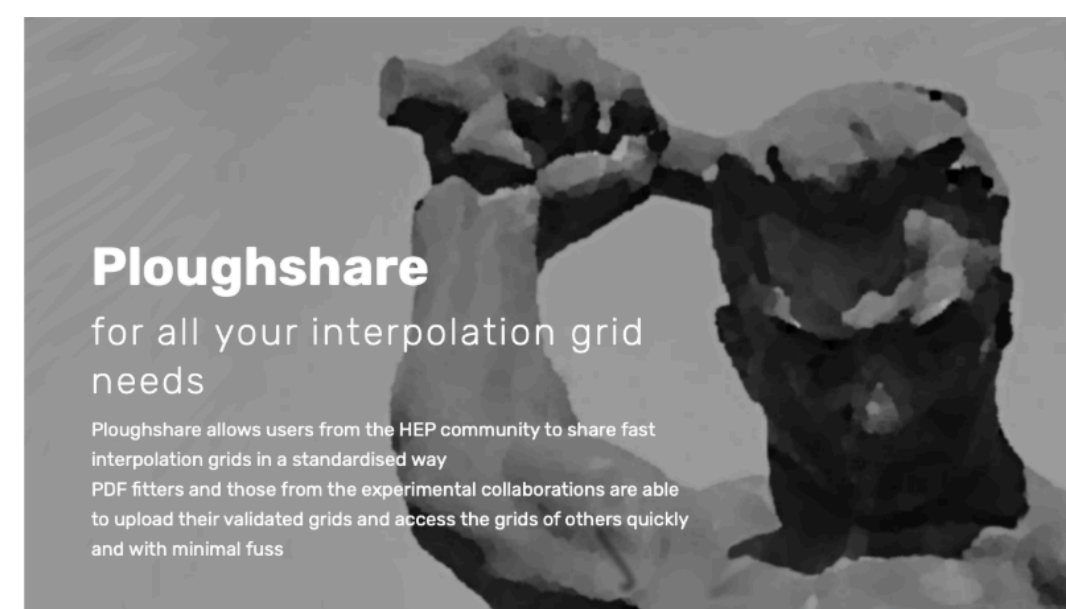
- To discriminate among PDF sets, test all global PDF sets against **new precise** data from LHC data & DIS HERA jets data. How well do various PDF sets describe data that are **not yet** included in the fit?
- Generalisation test** is crucial and possible using exact NNLO predictions (no k-factor approximation) thanks to PineAPPL, NNLOJET, MATRIX and Ploughshare

PineAPPL

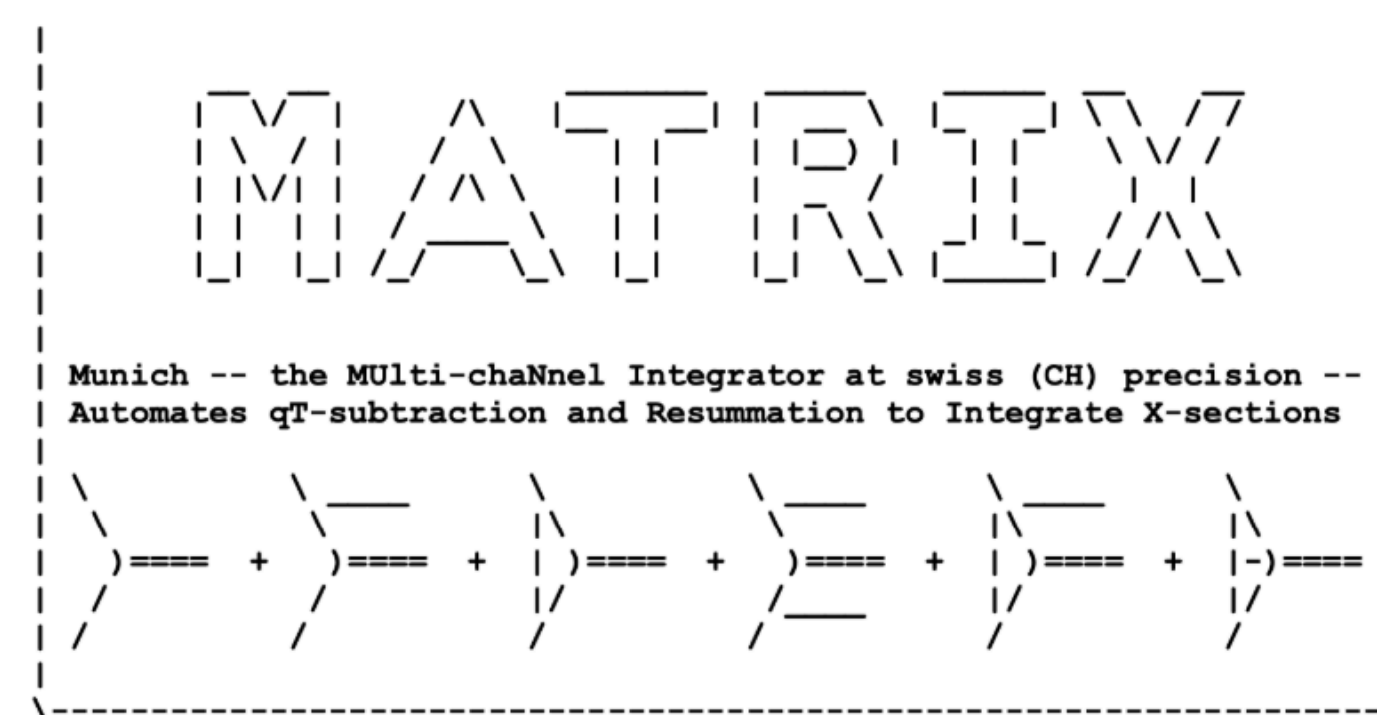
Carrazza et al: 2008.12789
Barontini et al: 2302.12124



Gehrman-De Ridder et al: 1507.02850,
1605.04295, 2301.11827, Britzger et al:
2207.13735, Cruz-Martinez et al: 2501.13167



Ploughshare project, APPLgrid, FastNLO
Kluge et al: hep-ph/0609285
Carli et al: 0911.2985
Czakon et al: 1704.08551



Grazzini et al: 1711.06631

- Data-theory agreement with unseen data must be measured by considering **all sources of uncertainties**: experimental, missing higher order (MHOU), PDF uncertainties, α_s uncertainties by including all bin-by-bin correlations

$$\chi^2 = \sum_{i,j=1}^{N_{\text{dat}}} \left(T_i^{(0)} - D_i \right) (\text{cov}^{-1})_{ij} \left(T_j^{(0)} - D_j \right)$$

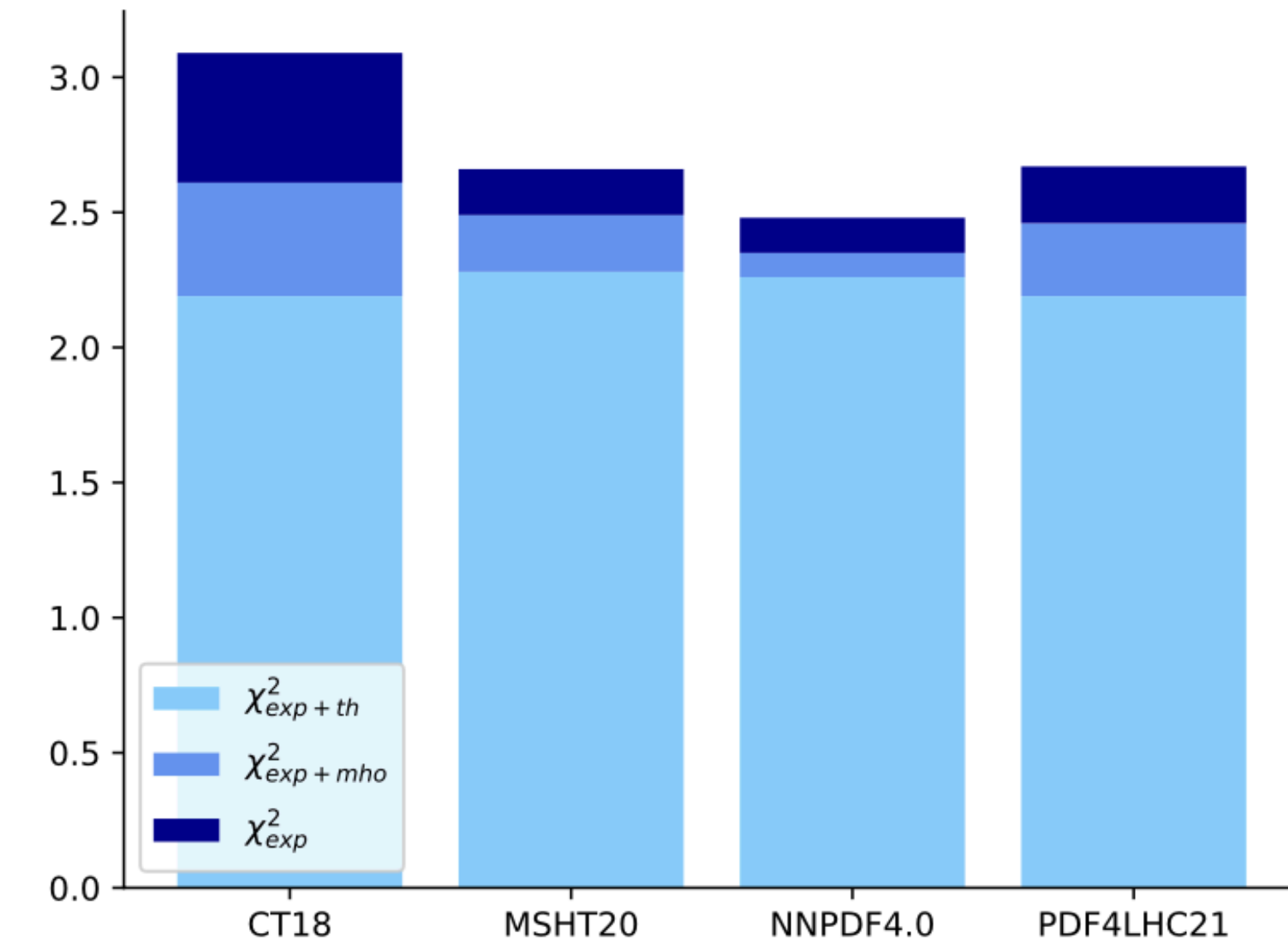
$$\chi_{\text{exp+mho+pdf+as}}^2 \leftrightarrow \text{COV} = \text{COV}_{\text{exp}} + \text{COV}_{\text{mho}} + \text{COV}_{\text{pdf}} + \text{COV}_{\text{as}}$$

HOW WELL DO MODERN PDF SETS PERFORM?

9/19

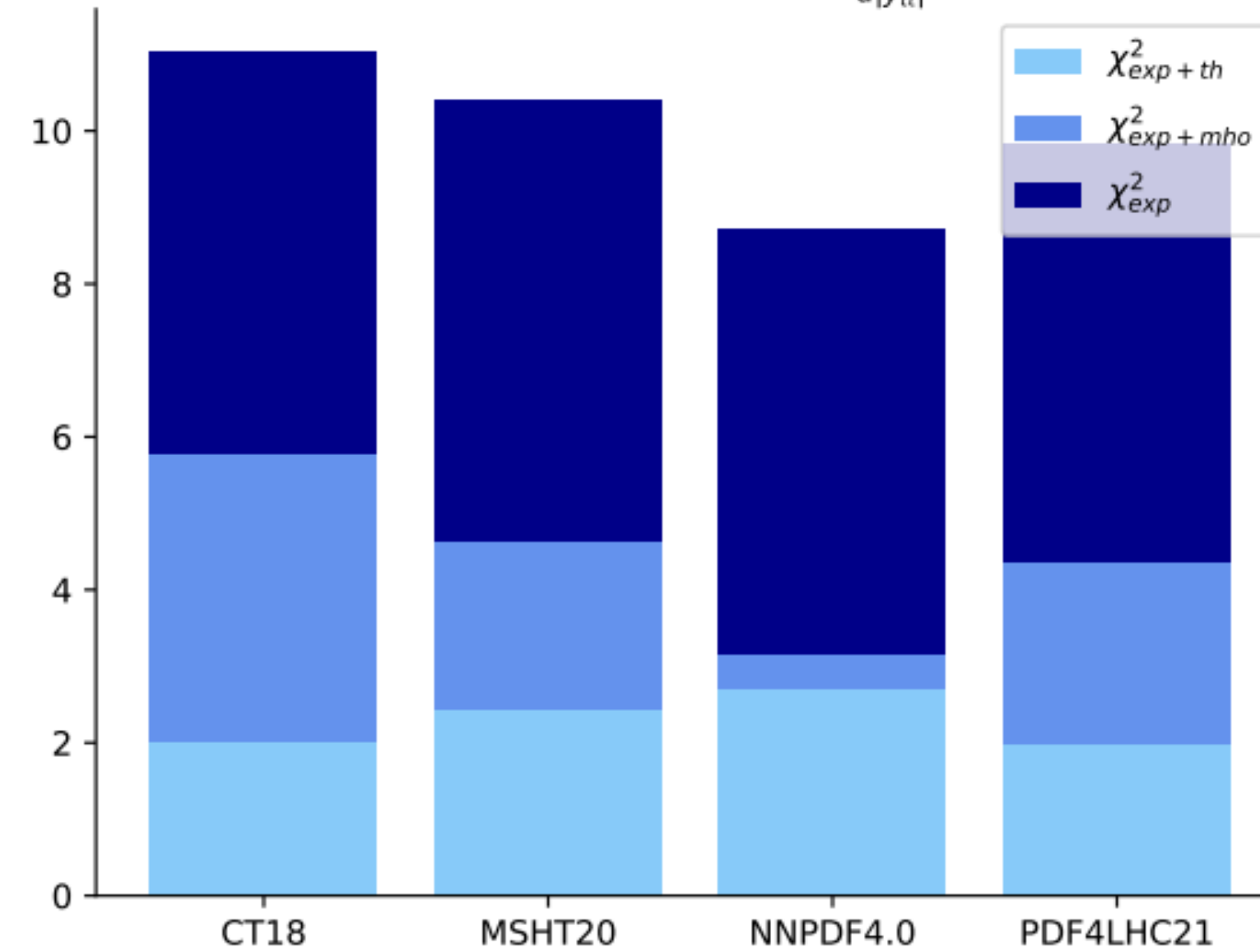
Chiefa et al: 2501.10359

LHCb $Z \rightarrow \mu\mu$



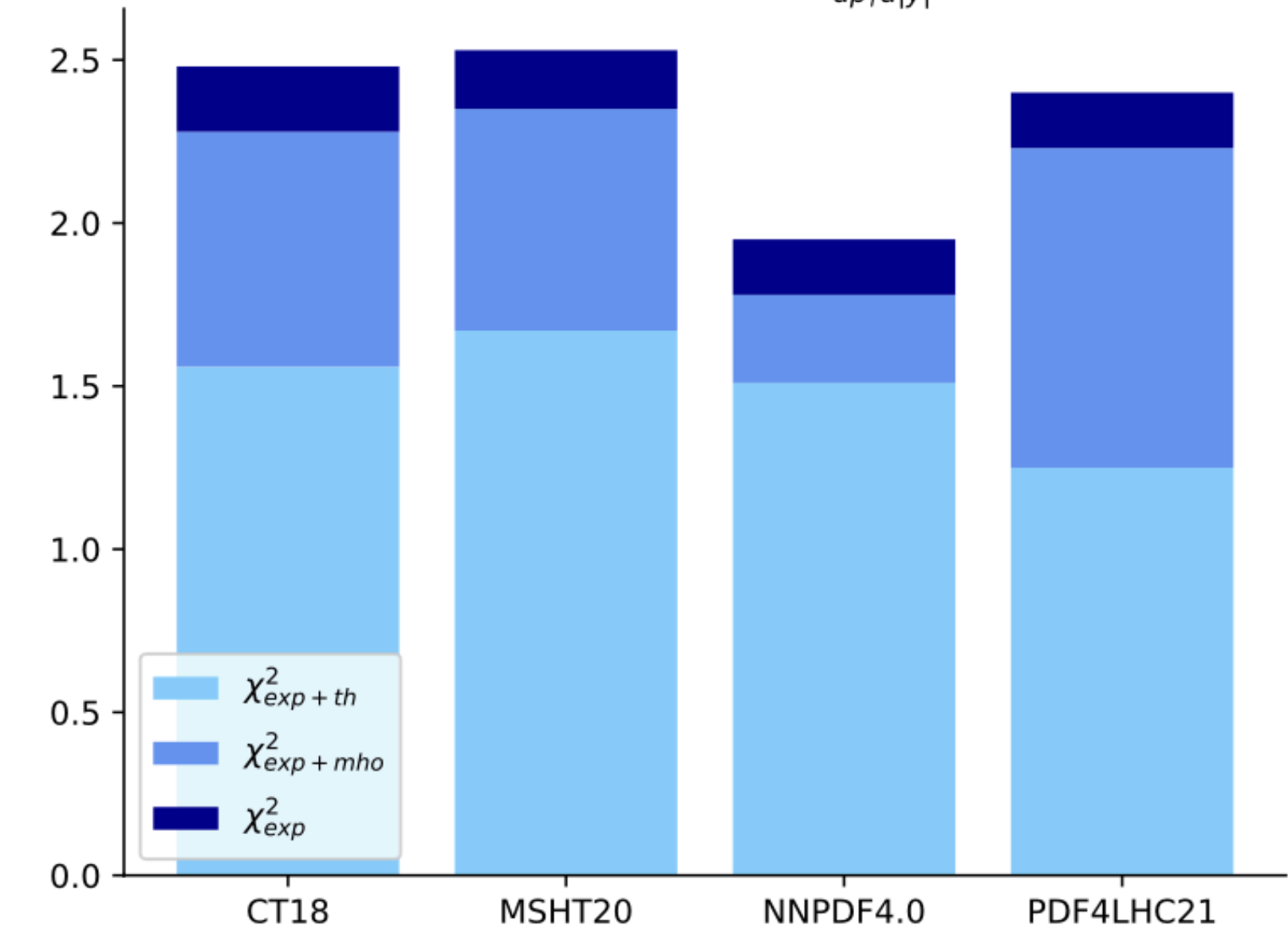
LHCb Z forward production at 13 TeV
LHCb collaboration [arXiv:2112.07458]

CMS 13 TeV $t\bar{t} \ell + j \frac{1}{\sigma} \frac{d\sigma}{d|y_{t\bar{t}}|}$



CMS $t\bar{t}$ production at 13 TeV, $l+j$
CMS collaboration [arXiv:2108.02803]

ATLAS Jet 13 TeV: $\frac{d^2\sigma}{dp_T d|y|}$

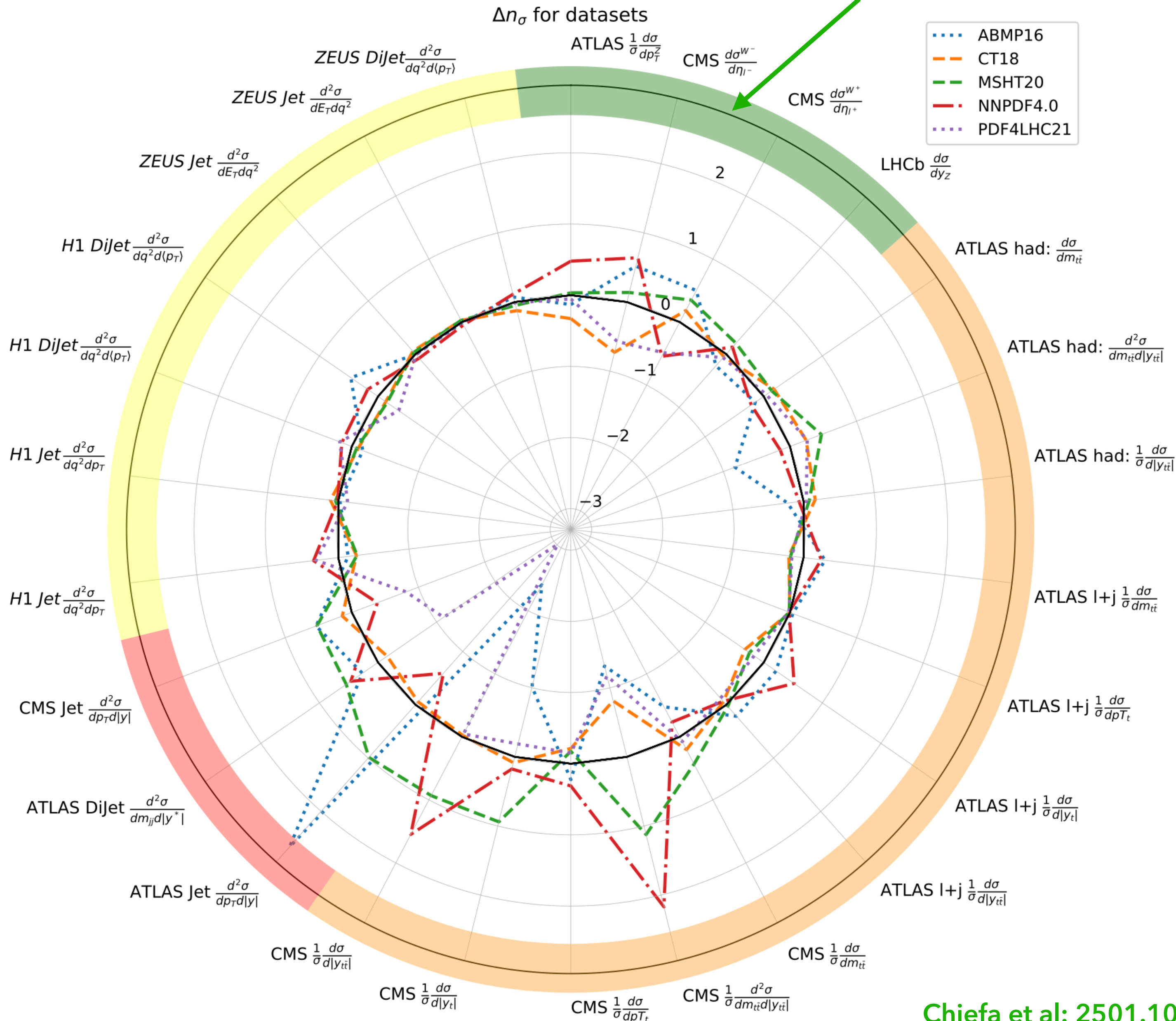
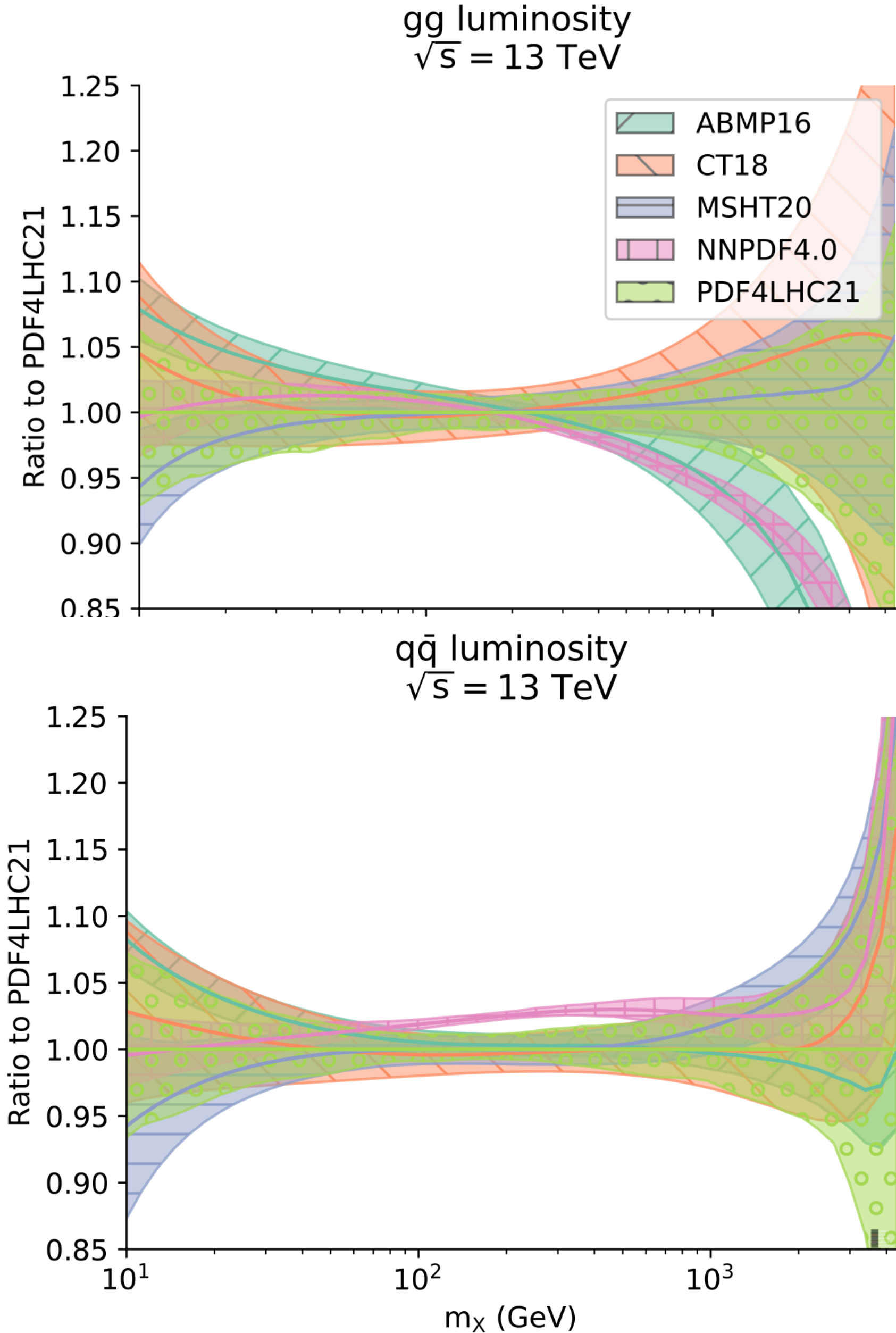


ATLAS incl. jet sec at 13 TeV, $R=0.6$, anti-kT
ATLAS collaboration [arXiv:1711.02692]

- Recently analysed 25 experimental distributions LHC@13 TeV and HERA jets measurements not yet included in any PDF analysis: inclusive jets, dijets, top differential distributions, W and Z production, Z pT, DIS jets [Chiefa et al, arXiv:2501.10359]
- Crucial to keep into account all sources of uncertainties and all bin-by-bin corrections.
- For some observables the inclusion of MHO uncertainties or PDF uncertainties changes the picture as compared to pure experimental χ^2
- LHC@13 TeV measurements do not strongly discriminate among PDF sets so far.
- NNPDF4.0, despite being the most precise (smallest PDF uncertainties in data region) yields good agreement with data!

HOW WELL DO MODERN PDF SETS PERFORM?

$$\Delta n_{\sigma}^{(i)} = \frac{\chi_{\text{exp+th}}^{2(i)} - \langle \chi_{\text{exp+th}}^2 \rangle_{\text{pdfs}}}{\sqrt{2/n_{\text{data}}}}$$

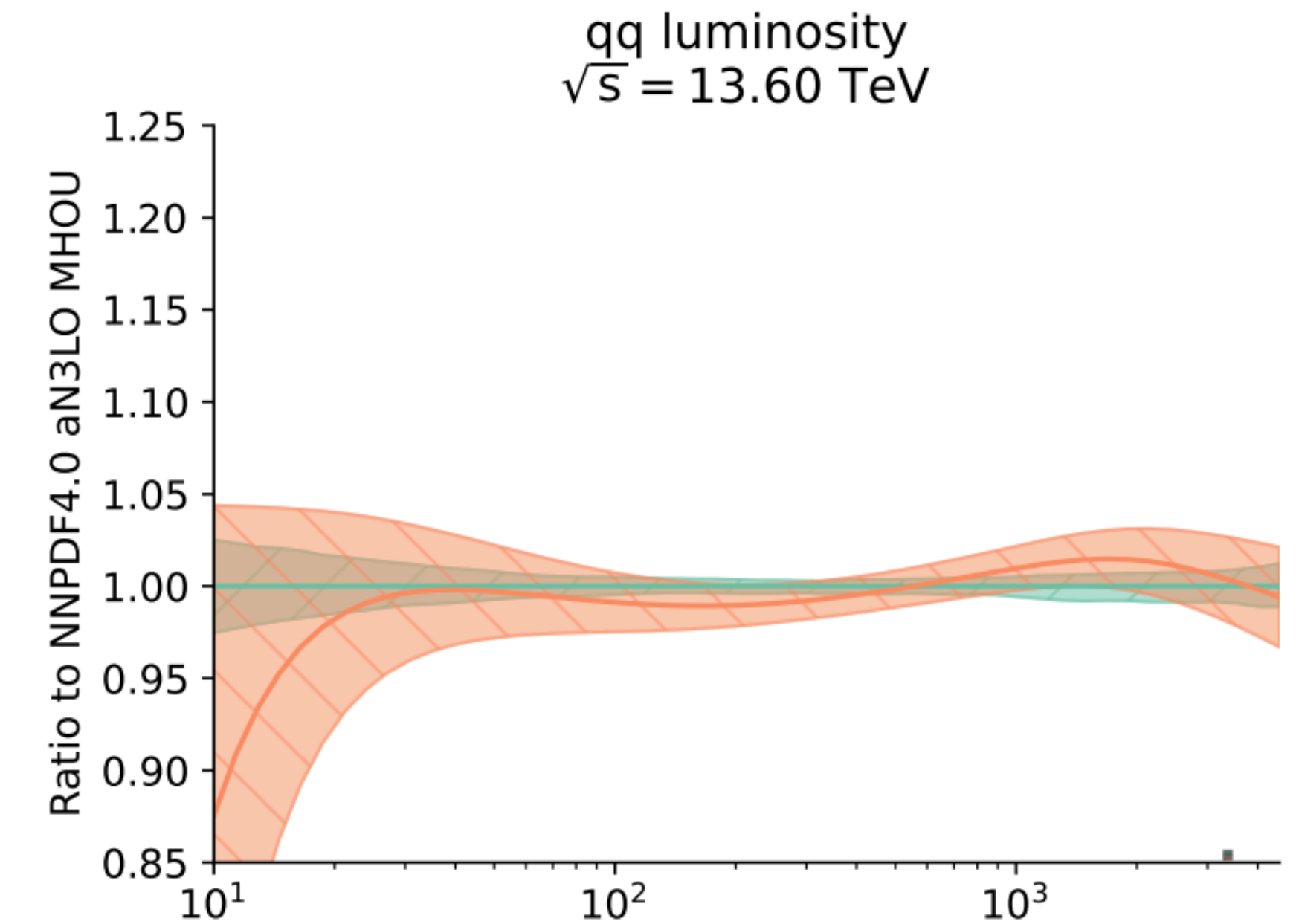
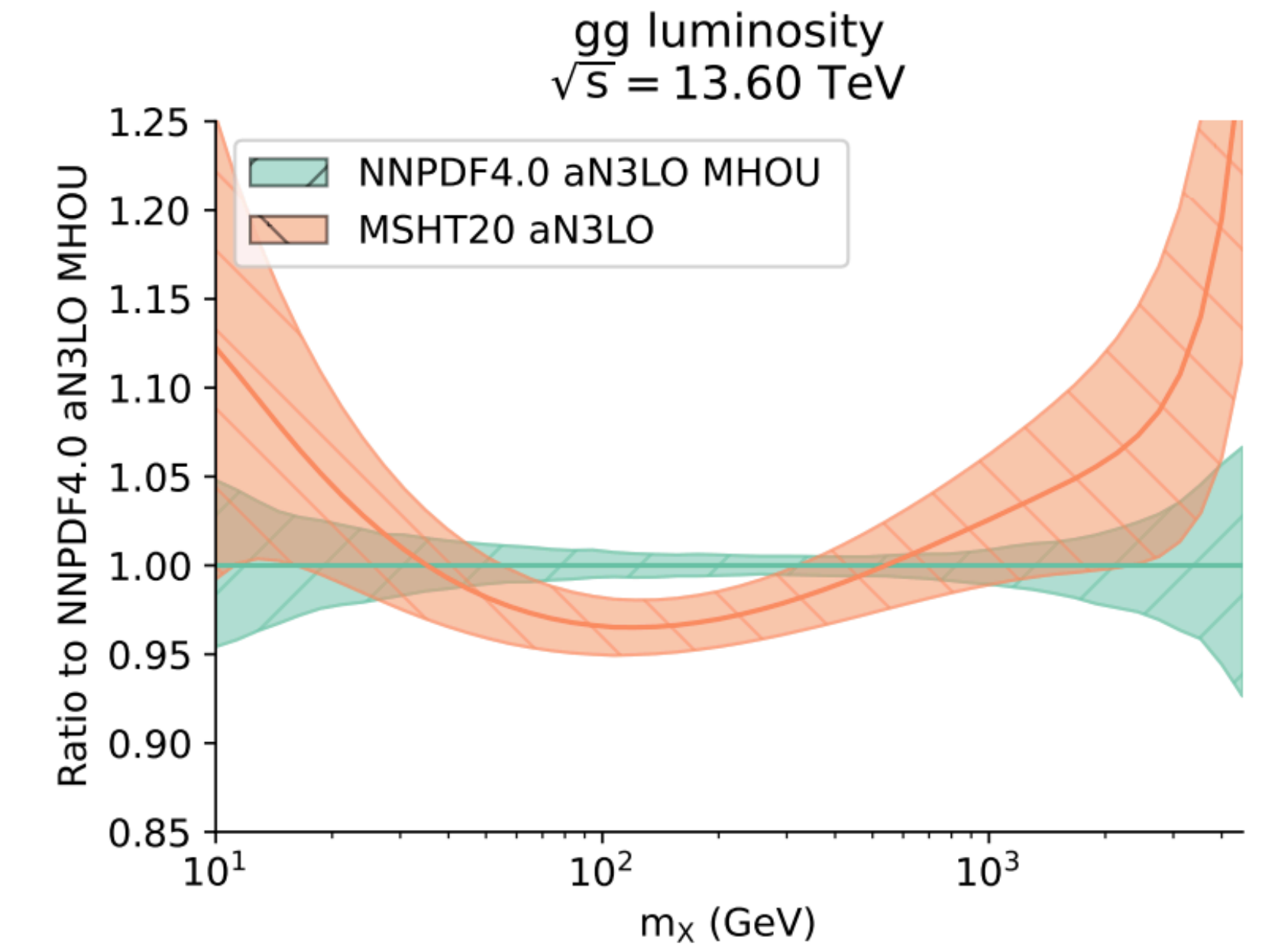


TOWARDS N3LO PDFS

11/19

First N3LO PDF sets by MSHT [McGowan et al 2207.04739] and NNPDF [Ball et al 2402.18635] collaborations

- Order-by-order convergence improved in both PDF sets and in phenomenological predictions
- Rather good agreement between collaborations' results considering different input included and strategies for the approximation
- aN3LO necessary to match the order of computation of partonic cross sections



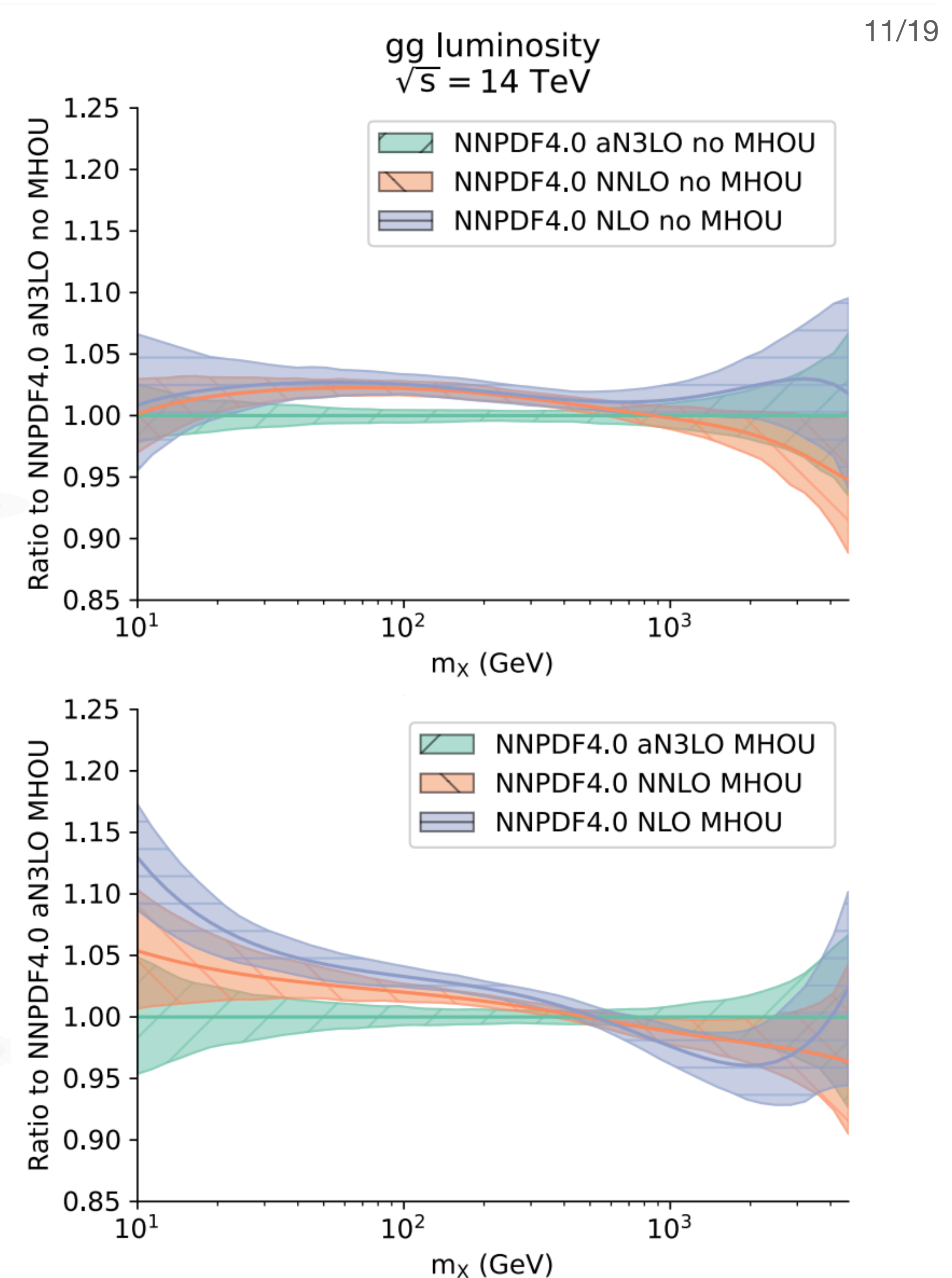
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- Rather good agreement between collaborations' results considering different input included and strategies for the approximation
- aN3LO necessary to match the order of computation of partonic cross sections

Results are not exact N3LO but rather aN3LO (approximated)

- Splitting functions not fully known, but known in enough limits and enough momenta to build a reasonable approximation [benchmark and references in arXiv:2406.16188]
- Fiducial pp predictions only accessible at NNLO (some only through K-factors)
- Effect of MHOUs estimated though scale variation greatly improves convergence



TOWARDS N3LO PDFS

Error estimate before aN3LO PDFs

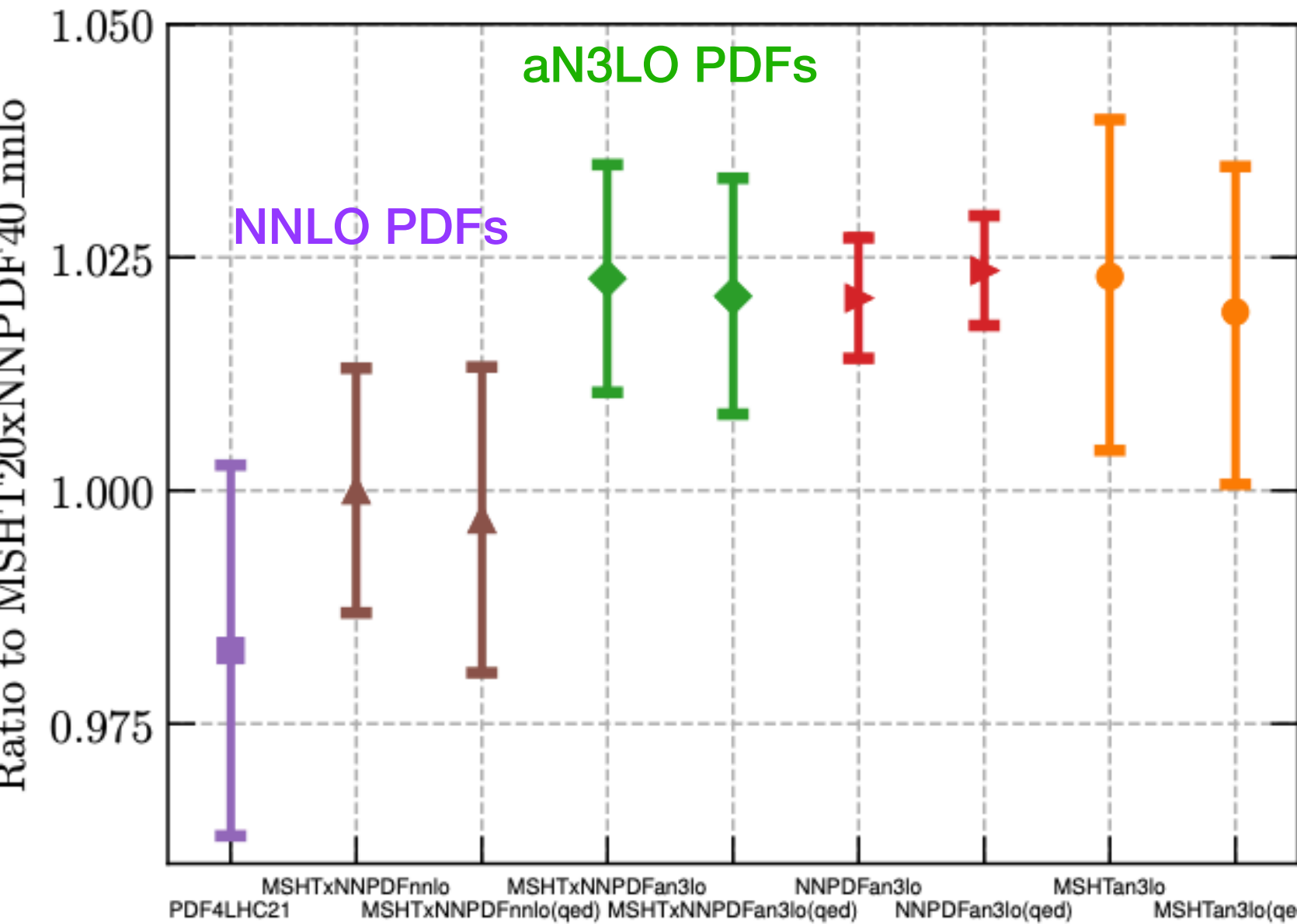
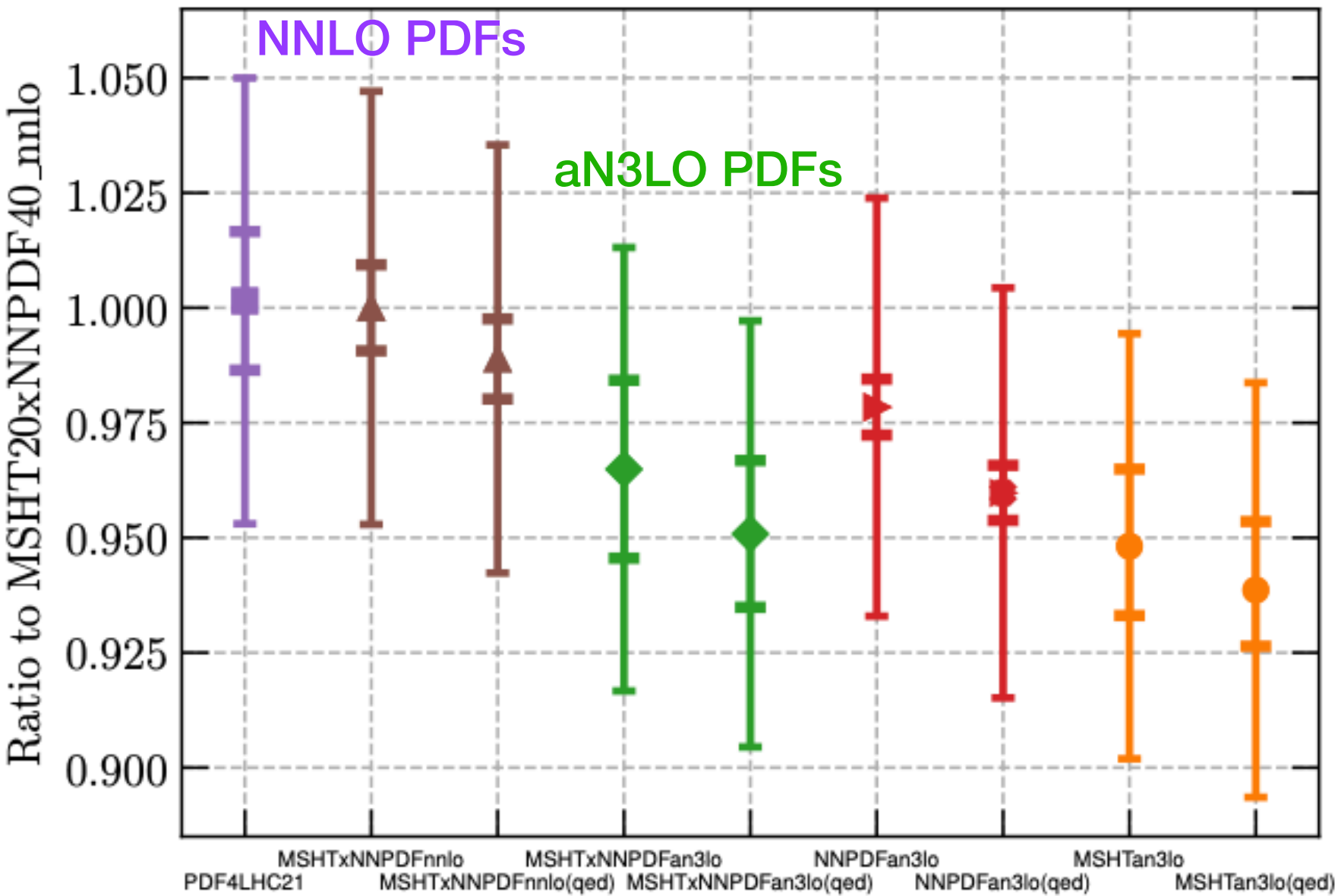
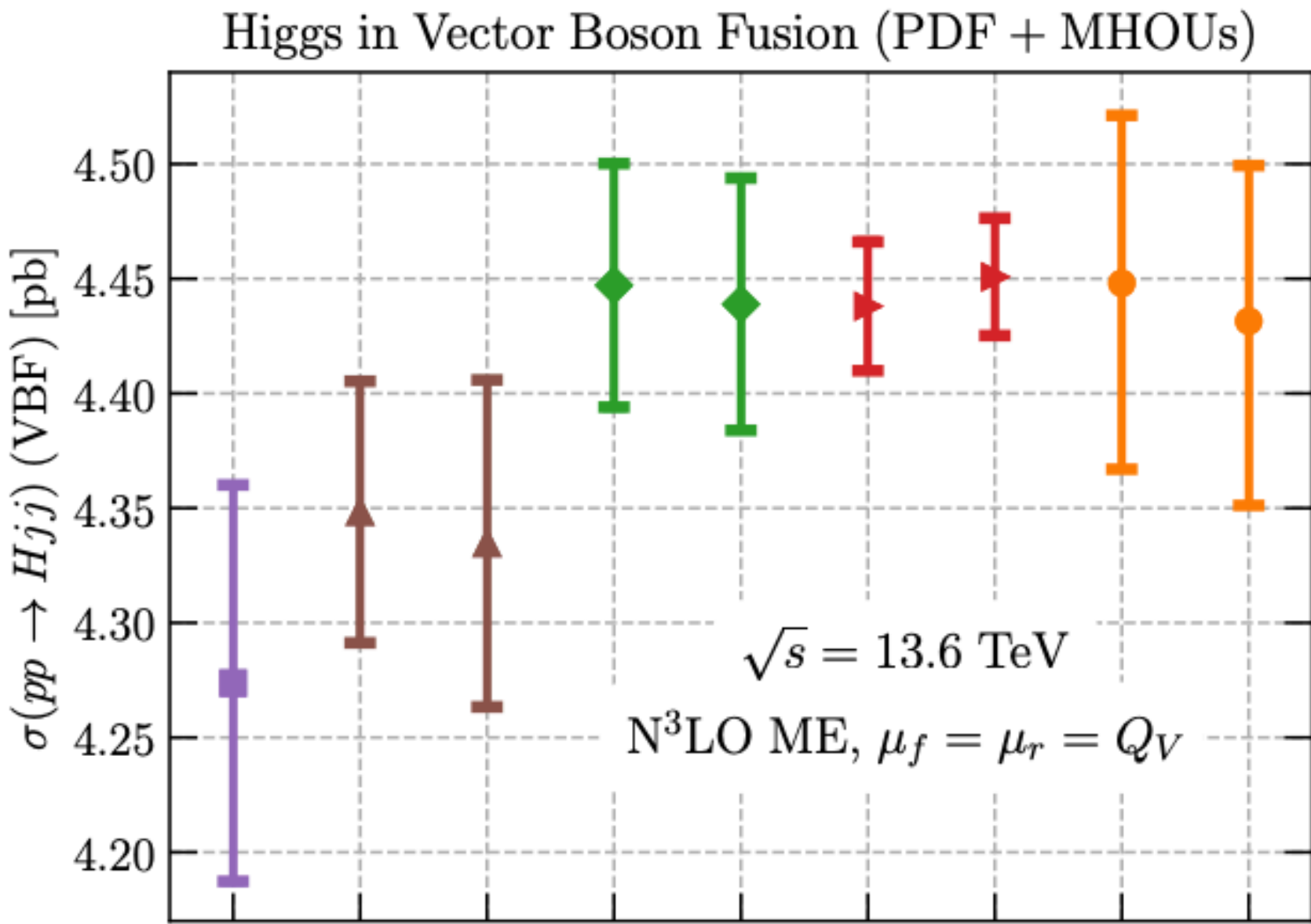
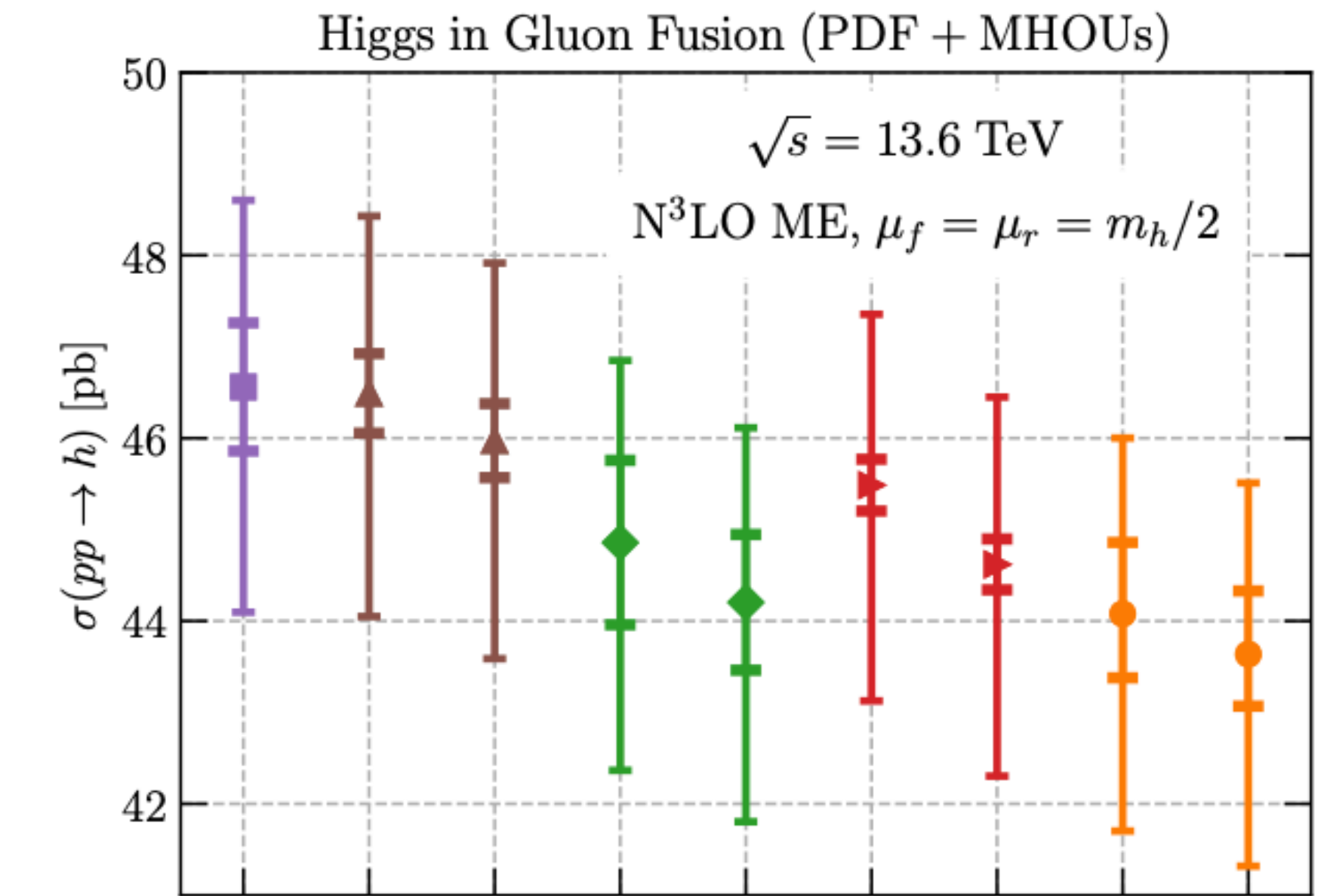
$$\Delta_{\text{NNLO}}^{\text{app}} \equiv \frac{1}{2} \left| \frac{\sigma_{\text{NNLO-PDF}}^{\text{NNLO}} - \sigma_{\text{NLO-PDF}}^{\text{NNLO}}}{\sigma_{\text{NNLO-PDF}}^{\text{NNLO}}} \right|$$

Actual error using aN3LO PDFs

$$\Delta_{\text{NNLO}}^{\text{exact}} \equiv \left| \frac{\sigma_{\text{N}^3\text{LO-PDF}}^{\text{N}^3\text{LO}} - \sigma_{\text{NNLO-PDF}}^{\text{N}^3\text{LO}}}{\sigma_{\text{N}^3\text{LO-PDF}}^{\text{N}^3\text{LO}}} \right|$$

	ggF	VBF
$\Delta_{\text{NNLO}}^{\text{(app)}}$	1.6%	0.5%
$\Delta_{\text{NNLO}}^{\text{(actual)}}$	3.3%	2.3%

Previous estimates of the effect of NNLO/N3LO mismatch were **optimistic**



PART II: PRECISION VS ACCURACY – NEW CHALLENGES, NEW FRONTIERS

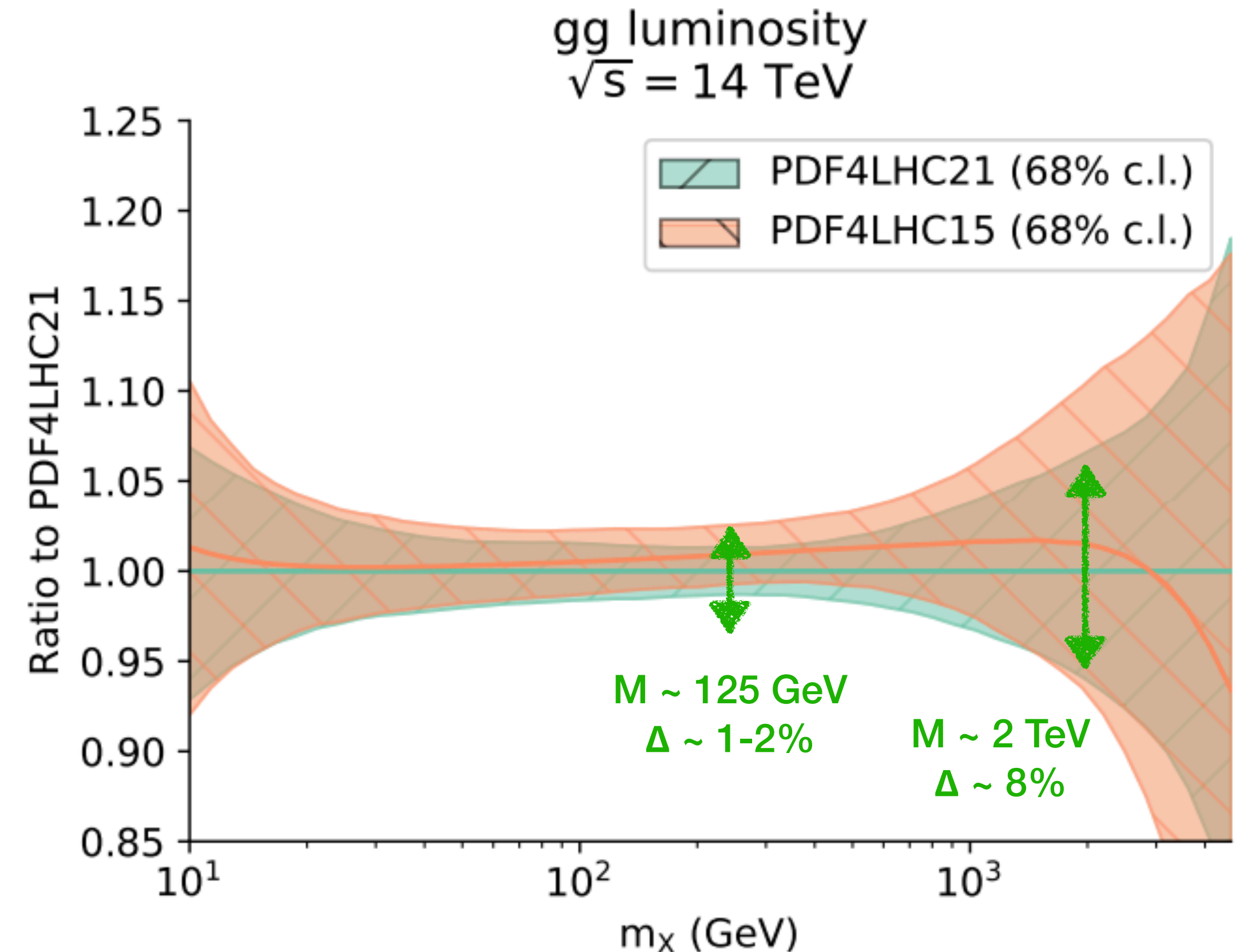
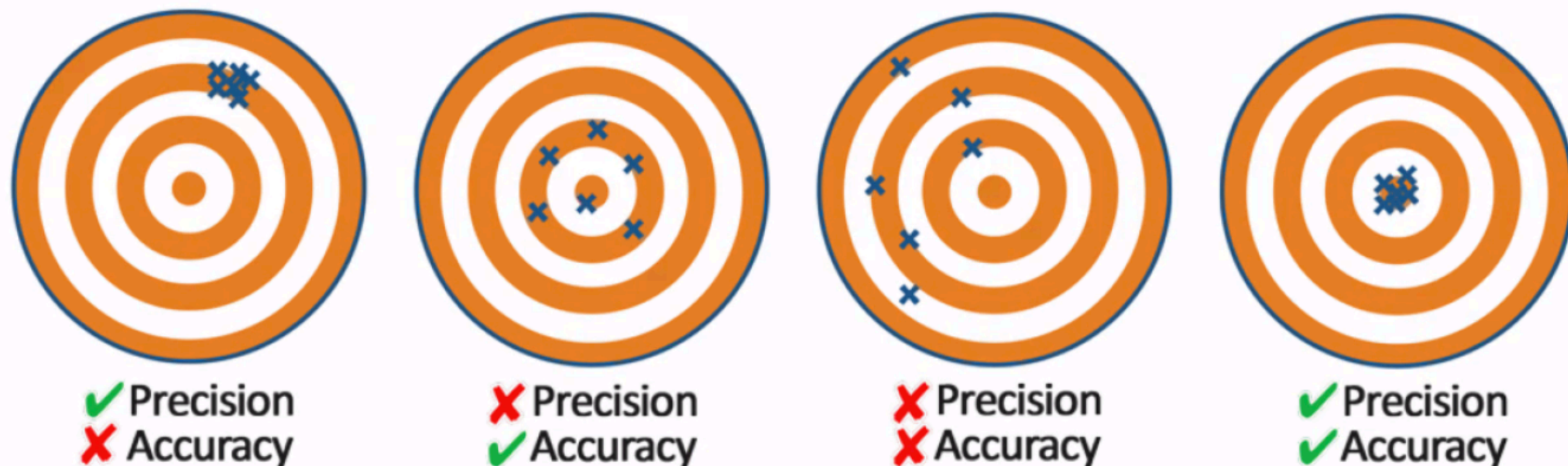
THE PRECISION VERSUS ACCURACY CHALLENGE

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At a time of precision physics, it is time for precision PDF determination, does precision match accuracy?

Highly non trivial challenges

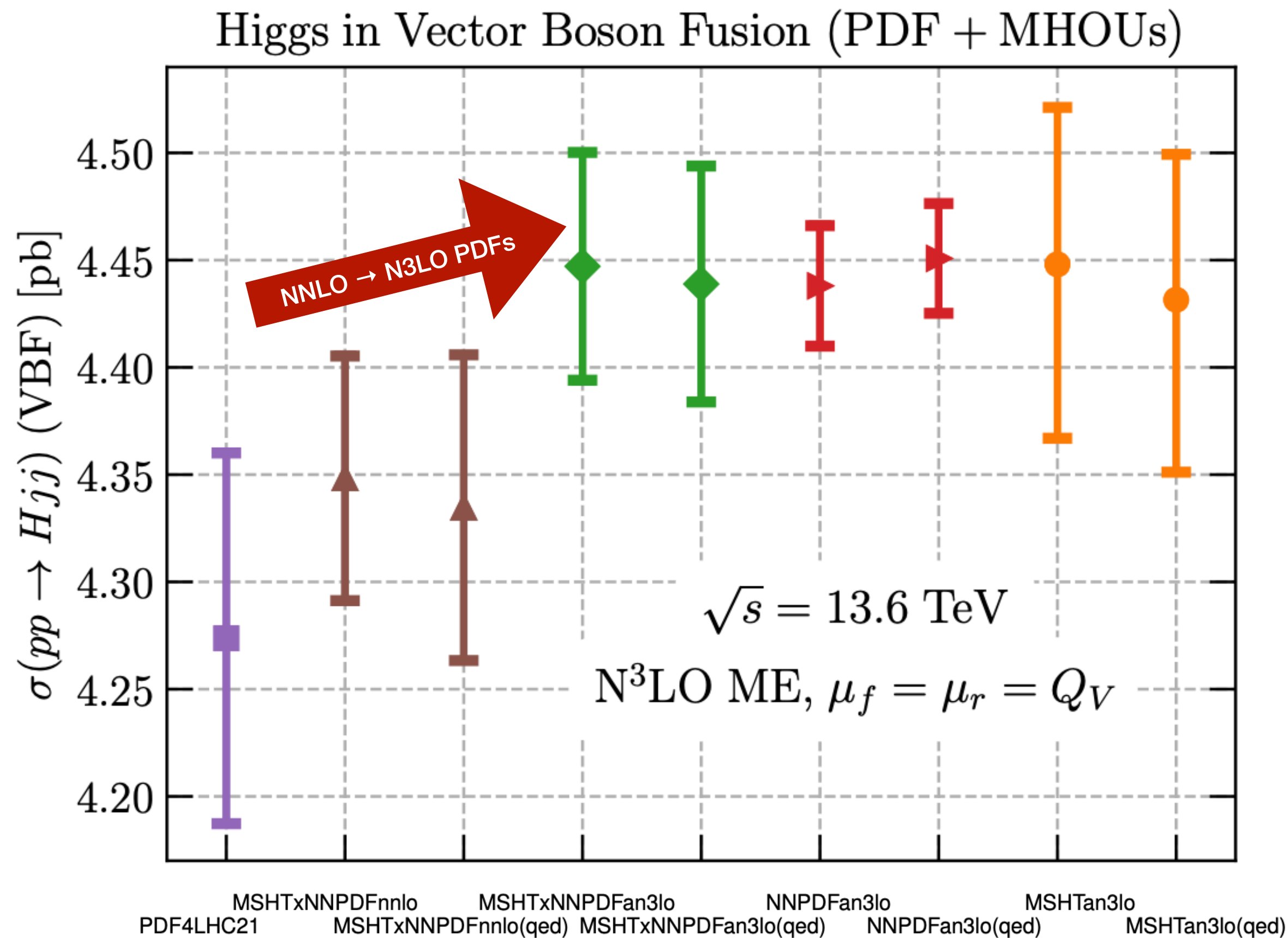
- ▶ Genuine inconsistencies in experimental inputs (possible underestimated, over-correlated systematics...)
- ▶ Imperfect fitting methodology (parametrisation, error propagation...)
- ▶ Inaccurate theoretical framework
 - ➔ Missing higher orders (exact N3LO, resummation...)
 - ➔ Other corrections (electroweak, nuclear, higher-twists, other non-perturbative effects...)
 - ➔ BSM effects in the high energy tails of distributions



PDF4LHC21 study 2203.05506

CHALLENGE #1: N3LO PDFS AND MISSING HIGHER ORDER UNCERTAINTIES

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e.g. Higgs in VBF @ N3LO

MSHT+NNPDF [arXiv:2411.05373](https://arxiv.org/abs/2411.05373)

- Shift between results obtained with NNLO PDFs and with aN3LO PDFs more significant than expected
- Next steps:
 - As more N3LO theory ingredients become available, **aN3LO PDFs updated** by improving convergence of results obtained with different methodologies
 - **Exact N3LO evolution**, exact NNLO grids for hadronic coefficients and N3LO k-factors
- Every step of the way becomes computationally more costly and complex for a smaller and smaller improvements. But **extremely needed!**
- What about other effects? Resummation, higher twists, power correction...
- Estimate of incomplete N3LO terms and MHO uncertainties still computed via scale variations: is there a better way?

CHALLENGE #2: DETERMINATION OF SM PARAMETERS

PDF set	$\alpha_s(m_Z)$	PDF uncertainty	g [GeV ²]	q [GeV ⁴]
MSHT20 [37]	0.11839	0.00040	0.44	−0.07
NNPDF4.0 [84]	0.11779	0.00024	0.50	−0.08
CT18A [29]	0.11982	0.00050	0.36	−0.03
HERAPDF2.0 [65]	0.11890	0.00027	0.40	−0.04

ATLAS collaboration, arXiv:2309.12986

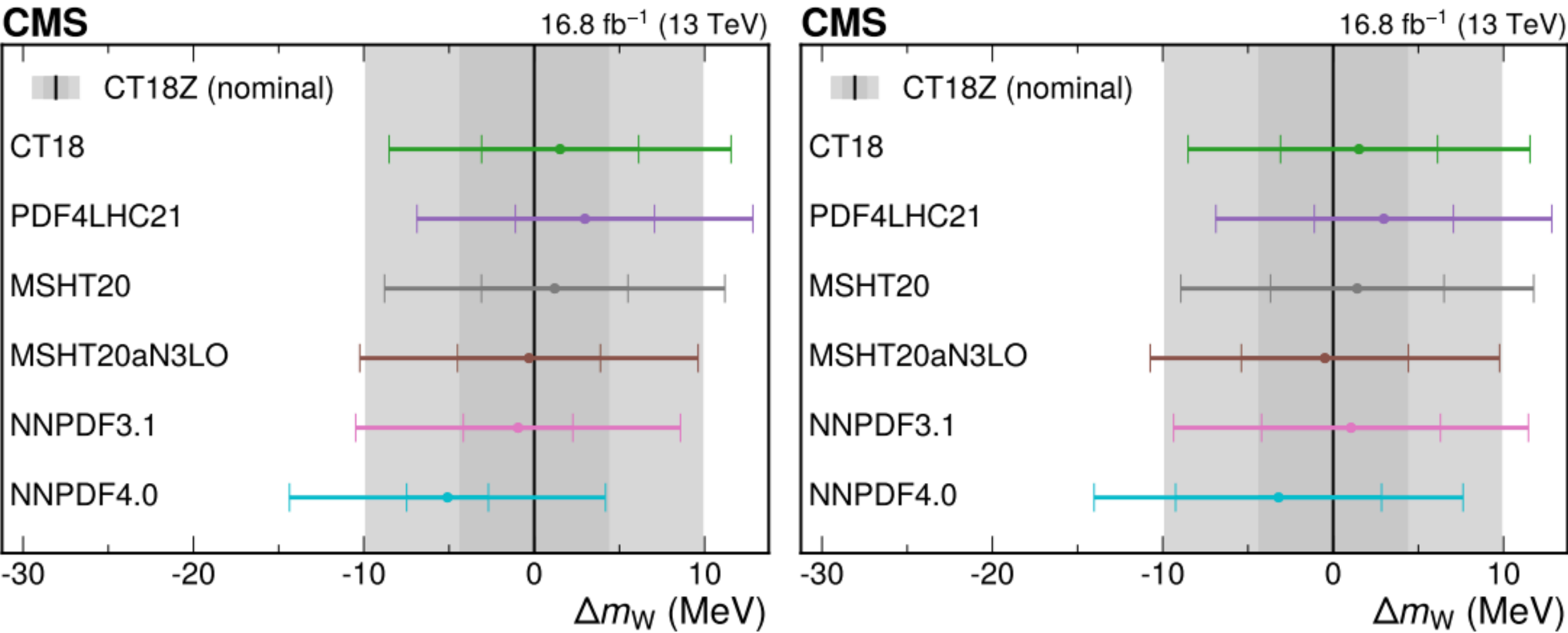
Significantly different results obtained when using different input PDFs.

- ATLAS determination of α_s from neutral-current Drell-Yan Z pT measurement most precise α_s determination ever performed from a single experiment
 $\Delta_{\alpha,\text{TOT}} = 9 \times 10^{-4}$ with $\Delta_{\alpha,\text{PDF}} = 5 \times 10^{-4}$ (MSHT20aN3LO)
But
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ATLAS collaboration, arXiv:2309.12986



CMS collaboration, arXiv: 2412.13872

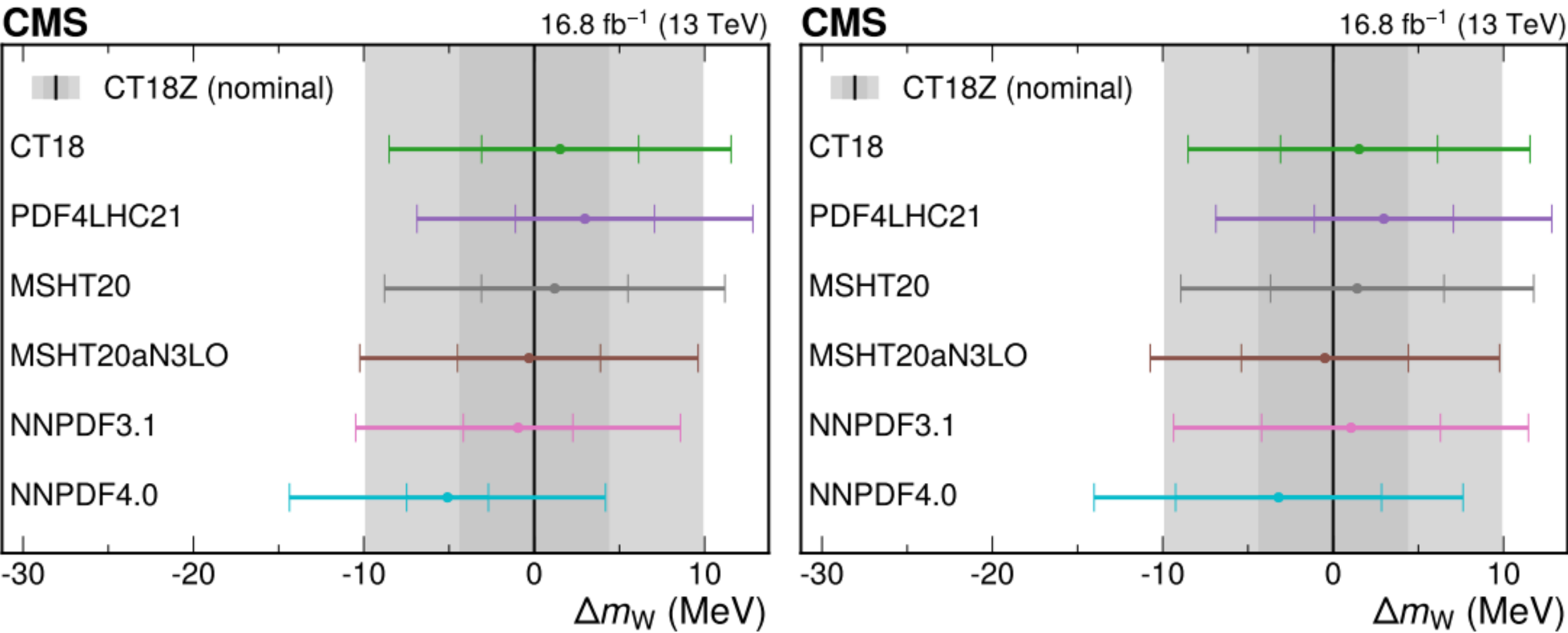
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- Similar situation in M_W determination [ATLAS-CONF-2023-004]
 $\Delta M_{W,\text{PDF}} = 7.7$ (14.6) MeV in $p_{T,l}(m_\tau)$ channel (CT18)
But
 $\delta M_{W,\text{PDFS}} = 17$ (21) MeV (shift MSHT20 versus NNPDF4.0)
- CMS M_W : inflate PDF uncertainties by a factor and profile with CMS data decreases shift between PDF set (but effectively giving much larger weight to a given measurement as compared to all experiments that determine PDFs in global fit)

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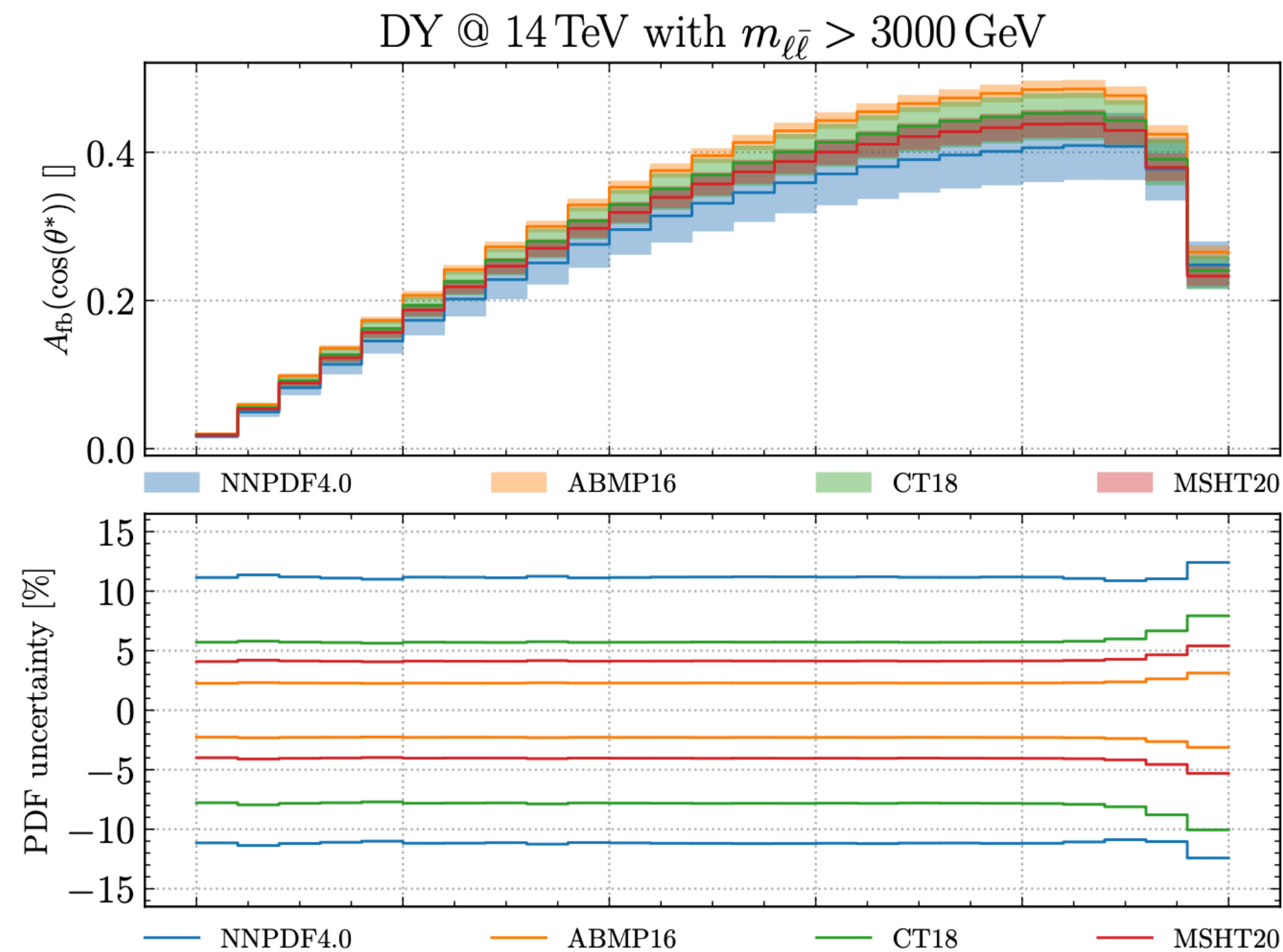
CMS collaboration, arXiv: 2412.13872

Can a better solution be achieved?
Simultaneous PDF-SM fits? Profiling over all data?

Significantly different results obtained when using different input PDFs.

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CHALLENGE #3: PRECISE PDFs FOR NEW PHYSICS SEARCHES



e. g. Heavy Z' search in DY Forward-Backward asymmetry

Ball et al arXiv: 2209.08115

$$x \approx \frac{M}{\sqrt{S}}$$

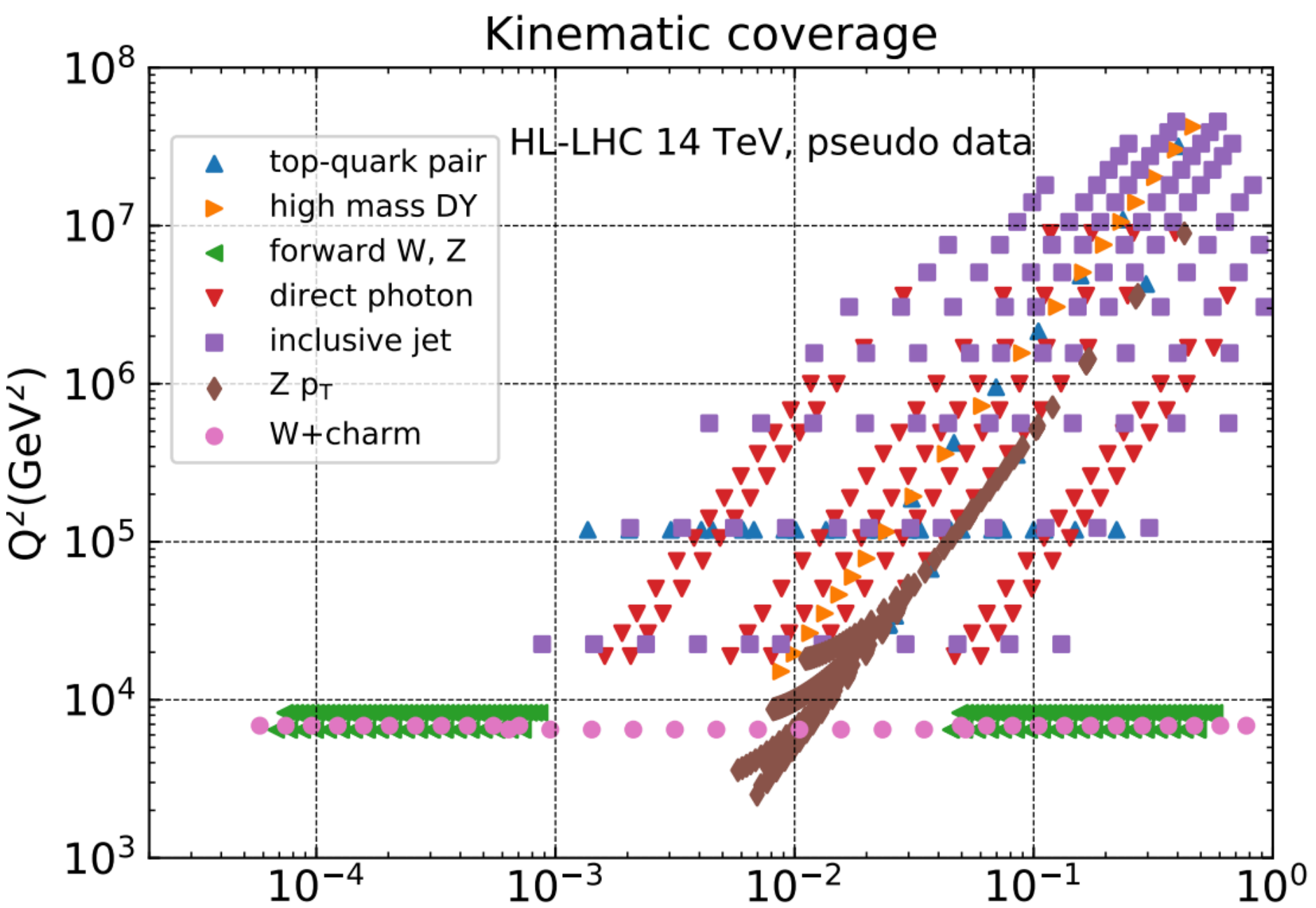
High-mass final states



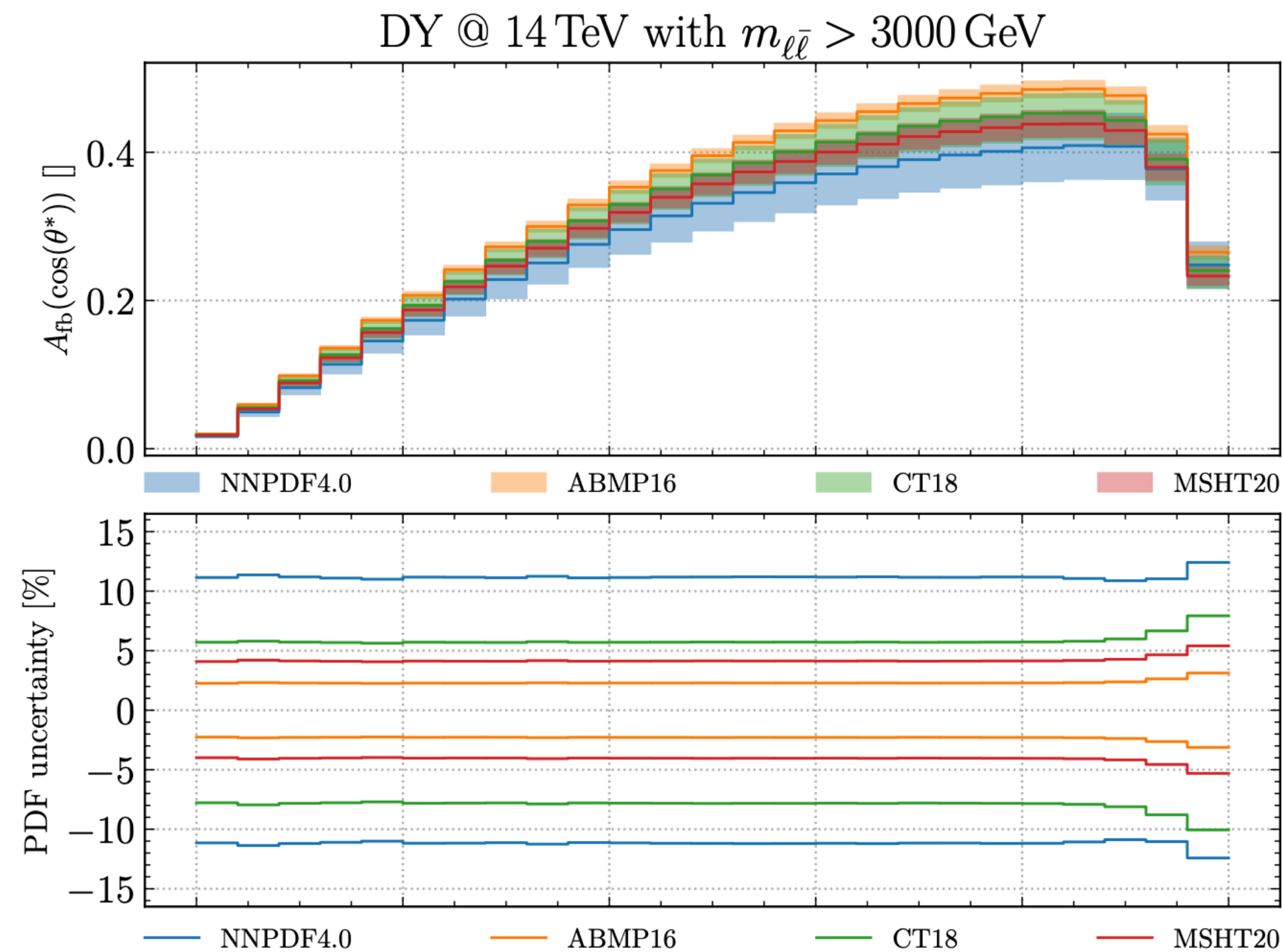
Large-x PDFs

- Large-x PDF affected by large uncertainties
- Reducing PDF uncertainties in large-x region is essential to characterise any possible new physics and to interpret deviations in the tails of experimental distributions
- Looking forward: **HL-LHC (and FCC-hh)**

Large x $\leftrightarrow$ Large E and/or Large Y



CHALLENGE #3: PRECISE PDFs FOR NEW PHYSICS SEARCHES



e. g. Heavy Z' search in DY Forward-Backward asymmetry

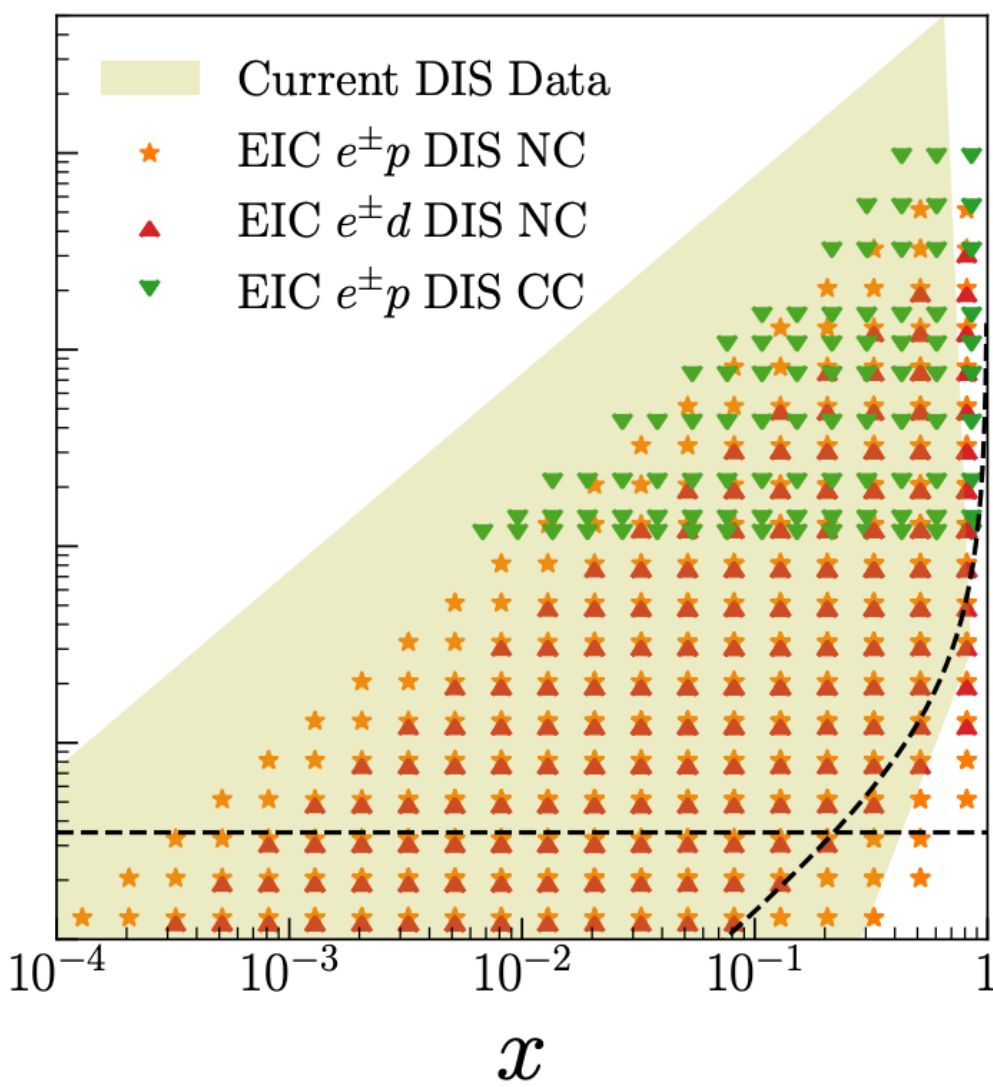
Ball et al arXiv: 2209.08115

$$x \approx \frac{M}{\sqrt{S}}$$

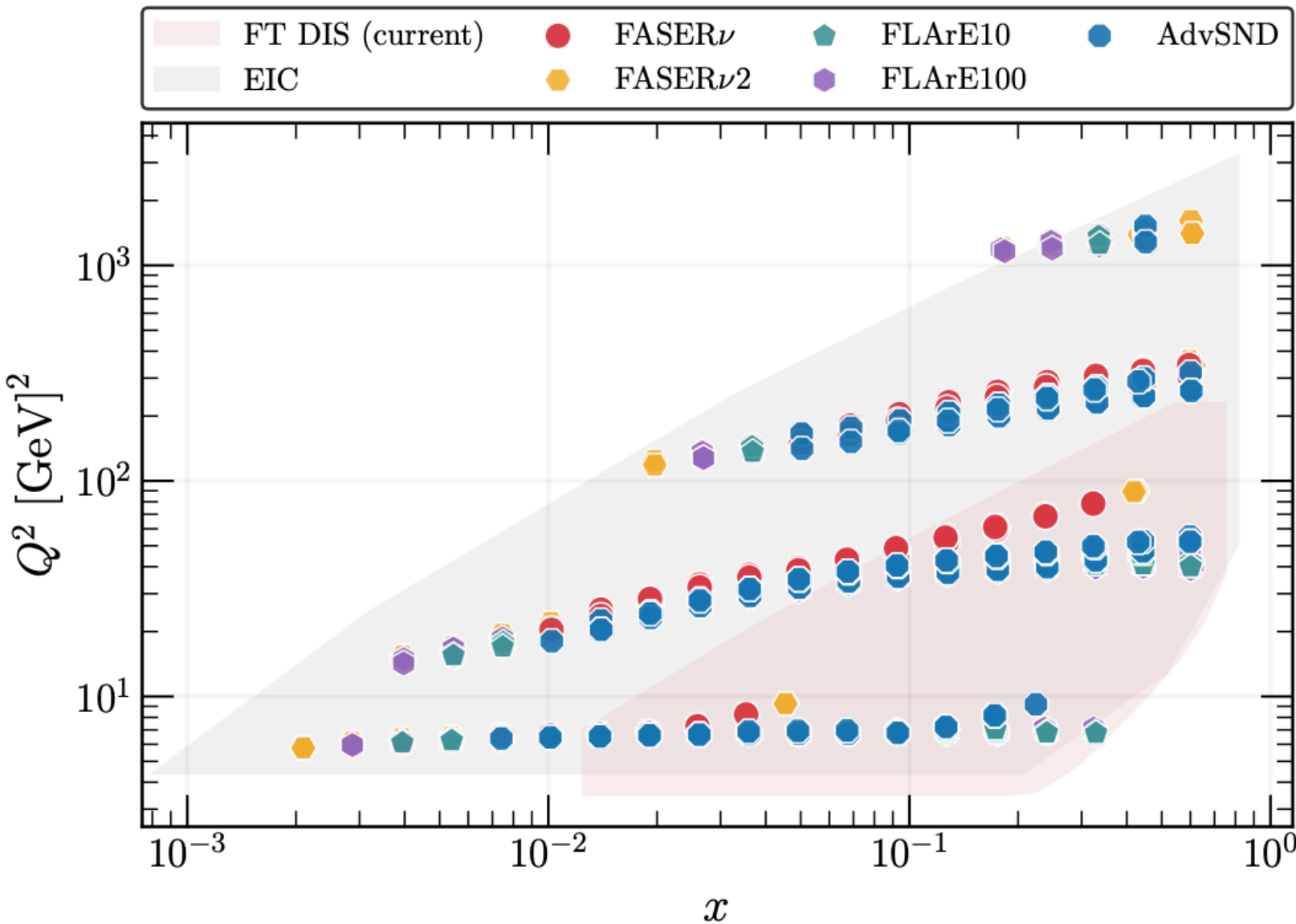
High-mass final states
 $\Leftrightarrow$
Large-x PDFs

- Large-x PDF affected by large uncertainties
- Reducing PDF uncertainties in large-x region is essential to characterise any possible new physics and to interpret deviations in the tails of experimental distributions
- Looking forward: **JLab, EIC, Forward Physics Facilities...**

Large x $\leftrightarrow$ Low/Medium E



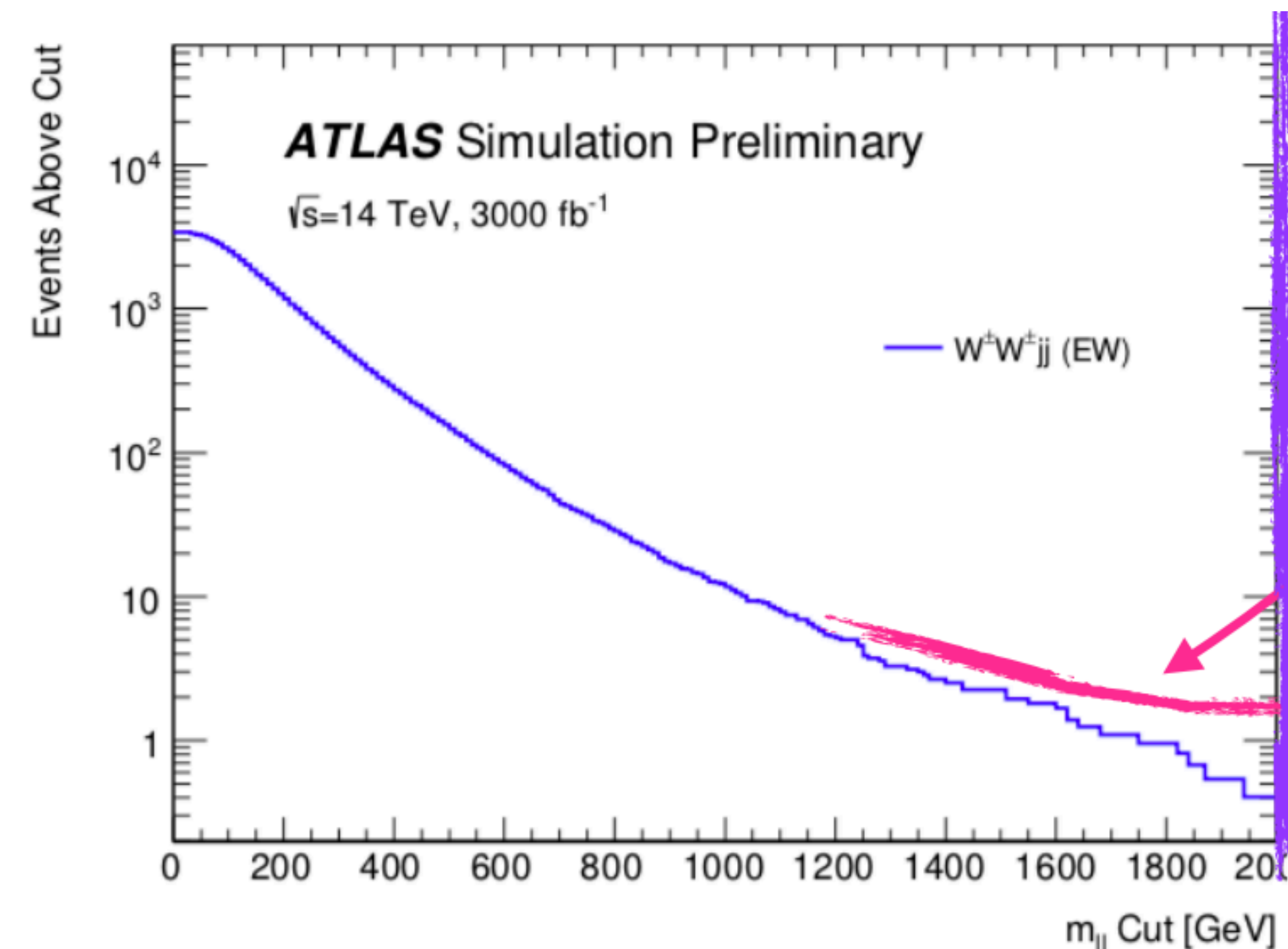
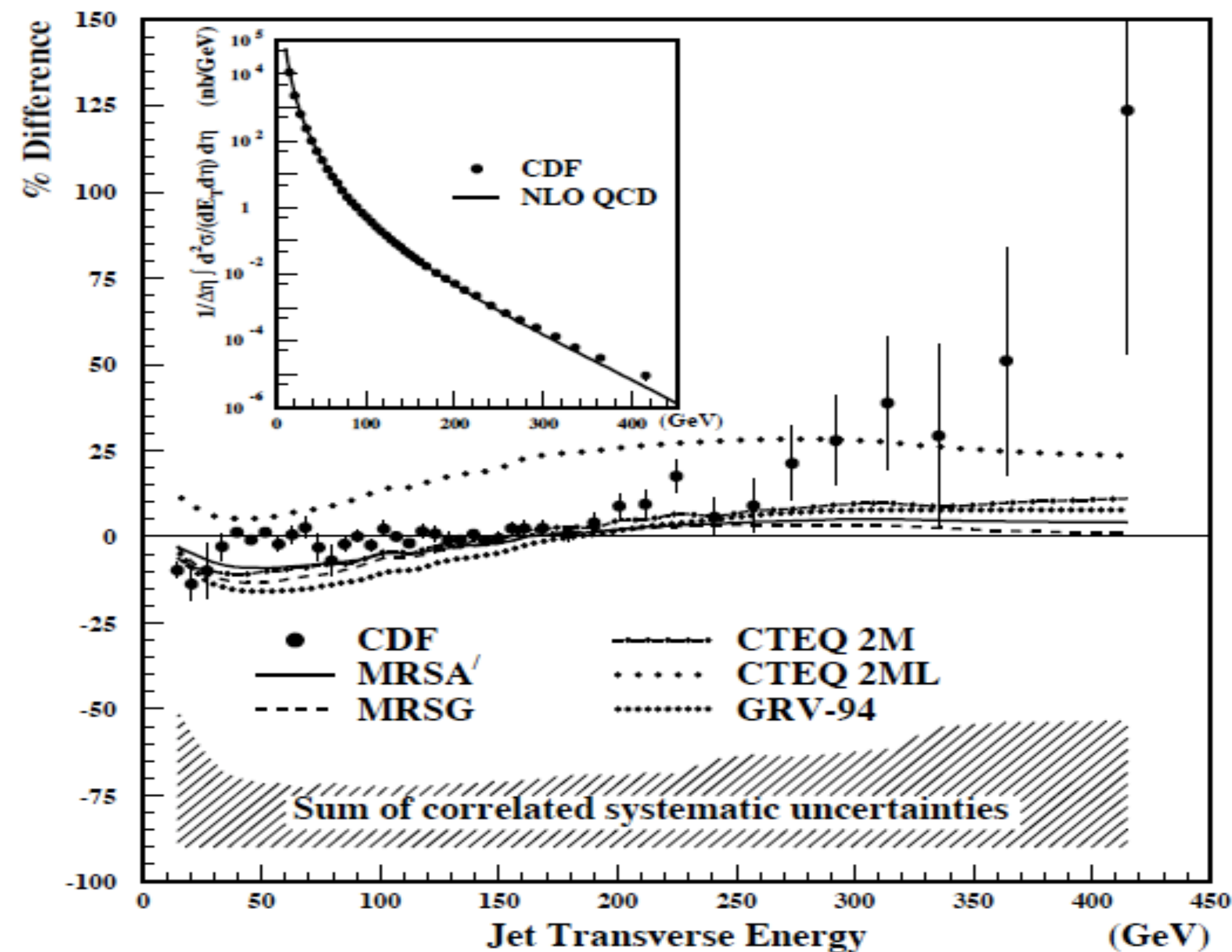
Khalek et al, 2102.00018



J Cruz-Martinez et al 2309.09581

CHALLENGE #3: PRECISE PDFS FOR NEW PHYSICS SEARCHES

17/19



CA Lee, HL/HE-LHC Jamboree, 1 March 2019

➡ Discrepancy between QCD calculation and CDF jets data (1995)

At that time no information on PDF uncertainties and theory predictions strongly depended on gluon shape at $x > 0.1$.
Once data included in the CTEQ fit, discrepancy disappeared.

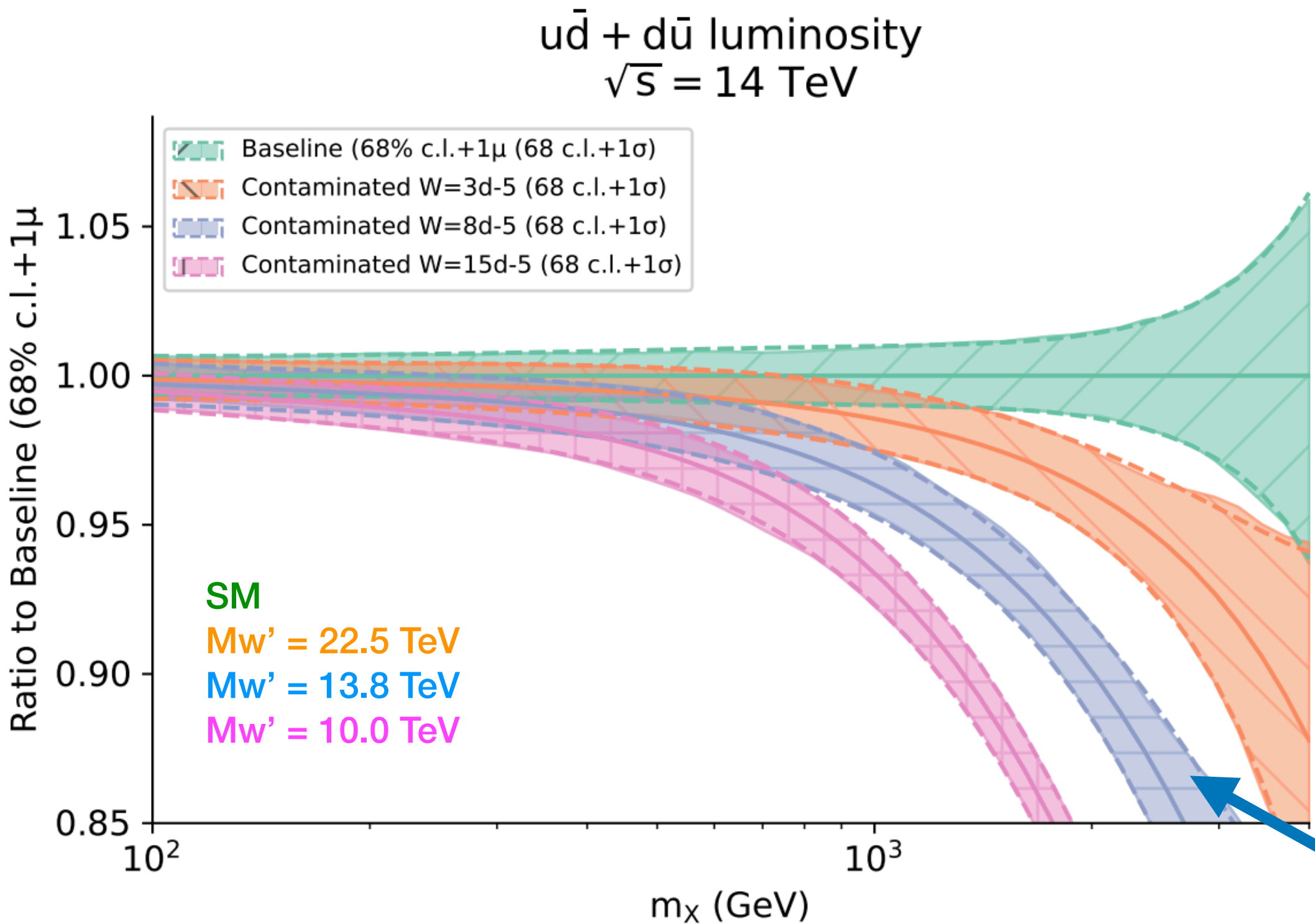
➡ Deviations from SM predictions in high energy tails (>2025)

New physics or limited understanding of proton structure?

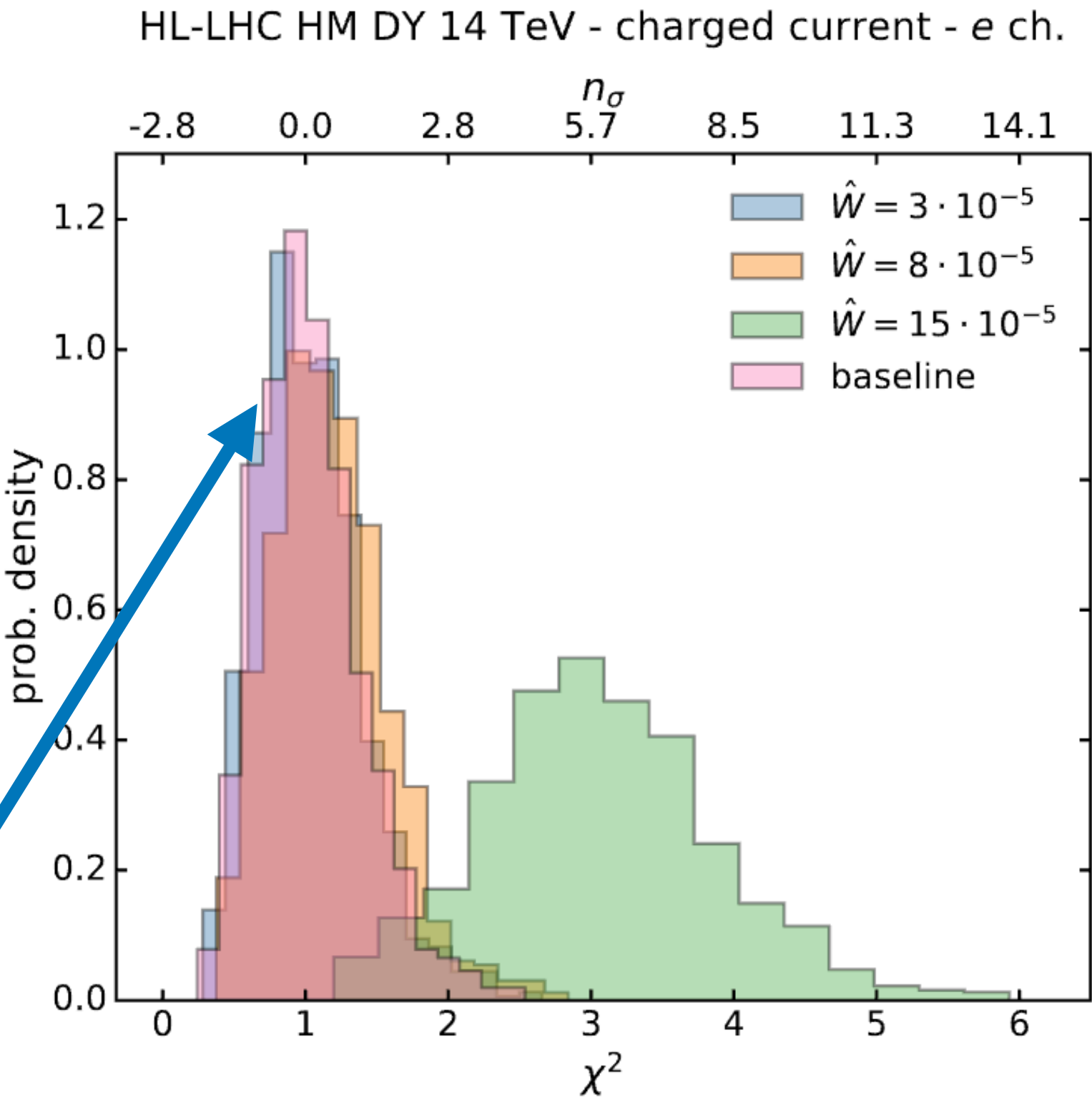
CHALLENGE #3: PRECISE PDFs FOR NEW PHYSICS SEARCHES

- Inject the “true” NP model and “true” PDFs in artificial data included in global fit
- Generate **HL-LHC** pseudo-data assuming “true” law of nature = “true” PDFs + “true” UV model
- Fit PDFs assuming SM
- **Can PDFs absorb signs of new physics? Yes**
- Important to tackle the issue (simultaneous fits, complementary constraints, test observables) and broaden understanding (gluon, strange)

Z'	W'
Selection test: 	Selection test: 
 Excluded from PDF fit	 Included in PDF fit
No impact on PDFs	PDFs contaminated



Max BSM bias
allowed by global fit
Without spoiling χ^2



CONCLUSIONS AND OUTLOOK

19/19

- In an era of precision at LHC, need precise and accurate PDFs
- Impressive advances in theory inputs and experimental inputs, pressure to validate and understand methodological differences.
- Tools like closure tests and generalisation tests are crucial to test methodology robustness, effects of possible experimental inconsistencies and even possible effects of new physics in the high energy tails
- Crucial reproducibility & open-source tools (and fitting codes)
- Much to look forward to at DIS2025 as far as PDFs are concerned

Updates from collaborations - [R. Thorne, O Zenaiev, T Hobbs, T R Rabemananjara WG1](#)

HQ schemes - [V. Bertone WG1](#)

Determination of α_S and PDFs - [R Stegeman, T Cridge WG1](#)

aN3LO combination - [T. Cridge WG1](#)

HL-LHC and other experiments synergies - [K Wichmann, MU WG1/6](#)

Higher twists - [A Accardi WG1](#)

Parametrisation studies - [A Courtoy WG1](#)

Closure tests with inconsistent data - [MU WG1](#)

Bayesian fits of PDFs - [L Mantani WG1](#)

... and much more!!

